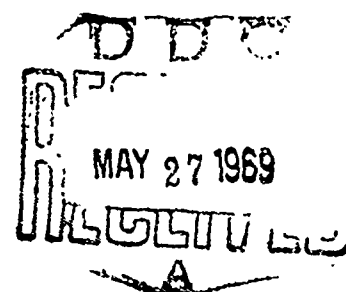


AD 688173

ENGINEERING STUDY OF  
BLAST-RESISTANT DOORS  
Submitted to  
U. S. CORPS OF ENGINEERS  
Protective Construction Branch  
Contract No. DA-49-129-ENG-434



by  
Charles D. Price  
Mosler Safe Co.  
30 November 1960

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### NOMENCLATURE

DLF	Dynamic Load Factor (to convert a given dynamic load to an equivalent static load)
E	Modulus of elasticity (psi)
$f_{dy}$	Dynamic yield strength of steel (psi)
I	Moment of inertia (inches <sup>4</sup> )
$K_L$	Load factor
$K_M$	Mass factor
$K_{LM}$	Load mass factor
k	Spring factor (kips/foot)
M	Bending moment (inch-pounds)
$P_r$	Reflected shock wave overpressure (psig)
$P_{so}$	Overpressure (psig)
S	Section modulus (inches <sup>3</sup> )
T	Time of idealized triangular load (seconds)
$T_n$	Natural period of oscillation (seconds)
t	Time in seconds
$t_+$	Positive phase duration (seconds)
$U_o$	Shock front velocity (feet per second)

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## SYNOPSIS

This final report is the nuclear-blast-resistant door section of a study, which also includes blast valve closures, under Contract DA-49-129-ENG-434 with the Protective Construction Branch, U. S. Corps of Engineers, Washington, D. C. Blast valve closures were covered in a separate report. (1)

The purpose of this report is to evaluate various existing blast-resistant door designs and then to select the optimum door designs for the door sizes, types, and blast pressure ratings specified in the contract, taking into consideration economy, ease of manufacture from standard available materials, reliability of operation, and a minimum amount of maintenance.

From the optimum door designs complete drawings and specifications were prepared suitable for competitive bidding and manufacture.

This report summarizes the results of the Interim Blast Door Study (2) which included detailed preliminary design calculations, sketches, and comparisons.

## SECTION I - SCOPE OF WORK

The criteria specifies 25, 50, and 100 psi overpressures (see Figures I-1, I-2, and I-3, which are compiled from item 3 in the Bibliography), with full reflected pressures to be withstood elasto-plastically by the doors, which are to be operable after three blasts under conditions of moisture and extremes of temperature with a minimum of maintenance.

The door sizes and types to be considered are as follows (see Figure I-4):

- A. Pedestrian door 3'-6" wide x 7'-0" high, single-leaf, side-hinged
- B. Pedestrian door 6'-0" wide x 7'-0" high, double-leaf, side-hinged
- C. Vehicular door 8'-0" x 8'-0", double-leaf, side-hinged
- D. Vehicular door 12'-0" x 12'-0", single- and double-leaf, sliding
- E. Rail and truck door 14'-0" wide x 18'-0" high, single-leaf, sliding
- F. Hatch door 3'-0" x 3'-0", single-leaf, side-hinged, suitable for horizontal or vertical mounting
- G. Service tunnel door 2'-6" wide x 4'-0" high, single-leaf, hinged

Door sizes mentioned above are clear opening sizes. The 12'-0" x 12'-0", 25 psi rating, double-leaf, sliding door is powered by a manually operated hand chain geared trolley. The 12'-0" x 12'-0", 50 and 100 psi rating, single-leaf sliding doors, and the 14'-0" x 18'-0", 25, 50, and 100 psi rating, single-leaf sliding doors are powered by electric motor drives with an emergency manual handwheel drive.

The remainder of the doors are manually opened and shut, either single or double-leaf. By using bank-vault-door type three-way adjustable hinges, the door leaves are easily opened and shut by one person with just a few pounds pull on the door handle, even though the door leaf may weigh 5 tons or more.

The doors were designed complete with frame and hardware. Doors and frames (except for sliding doors) were designed as integral units. The frames are of a one-piece box construction. The doors are designed to be mounted in the door frames, adjusted and operated at the factory, and shipped together as one unit, thus insuring proper fit and operation on the job.

Doors are also designed to resist a 25% maximum rebound force, except where calculations indicate a greater percentage, in which case the calculated figure is used. The rebound force is taken care of by a bank-vault-door type locking bolt mechanism.



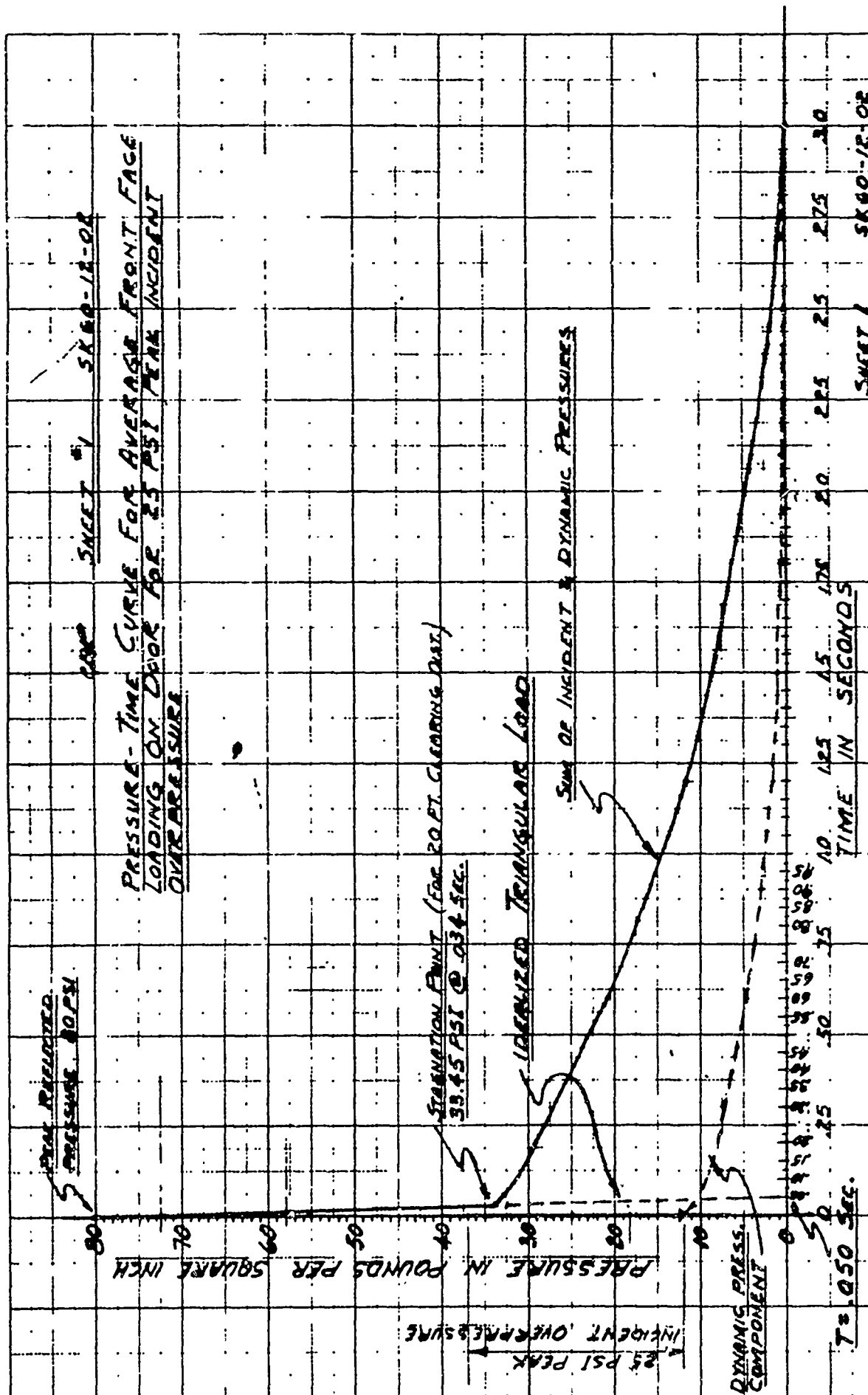


Figure I-1

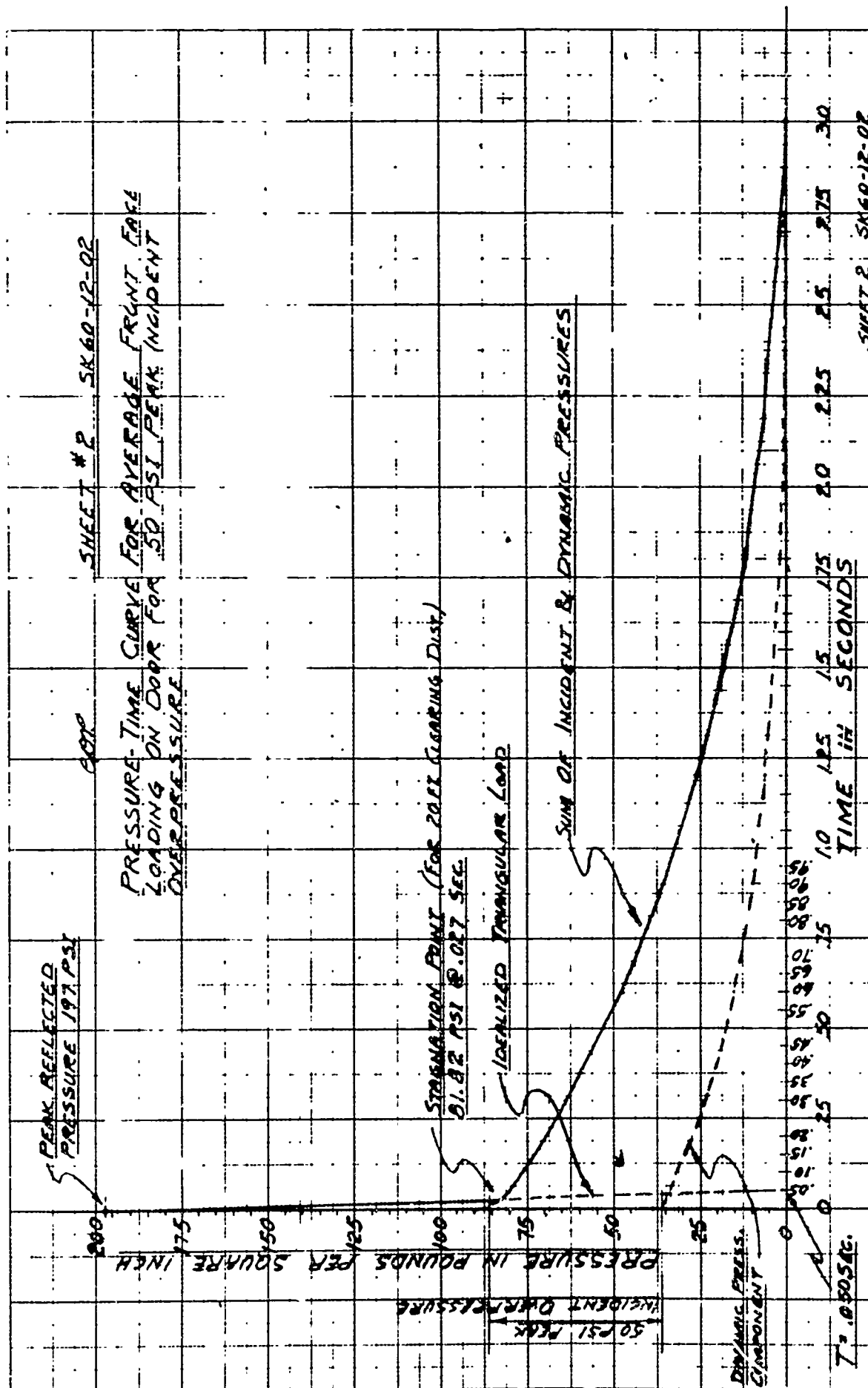


Figure I-2

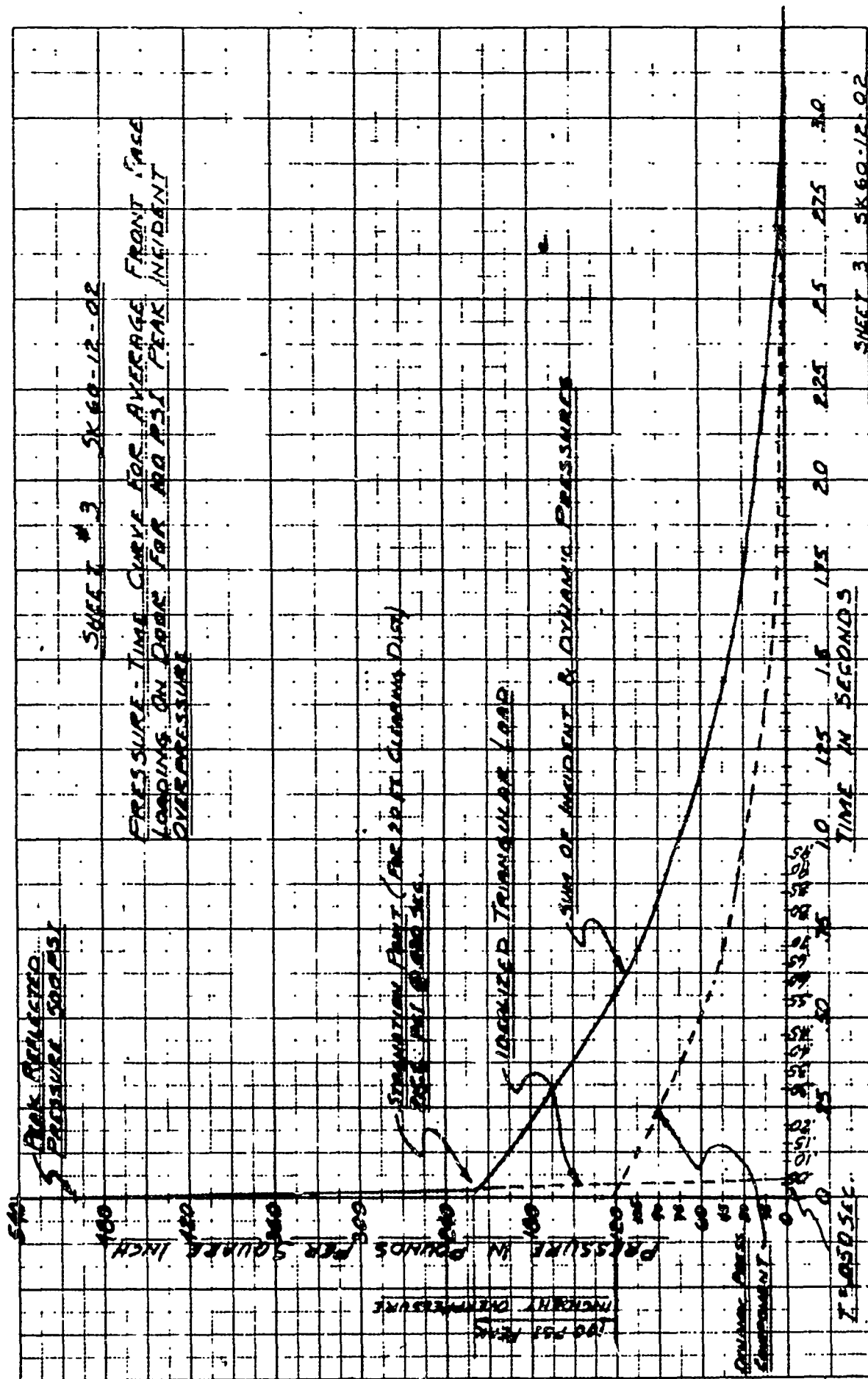
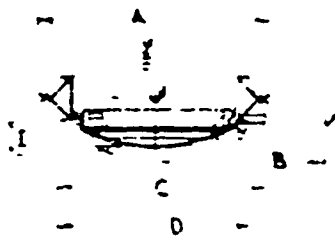
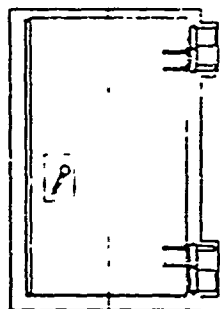


Figure I-3

CEP INC. SL. FR. SH. E. CO.

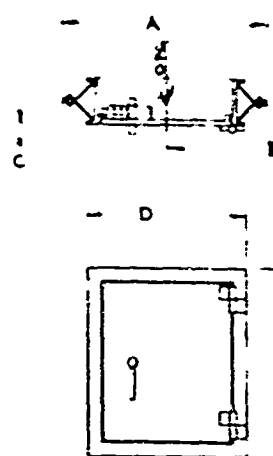


- DISTANCE NECESSARY FROM  
E OPG TO WALL TO OBTAIN  
FULL CLEAR OPG WHEN DOOR  
IS OPEN

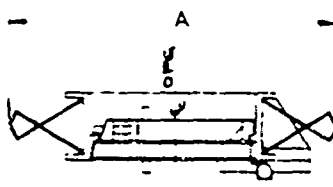


FLOOR LEVEL

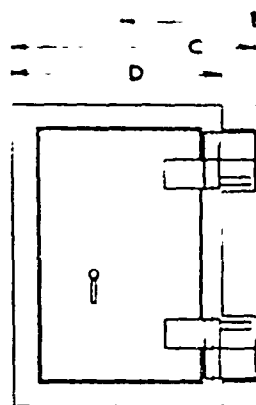
SIZE	PRESSURE	A	B	C	D	E	F	G	H	I	SHIPPING WT.
3'-6" x 7'-0"	25 PSI	64	58 1/2	57 1/2	52	12	91 1/2	102 1/2	5/8	9 3/8	2300



SIZE	PRESSURE	A
3'-0" x 3'-0"	25 PSI	61 1/2
3'-0" x 3'-0"	50 PSI	67
3'-0" x 3'-0"	100 PSI	84
2'-6" x 4'-0"	25 PSI	56
2'-6" x 4'-0"	50 PSI	60 1/2
2'-6" x 4'-0"	100 PSI	68 1/2



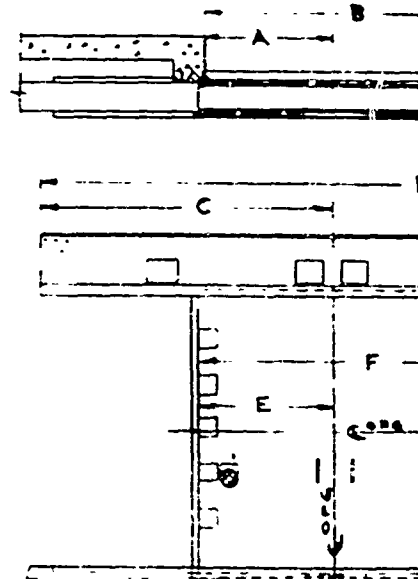
DISTANCE NECESSARY  
FROM E OPG TO WALL TO  
OBTAIN FULL CLEAR OPG  
WHEN DOOR IS OPEN



- E -

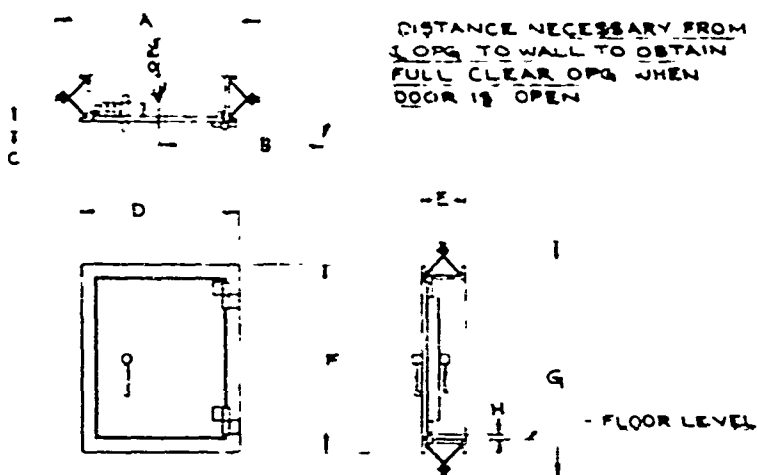
FLOOR  
LEVEL

SIZE	PRESSURE	A	B	C	D	E	F	G	H	I	SHIPPING WT.
3'-6" x 7'-0"	50 PSI	71 1/2	44	63 1/2	55 1/2	18	95 1/2	111 1/2	5/8	4 1/2	6000
3'-6" x 7'-0"	100 PSI	83 1/2	68	64 1/2	58 1/2	24	98 1/2	124 1/2	5/8	4 1/2	10400

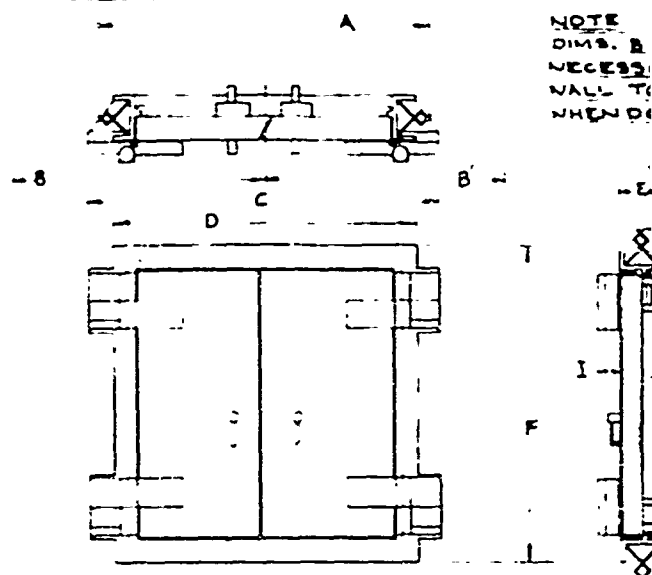


SIZE	PRESSURE	A
12'-0" x 12'-0"	25 PSI	6'-0"

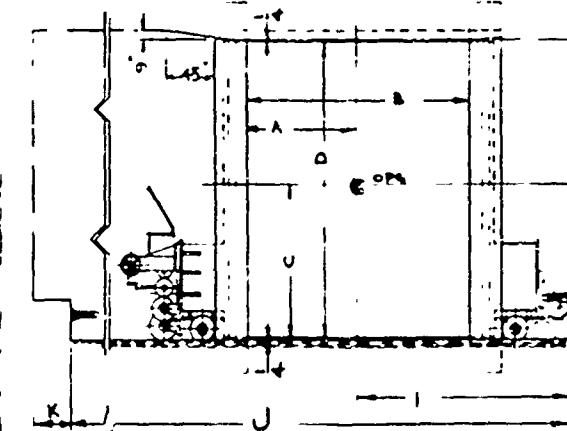
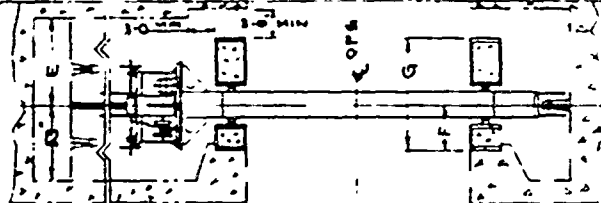
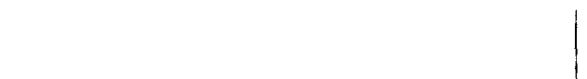
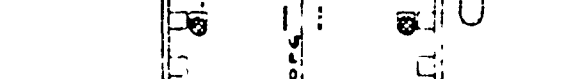
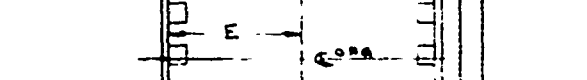
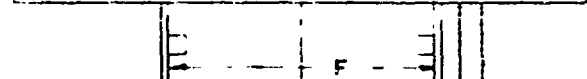
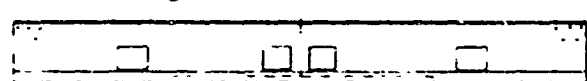
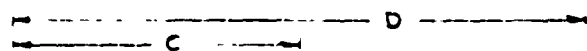
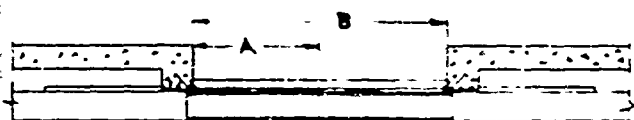
A



SIZE	PRESSURE	A	B	C	D	E	F	G	H	SHIPPING WT.
3'-0" x 3'-0"	25 PSI	61 1/2	55 1/2	3 1/2	45 1/2	12	4 1/2	60 1/2	5/8	880
3'-0" x 3'-0"	50 PSI	67	55 1/2	3 1/2	45 1/2	18	4 1/2	66	5/8	3000
3'-0" x 3'-0"	100 PSI	84	55 1/2	3 1/2	46 1/2	24	4 1/2	72 1/2	5/8	3200
2'-6" x 4'-0"	25 PSI	56	46 1/2	2 1/2	41 1/2	12	3 1/2	72 1/2	5/8	1400
2'-6" x 4'-0"	50 PSI	60 1/2	47	3	40 1/2	18	3 1/2	77 1/2	5/8	3000
2'-6" x 4'-0"	100 PSI	68 1/2	47	3 1/2	40 1/2	24	3 1/2	83 1/2	5/8	4400



SIZE	PRESSURE	A	B	B'	C	D	E	F	G	H	I
6'-0" x 7'-0"	25 PSI	91 1/2	36 1/2	38	99 1/2	85 1/2	12	57 1/2	104 1/2	7/8	4 1/2
6'-0" x 7'-0"	50 PSI	102 1/2	40	40	99 1/2	83 1/2	18	57 1/2	96 1/2	5/8	4 1/2
6'-0" x 7'-0"	100 PSI	105 1/2	40	41	104 1/2	86 1/2	24	98 1/2	120 1/2	1 1/2	5 1/2
8'-0" x 8'-0"	25 PSI	102 1/2	47	49 1/2	123 1/2	109 1/2	12	109 1/2	117 1/2	8	4 1/2
8'-0" x 8'-0"	50 PSI	29 1/2	50	56 1/2	134 1/2	110 1/2	18	110 1/2	126 1/2	1 1/8	6 1/2
8'-0" x 8'-0"	100 PSI	137 1/2	50	54 1/2	134 1/2	112 1/2	24	104 1/2	137 1/2	1 3/8	6 1/2



SIZE	PRESSURE	A	B	C	D	E	F	G	H	I	SHIPPING WT.
12'-0" x 12'-0"	25 PSI	6'-0"	12'-0"	11'-6"	27'-0"	6'-3"	12'-6"	6'-0"	12'-0"	13'-4"	35 500

SIZE	PRESSURE	A	B	C	D	E	F	G	H	I	J
12'-0" x 12'-0"	50 PSI	6'-0"	12'-0"	6'-0"	12'-0"	5'-7"	3'-11"	9'-3"	17'-0"	12'-6"	44-10
12'-0" x 12'-0"	100 PSI	6'-0"	12'-0"	6'-0"	12'-0"	5'-7"	4'-6"	11'-7"	17'-0"	12'-6"	44-10
14'-0" x 18'-0"	25 PSI	7'-0"	14'-0"	9'-0"	18'-0"	5'-7"	2'-7"	4'-1"	22'-0"	14'-4"	50-4
14'-0" x 18'-0"	50 PSI	7'-0"	14'-0"	9'-0"	18'-0"	6'-2"	4'-0"	6'-6"	22'-0"	14'-4"	51-7
14'-0" x 18'-0"	100 PSI	7'-0"	14'-0"	9'-0"	18'-0"	6'-7"	3'-8"	6'-10"	24'-0"	14'-1"	54-4

**GENERAL NOTES**  
 PRESSURE SHOWN ARE  
 INCIDENT BLAST OVER PRESSURE  
 DOORS DESIGNED TO RESIST  
 FULL REFLECTED PRESSURES

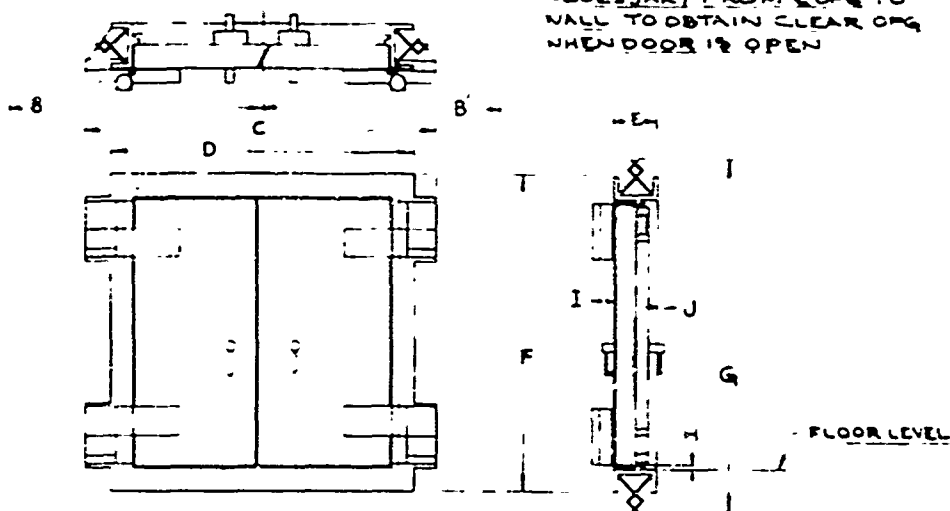
REVISIONS 6-6-60

DESIGNED BY  
 C. Olen  
 CHECKED BY  
 C. Olen  
 DATE  
 6/6/60

TITLE  
 101A  
 101

SEE RV FROM  
TO OBTAIN  
PQ WHEN

NOTE  
DIMS. B & B' DISTANCE  
NECESSARY FROM LOGS TO  
WALL TO OBTAIN CLEAR OPG  
WHEN DOOR IS OPEN



FLOOR LEVEL

FLOOR LEVEL

SHIPPING WT.

SIZE	SHIPPING WT.
6-0	850
6-0	3000
6-0	3200
6-0	1400
6-0	3000
6-0	4400

SIZE	PRESSURE	A	B	B'	C	D	E	F	G	H	I	J	SHIPPING WT
6-0' x 7-0'	25 PSI	91 1/2	36 1/2	38	99 1/2	85 1/2	12	57 1/2	104 1/2	5 1/8	4 3/4	3 1/2	8000
6-0' x 7-0'	50 PSI	102 1/2	40	40	99 1/2	83 1/2	18	57 1/2	96 1/2	5 1/8	4 3/4	—	13,100
6-0' x 7-0'	100 PSI	105 1/2	40	41	104 1/2	86 1/2	24	98 1/2	120 1/2	1 1/2	5 1/2	—	19,600
8-0' x 8-0'	25 PSI	116 1/2	47	49 1/2	123 1/2	109 1/2	12	109 1/2	117 1/2	7 1/8	4 3/4	3 1/2	13,900
8-0' x 8-0'	50 PSI	29 1/2	50	56 1/2	134 1/2	110 1/2	18	118 1/2	126 1/2	1 1/8	6 1/2	—	19,000
8-0' x 8-0'	100 PSI	137 1/2	50	54 1/2	134 1/2	112 1/2	24	110 1/2	137 1/2	1 1/8	6 1/2	—	42,250

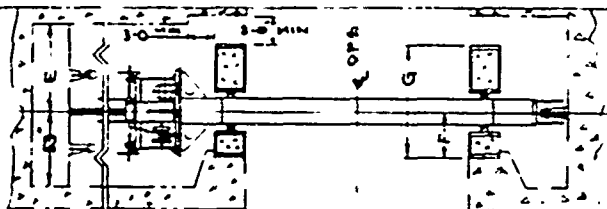
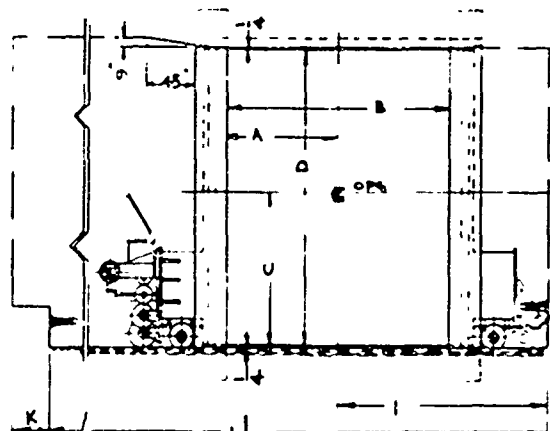
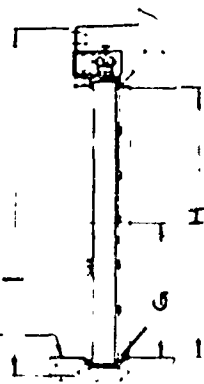
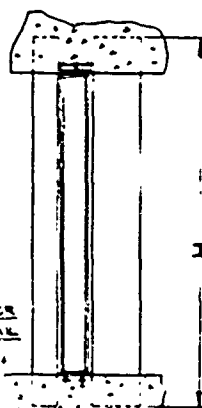


Figure I-4



EXTRA WHEN DOOR  
IS USED FOR RAIL  
ROAD CARS  
(4 X 12 DOOR ONLY)



SIZE	SHIPPING WT
12-0	35,500

SIZE	PRESSURE	A	B	C	D	E	F	G	H	I	J	K	SHIPPING WT
12-0' x 12-0'	50 PSI	6-0'	12-0'	6-0'	12-0'	5-7'	3-11'	9-5'	17-0'	12-6'	44-10'	2-4'	124,500
2-0' x 12-0'	100 PSI	6-0'	12-0'	6-0'	12-0'	5-7'	4-6'	11-7'	17-0'	12-6'	44-13'	2-4'	152,500
14-0' x 18-0'	25 PSI	7-0'	14-0'	9-0'	18-0'	5-7'	2-7'	4-6'	22-0'	16-4'	50-4'	2-4'	115,000
14-0' x 18-0'	50 PSI	7-0'	14-0'	9-0'	18-0'	6-2'	4-0'	6-6'	22-0'	16-6'	51-7'	2-4'	180,008
14-0' x 18-0'	100 PSI	7-0'	14-0'	9-0'	18-0'	5-7'	3-8'	13-10'	24-0'	16-1'	54-4'	2-4'	294,000

FIGURE HAS G-G-60

GENERAL NOTES  
PURE SHOWN ARE  
INT BLAST OVER PRESSURE  
& DESIGNED TO RESIST  
REFLECTED PRESSURES

DESIGNER  
CHECKED BY  
DATE  
SCALE

THUSLER HAMILTON OHIO  
TITLE STD DOOR TYPE  
BLAST RES STANT DOORS  
B-450318

## SECTION II - REVIEW OF EXISTING ELAST DOORS STUDIED

Rather than a detailed list of all door drawings available for study (which would be unduly voluminous), a representative cross-section of various doors is presented.

<u>Drawing</u>	<u>Description</u>
Ammann & Whitney 60-02-058, Sheet #18 5'-4" x 7'-2" opening Side-hinged	Constructed of 8" channel and beams running short way of door with 3/8" outer plate and 1/4" back plate. 3 side hinges, 3 separate manual latches, and rubber gasket.
Ammann & Whitney 60-02-58, Sheet #17 10'-0" x 14'-0" sliding door	Constructed of 14" @ 43 WF beams running long way of door with 3/8" outer plate and 1/4" back plate. Runs on three 2-ton trolleys. Sealing gasket and turnbuckle anchor dogs.
Ammann & Whitney Sheet #1 & Sheet #2 6'-0" x 8'-0"	Constructed of 8" thick solid steel plate. Moved on double flanged wheels on bottom of door. Sliding door.
Black & Veatch 33-15-58, Sheet #9 12'-0" x 12'-0" Double sliding door	Constructed of 12" "I" beams running long way. 9/16" thick steel plates front and back. Runs on trolleys. 3/16" x 1-1/2" rubber-impregnated canvas belting for seals.
Black & Veatch 33-03-15, Sheet #8 3'-0" x 6'-8"	Constructed of 4" channels running short way of door with 3/8" thick steel plates front and back. Spring bronze seals. Side hinged door.
Black & Veatch 33-03-15, Sheet #7 8'-0" x 8'-0"	Constructed of 6" "I" beams running long way with 5/8" thick steel plates front and back. Spring bronze seals. Double-leaf, side-hinged door.

DrawingDescription

Lorenzo S. Winslow  
49-100-9  
3'-0" x 6'-6"  
Side-hinged

Constructed of structural tees, ST 5 I's running short way and ST 5 B's running long way, with 7/16" thick steel outer plate and 1/4" thick steel back plate.

Lorenzo S. Winslow  
49-100-9  
4'-8" x 6'-6"  
Side-hinged

Double door, constructed of structural tees, ST 5 I's running long way and 5" x 1-1/8" bars running short way, with 1/2" thick steel outer plate and 1/4" thick steel back plate.

Leo A. Daly  
A-11  
7'-9" high  
Single- and Double-  
leaf, side-hinged

Constructed of 1/4" thick steel plate with 3" x 2" x 1/4" angle frame, with canvas-covered rubber gasket and refrigerator type handle and latch.

General Services  
Administration  
49-100-9  
3'-8-1/2" x 6'-7-1/8"  
Side-hinged

6-11/16" thick door consists of structural tees, ST 6 I's running short way and ST 6 B's running long way, with 6" channel outer frame, with 7/16" thick steel outer plate and 1/4" thick steel back plate.

General Services  
Administration  
49-100-9  
2'-8" x 6'-7"  
Side-hinged

5-11/16" thick door consists of structural tees, ST 5 I's running short way and ST 5 B's running long way, with 5" channel outer frame, with 7/16" thick steel outer plate and 1/4" thick steel back plate.

Faulkner, Kingsbury,  
& Stenhouse

13 various size doors consisting of 5/8" or 7/8" thick solid steel plate on outer or hinge side and an outside frame of 3-1/2" x 1" steel bar with a 1/8" steel back cover plate.

Daniel, Mann, Johnson  
& Mendenhall &  
Associates  
AP-1511/16  
5'-0" x 7'-0"

2" thick curved steel plate, side-hinged door.



From the preceding summary of existing door designs, the following generalities are obtained:

1. Large doors are of built-up construction with a heavy front and back steel plate, with structural steel beams between the plates.
2. Built-up-construction doors feature more one-way construction than two-way construction. On double-leaf doors the one-way construction runs the long way of the door due to the one edge of the door being unsupported.
3. Built-up-construction doors with two-way reinforcement feature a "tee" beam reinforcement which allows the leg of the tee to be welded to one plate and the other plate to be slotted and welded to the flange of the tee from the outside, overcoming what would otherwise be a fabrication problem. Two-way reinforcement is very much in the minority, however.
4. Small or medium strength and size doors might be made of a solid steel plate as well as of a built-up fabrication.
5. There is a wide variety of hinges and latching devices, practically none of which appear adequate and capable of withstanding significant rebound forces.
6. Little progress has been made in the design of doors departing from conventional designs, such as curved doors or prestressed concrete doors.

Of considerable interest, in addition to the above-mentioned doors, is a particular door design which was successfully tested in 1957 in "Operation Plumbob" at the Nevada Test Site under very high pressures. This was a standard bank vault door, a Mosler Safe Co. C-10 door. The damage to the door was only superficial, peeling off ornamental trim, etc., the door being reopened without any difficulty. The interior of the above-ground vault was entirely protected by the door. Although the concrete covering of the vault was badly damaged, the steel lining of the vault kept it air tight. This door is shown in Figures II-1, II-2, II-3, II-4, and II-5.

NOT REPRODUCIBLE

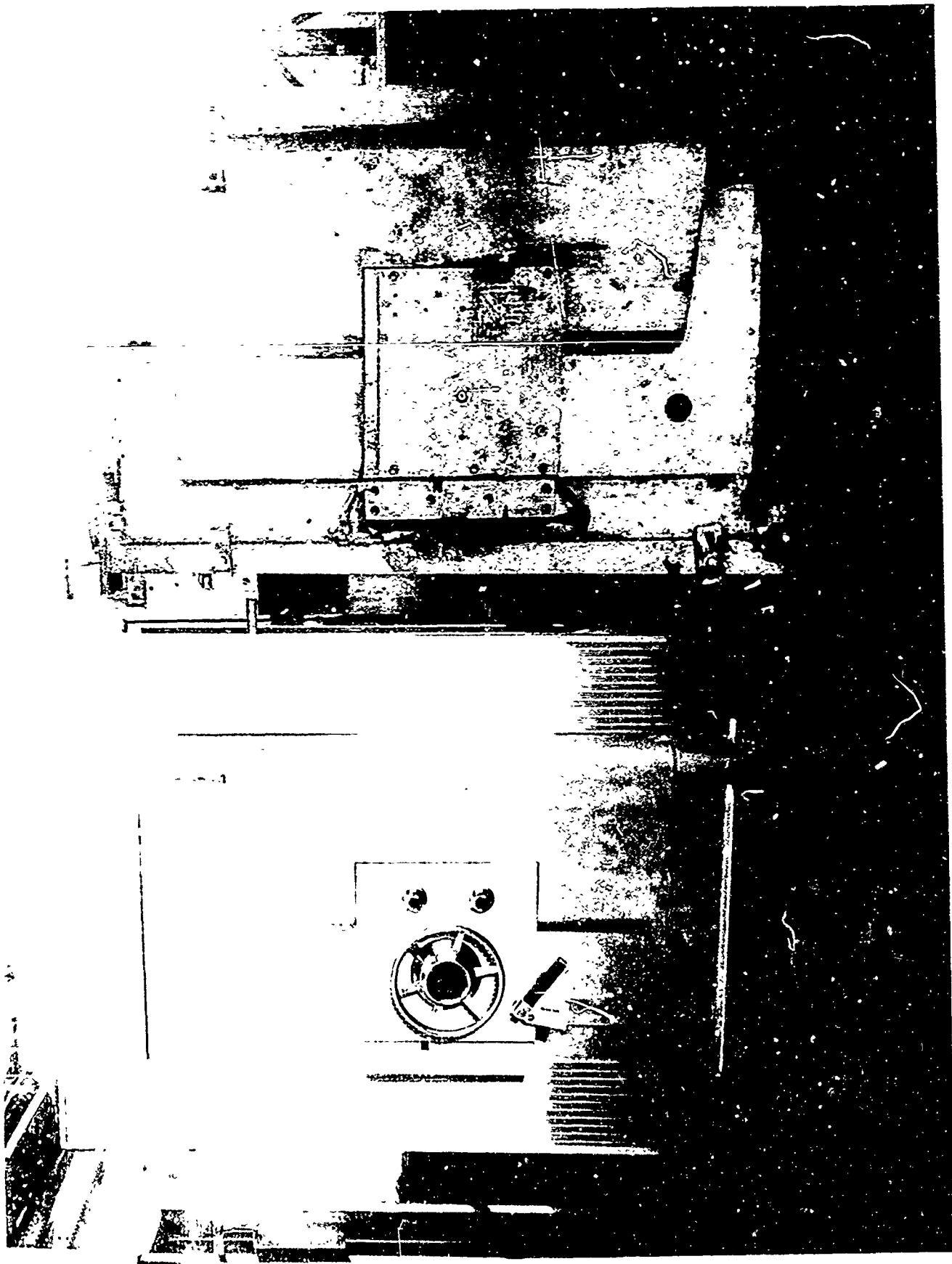


Figure II-1

NOT REPRODUCIBLE

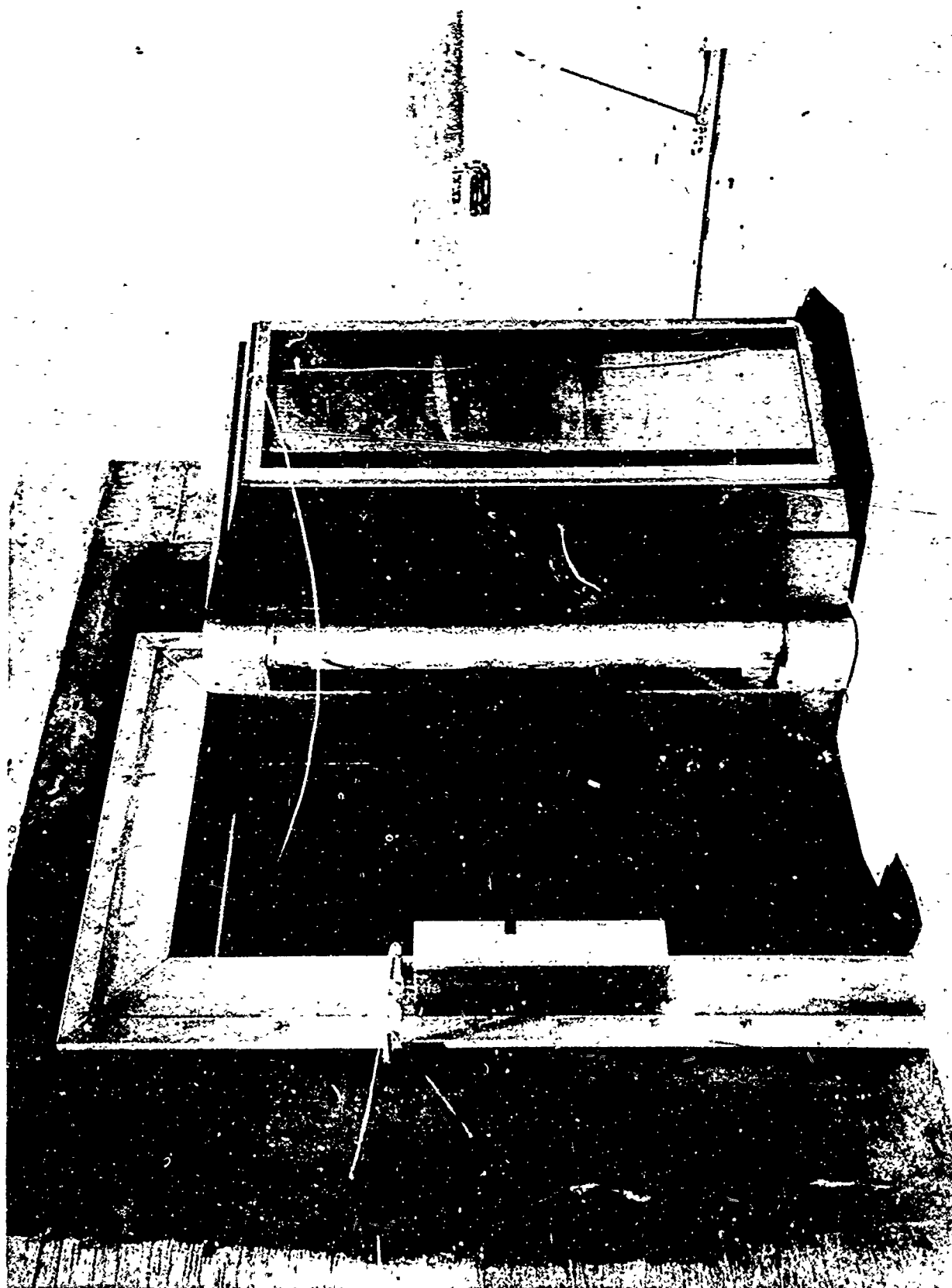


Figure II-2

NOT REPRODUCIBLE



Figure II-3

NOT REPRODUCIBLE

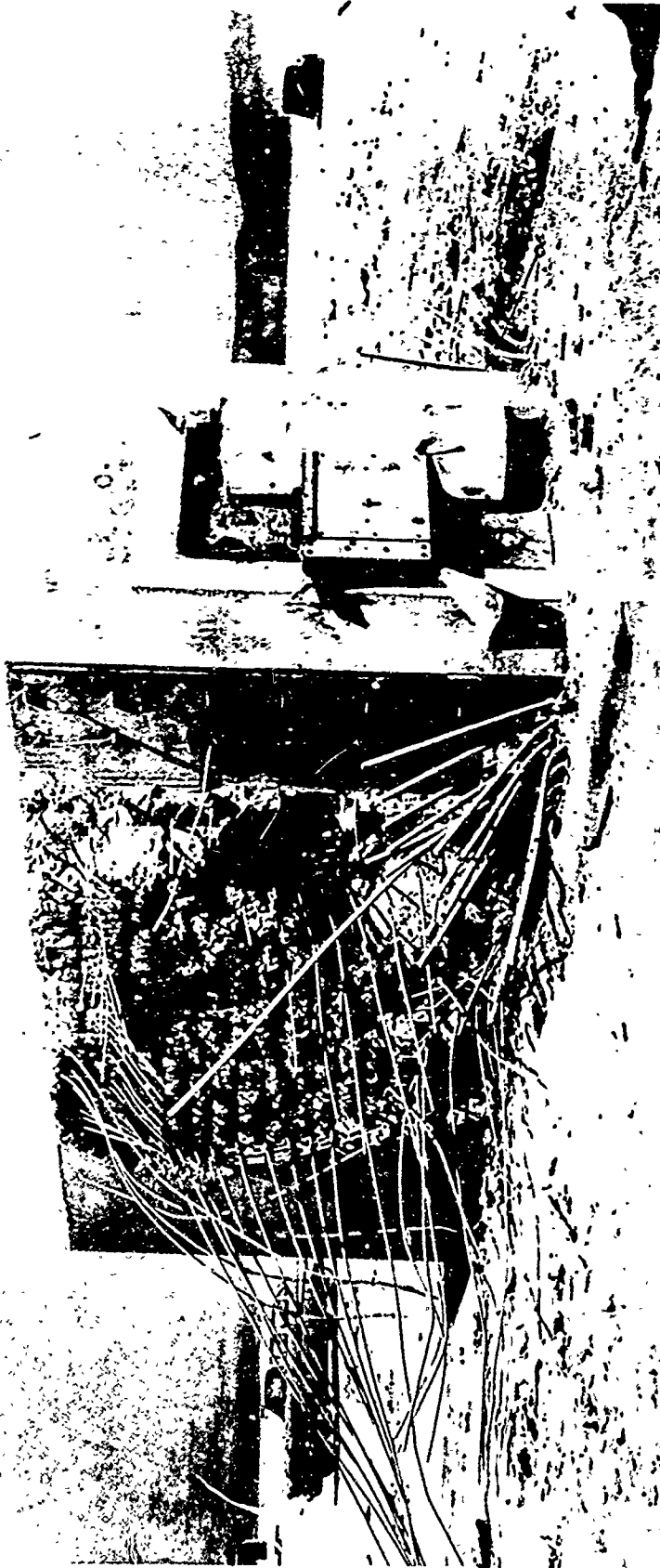


Figure II-4

NOT REPRODUCIBLE



Figure II-5

### SECTION III - COMPARISON OF DOOR DESIGNS AND FINAL DOOR DESIGN SELECTIONS

There are several possibilities of door designs and materials. Possible designs included:

- A. Solid flat plate door leaves
- B. One-way reinforced built-up welded door leaves
- C. Two-way reinforced built-up welded door leaves
- D. Curved door leaves

Possible materials for door leaves included:

- A. Aluminum
- B. Concrete
- C. Plastic
- D. Steel

Referring to Interim Blast-Resistant Door Study (2), for reasons of economy and ease of fabrication, steel was selected as the best material.

Likewise, for the various possible door designs, the one-way reinforced built-up welded door leaf design was selected for all but the lighter section doors. For these doors it was found more economical to use the solid steel flat plate design.

For easy swinging of the hinged type doors, only two hinges should be used for best performance and ease of operation. The bottom hinge contains radial-thrust bearings to take all the downward weight of the door and half of the radial (horizontal) thrust which is due to the rotational effect of the overhang of the door.

The upper hinge takes only the other half of the radial (horizontal) thrust (which is actually a couple). This construction, by relieving the upper hinge bearing of any thrust loads, allows adjustment of the hinge in a vertical direction without danger of overloading the bearings by the adjusting screws. In

some designs studied the weight of the door was evenly divided by thrust bearings in the upper and lower hinges, which could result in overloaded hinge bearings if there is a slight misalignment or if one of the vertical adjusting screws is turned too far so that the screw is trying to "jack" against the two bearings and force them apart. In other door designs studied there were three hinges per door leaf, which made this problem even worse. In the final hinged door design the upper hinge bearing "floats" vertically on the hinge pin and is therefore unaffected by vertical adjustment or misalignment.

The top and bottom hinges by being adjustable in the other two directions also, become three-way adjustable. This permits very accurate alignment of the doors so that they swing easily, do not go "up hill" or "down hill", and have no "run" in any position.

Since the door leaf, when closed, seats evenly against a finished section of the door frame all around the door periphery, and is firmly clamped from "rebounding" open by means of the tapered end locking bolt system, the blast forces on the door are isolated from the hinge bearings.

The tapered wedge locking bolt system used in the final design is a duplicate of the same system which has been used for the last 50 years on bank vault doors and was successfully tested under an actual nuclear blast in "Operation Plumbbob."

A completed 6'-0" x 7'-0" double-leaf blast door, 100 psi rating, is shown in Figures III-1 and III-2.

If it is desired to have these blast doors power-operated (say for remote control or interlocking in pairs), this is easily accomplished. Figures III-3 and III-4 show the 3'6" x 7'-0" single-leaf blast door, 100 psi rating, with the additional blast-proof operator.



NOT REPRODUCIBLE



Figure III-1

NOT REPRODUCIBLE

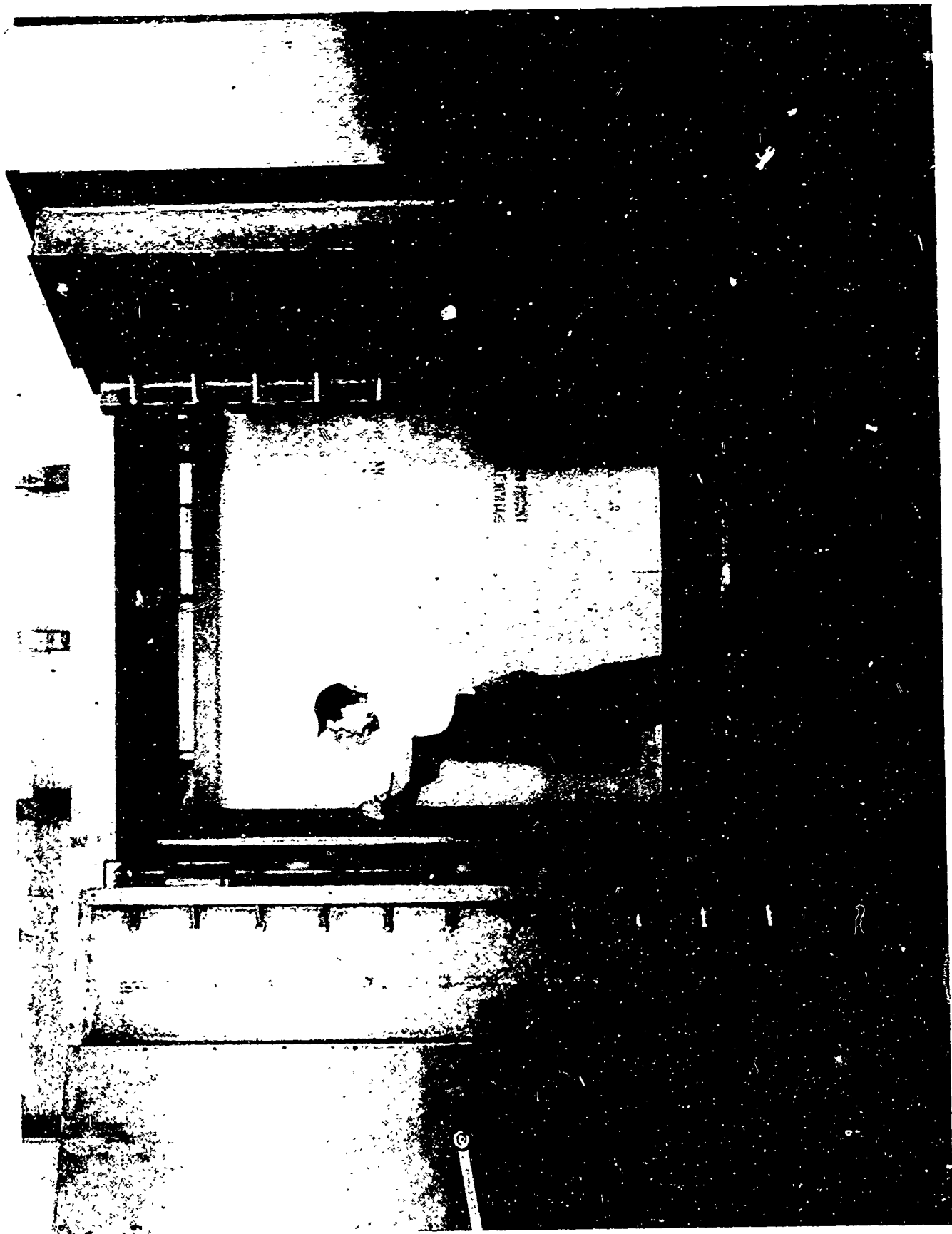


Figure III-2

NOT REPRODUCIBLE



Figure III-3

NOT REPRODUCIBLE



Figure III-4

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A composite list of the door sizes, drawing numbers, and specification numbers of the final door designs is as follows:

<u>Door Size</u>	<u>Drawing Number</u>			<u>Specification Number</u>
	<u>25 PSI</u>	<u>50 PSI</u>	<u>100 PSI</u>	
3'-6" x 7'-0"	60-12-06	60-12-07	60-12-08	60-12-06-60
6'-0" x 7'-0"	60-12-09	60-12-10	60-12-11	60-12-09-60
8'-0" x 8'-0"	60-12-12	60-12-13	60-12-14	60-12-12-60
12'-0" x 12'-0"	60-12-15	60-12-16	60-12-17	60-12-15-60
14'-0" x 18'-0"	60-12-18	60-12-19	60-12-20	60-12-18-60
3'-0" x 3'-0"	60-12-21	60-12-22	60-12-23	60-12-21-60
2'-6" x 4'-0"	60-12-24	60-12-25	60-12-26	60-12-24-60

#### SECTION IV - DESIGN CALCULATIONS

In calculating the strengths of the door leafs, there are three basic types of calculations, as follows:

1. Curved door, 3'-6" x 7'-0", 25 psi rating (Figure IV-1)
2. Solid steel plate doors simply supported all four sides, all 3'-0" x 3'-0" and 2'-6" x 4'-0" doors (Figure IV-2)
3. Structural Beam doors welded flange to flange (Figure IV-3)

In the case of the welded structural beam doors, calculations were made on a per beam basis, considering the beam as simply supported each end.

In the case of the solid steel plate doors, the calculations were made on the basis of a plate simply supported on all four sides. Basic plate formulae used were from "Theory of Plates and Shells" by Prof. S. Timoshenko (13).

For the convex curved plate door a completely elastic design was used, as the curved plate would otherwise fail by buckling as soon as the elastic limit was exceeded.

In all cases calculations were made in accordance with the Corps of Engineers Design Manuals (4 through 12). The Design Manuals show two basic approaches, the Energy Method and the Deflection Method. The Deflection Method was chosen as the most suitable. A numerical method of analysis was used in conjunction with an Acceleration Impulse Extrapolation Table.

Recurring constants in the various door calculations were lumped together to form one constant. Derivations of the various constants are shown in Figures IV-5 through IV-

Calculations are broken down into repetitive step-by-step procedures. A certain door section is assumed and then by a series of trials the optimum section is determined.

Typical calculations are shown for the 3'-6" x 7'-0", 25 psi curved door (Figure IV-1), the 3'-6" x 7'-0", 50 psi built-up door (Figure IV-2), the 14'-0" x 18'-0", 50 psi built-up door (Figure IV-3), and the 2'-6" x 4'-0", 100 psi, solid steel plate door (Figure IV-4).

DOOR NO. 60-12-06  
TRIAL NO. 1  
CURVED DOOR

CALCULATIONS BY T.A.  
CHECKED BY H.S.

Door opening = 3'-6" × 7'-0"

Door vertical

Assume 6" bearing width and  $\alpha = 60^\circ$ , arch fixed at supports

$f_s = 41.6$  ksi

Incident pressure = 25 psi =  $P_{so}$

Peak reflected pressure - 80 psi

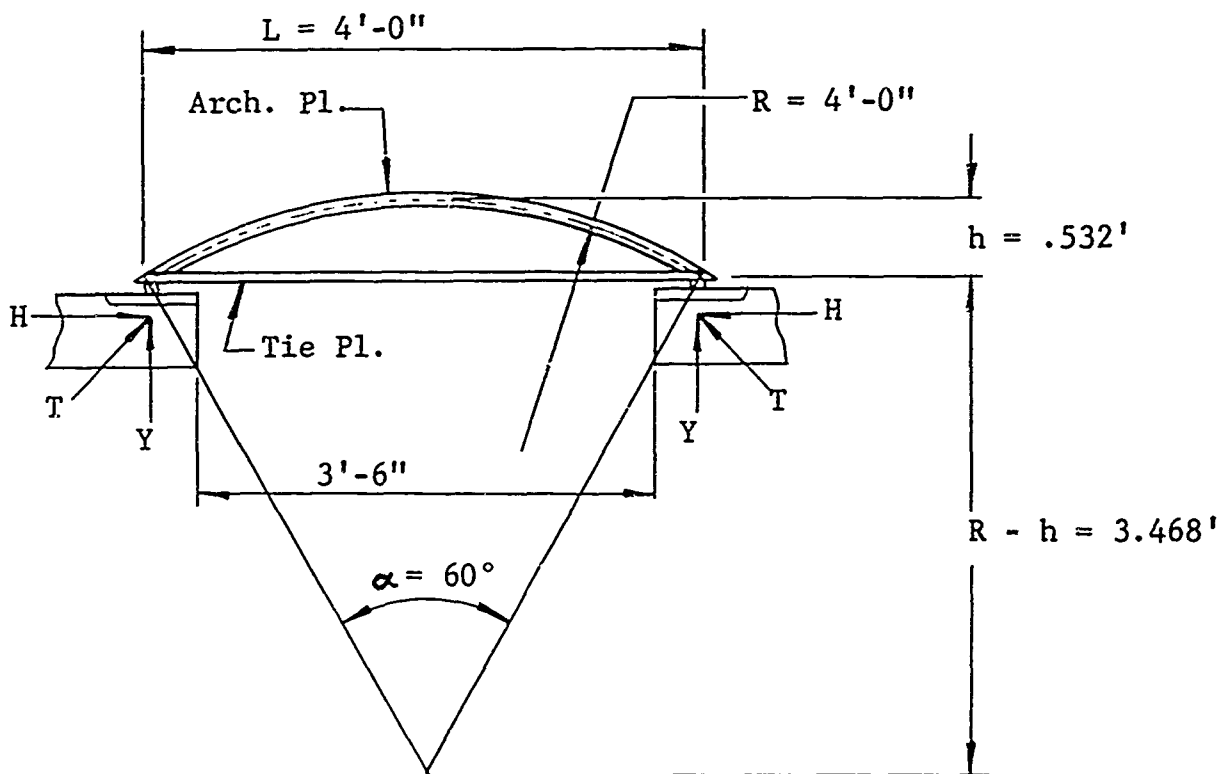


Figure 4V-1

$$R = \frac{L/2}{\sin \alpha/2} = \frac{2.00}{0.50} = 4.00$$

$$R - h = R \cos \alpha/2 = 4 (.867) = 3.468$$

$$h = .532$$



DOOR 60-12-06  
Trial No. 1

### Design for Direct Loading - Elastic

Assume a D.L.F. = 2.00

$P_r = .080$  ksi

$T = P_r R = .08 (2) 12 (4) = 7.68$  k/in.

$V = P_r R \sin \alpha/2 = .08 (2) 12 (4) .5 = 3.84$  k/in.

$H = P_r R \cos \alpha/2 = .08 (2) 12 (4) .867 = 6.66$  k/in.

### Required Thickness

Arch Plate  $t = \frac{7.68}{41.6} = .185$

Try 3/16" plate

Tie Plate  $t_1 = \frac{6.66}{41.6} = .160$

Try 11/64" plate

### Shock Velocity

$$U_o = 1117 \left[ 1 + \frac{6 P_{so}}{7 (14.7)} \right]^{\frac{1}{2}}$$

$$U_o = 1117 \left[ 1 + \frac{6 (25)}{102.9} \right]^{\frac{1}{2}} = 1750 \text{ ft/sec}$$

### Time of Pressure Rise

$$t_o = \frac{h}{U_o} = \frac{.532}{1750} = .000304 \text{ sec.}$$

### Period of Vibration of Arch Plate

$$T_N = 2\pi \frac{L^2}{C_2} \sqrt{\frac{m}{EI}}$$

$$C_2 = 4 \sin^2 \alpha/2 \left[ \frac{2}{3} \left( \frac{R}{k} \right)^2 + \left( \frac{\pi^2}{\alpha^2} - 1 \right)^2 \right]^{\frac{1}{2}}$$

$$k = \sqrt{\frac{I}{A}} = \sqrt{\frac{\frac{12 (3/16)^3}{12}}{\frac{12 (3/16)}{12}}} = \sqrt{\frac{(3/16)^2}{12}} = .0541 \text{ in.}$$

$$\frac{R}{k} = \frac{48}{.0541} = 887.2$$

DOOR 60-12-06

Trial No. 1

$$\alpha = 60^\circ = \pi/3 \text{ radians} \quad \pi^2/\alpha^2 = 9$$

$$C_2 = 4 (.5)^2 \left[ \frac{2}{3} (887.2)^2 + (9-1)^2 \right]^{\frac{1}{2}} \\ = 1 \left[ 5.24749 (10^5) + 64 \right]^{\frac{1}{2}} = 724.3$$

$$L = .48''$$

$$E = 30 (10^6) \text{ psi}$$

$$I = \frac{bd^3}{12} = \frac{1 (3/16)^3}{12} = .000549 \text{ in}^4/\text{in}$$

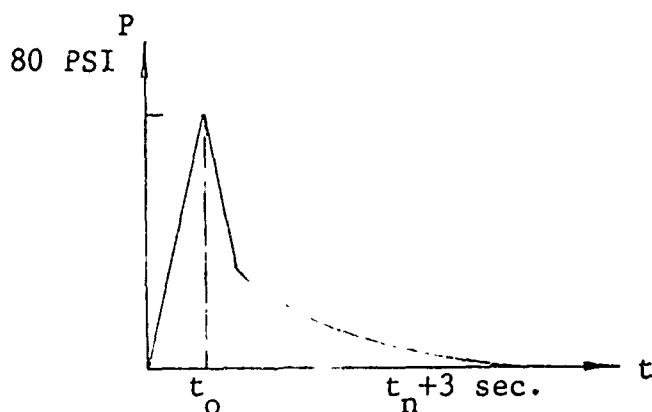
$$W = 490 \left( \frac{3/16}{12} \right) = 7.6 \text{ psf}$$

$$m = \frac{7.6}{32.2 (12) 144} = .000138 \text{ #sec}^2/\text{in}^3$$

$$T_n = 2\pi \frac{(48)^2}{724.3} \sqrt{\frac{.000138}{30 (10^6) .000549}} \\ = 19.98 \sqrt{8.38 (10^{-10})} = .001828$$

#### Dynamic Response of Arch Plate

The loading curve is assumed to have a triangular shape as shown below.



$$\frac{t_o}{T_n} = \frac{.000304}{.001828} = .16$$

$$D.L.F. = 1.95 \quad \approx 2 \quad \text{Section O.K.}$$

(The David W. Taylor Model Basin, USN,  
"Effects of Impact on Simple Elastic Structures".  
Report 481, April 1942, Fig. 18)

DOOR 60-12-06  
Trial No. 1

Buckling

$$P_c R = \frac{EI}{R^3} (k^2 - 1)$$

$$k = 8.5 \text{ for } \alpha = 60^\circ$$

$$P_c R = \frac{30 (10^6) .000549}{(48)^3} \left[ (8.5)^2 - 1 \right]$$

$$= .1489 \left[ 71.25 \right] = 10.6 \text{ psi} \quad 80 (2) = 160 \text{ psi} \quad \text{No Good}$$

3/16" plate O.K. for elastic direct loading, but not good for buckling. Try 1/2" plate for buckling.

$$I = \frac{bd^3}{12} = \frac{1 (1/2)^3}{12} = .0104$$

$$P_c R = \frac{30 (10^6) .0104}{(48)^3} \left[ (8.5)^2 - 1 \right]$$

$$= 2.82 \left[ 71.25 \right] = 201 \text{ psi} \quad 80 (2) = 160 \text{ psi} \quad \text{O.K.}$$

Use 1/2" arch plate

Use 11/64" tie plate

CALCULATIONS

1-WAY SPAN DOOR  
BUILT-UP DESIGN  
SIMPLY SUPPORTED 4 SIDES  
3'-6" x 7'-0", 50 PSI

TRIAL NO. 2

ELASTO-PLASTIC  
DOOR NO. 60-12-07  
CALCULATIONS BY T.A.  
CHECKED BY H.S.

GIVEN:

Assumed Beam	=	5 x 5 WF 16#
T = Load Duration	=	.050 Sec.
P <sub>r</sub> = Peak Reflected Pressure	=	197 PSI
W = Total Weight of Beam	=	58.6 Lbs.
A = Area of Beam (Width x Span)	=	220.5 Sq. In.
L = Span Length of Beam	=	3-1/2 Feet
S = Section Modulus of Beam	=	8.53 Inch <sup>3</sup>
I = Moment of Inertia of Beam	=	21.3 Inch <sup>4</sup>
K <sub>LM<sub>e</sub></sub> = Elastic Mass Constant	=	.780
K <sub>LM<sub>p</sub></sub> = Plastic Mass Constant	=	.667

FIND:

1. MAXIMUM ELASTIC DEFLECTION (FEET)

$$\begin{aligned}
 X_{el} &= .0017333 \times \frac{L^2 \times S}{I} = .001733 \times \frac{3.5^2 \times 8.53}{21.3} \\
 &= .0017333 \times 4.91 = \underline{.008511}
 \end{aligned}$$

2. NATURAL PERIOD (SECONDS)

$$\begin{aligned}
 T_n &= 6.2832 \times \sqrt{\frac{M_e}{K_1}} \\
 &= 6.2832 \times \sqrt{\frac{.001420}{7949}} \\
 &= 6.2832 \times \sqrt{.000000178638} \\
 &= 6.2832 \times .00042265 = \underline{.00266}
 \end{aligned}$$

3. EQUIVALENT MASS (ELASTIC) (KIP-SEC<sup>2</sup>/FT.)

$$M_e = \frac{W \times K_{LM_e}}{32,200} = \frac{58.6 \times .78}{32,200} = \underline{.001420}$$

4. EQUIVALENT MASS (PLASTIC) (KIP-SEC<sup>2</sup>/FT.)

$$M_p = W \times 20.704 \times 10^{-6} = \underline{.001213}$$

5. STIFFNESS FACTOR (KIP/FOOT)

$$K_1 = 16,000 \times \frac{I}{L^3} = 16,000 \times \frac{21.3}{42.875} = \underline{7,949}$$

6. MAX. ELASTIC RESISTANCE (KIP LB)

$$R_{el} = 27.7333 \times \frac{S}{L} = 27.7333 \times \frac{8.53}{3.5} = \underline{68}$$

7. CONSTANTS FOR EXTRAPOLATION TABLEELASTIC RANGE

$$a. \frac{T_n}{10} = \frac{.00266}{10} = \underline{.000266}$$

$$b. \triangle t = \underline{.0002}$$

$$c. (\triangle t)^2 = \underline{4 \times 10^{-8}}$$

$$d. P_o = \frac{P_r \times A}{1,000} = \frac{197 \times 220.5}{1,000} \text{ KIP } \underline{43.4}$$

$$e. P_1 = P_o \left(1 - \frac{\triangle t}{.05}\right) = 43.4 \left(1 - \frac{.0002}{.05}\right) = \underline{43.2}$$

$$f. P_o - P_1 = 43.4 - 43.2 = \underline{.2}$$

$$g. a_o = \frac{1}{M_e} \left( \frac{P_o}{2} + \frac{P_1 - P_o}{6} \right) = \frac{1}{.001420} \left( \frac{43.4}{2} - \frac{.2}{6} \right) \\ = \underline{15,253}$$

$$h. X_1 = a_o \times (\triangle t)^2 = 15,253 \times (4 \times 10^{-8}) = \underline{.000610}$$

$$i. \frac{(\triangle t)^2}{M_e} = \frac{4 \times 10^{-8}}{.001420} = \underline{2817 \times 10^{-8}}$$

PLASTIC RANGE

$$a. \triangle t = .0002$$

$$b. (\triangle t)^2 = 4 \times 10^{-8}$$

$$c. \frac{(\triangle t)^2}{M_p} = \frac{4 \times 10^{-8}}{.001213} = \underline{3298 \times 10^{-8}}$$

# ACCELERATION IMPULSE EXTRAPOLATION TABLE

$X_{el} = .008511$   $R_{el} = 68$   $K_1 = 7949$

N	t (Sec.)	$P_n$ (Kips)	$R_n$ (Kips)	$P_n - R_n$ (Kips)	$\frac{(\Delta t)^2}{m}$	$A_n(\Delta t)^2$ (Feet)	$2 X_n$ (Feet)	$X_{n-1}$ (Feet)	$X_{n+1}$ (Feet)	Remarks
0	0	43.4	--	--	$10^{-8} \times 2817$	.000610	0	0	0	
1	.0002	43.2	4.8	38.4	"	.001082	.001220	0	.000610	
2	.0004	43.0	18.3	24.7	"	.000696	.004604	.000610	.002302	
3	.0006	42.8	37.3	5.5	"	.000155	.009380	.002302	.004690	
4	.0008	42.6	57.5	-14.9	"	-.000418	.014466	.004690	.007233	
5	.0010	42.4	68.0	-25.6	$10^{-8} \times 3298$	-.000844	.018716	.007233	.009358	
6	.0012	42.2	68.0	-25.8	"	-.000850	.021278	.009358	.010639	
7	.0014	42.0	68.0	-26.0	"	-.000857	.022140	.010639	.011070	MAX.
8	.0016	41.8	64.6	-22.8	"	-.000752	.021288	.011070	.010644	
9	.0018	41.6	55.2	-13.6	"	-.000449	.018932	.010644	.009466	
10	.0020	41.4	42.3	- 0.9	"	-.000030	.015678	.009466	.007839	
11	.0022	41.2	29.1	12.1	"	.000399	.012364	.007839	.006182	
12	.0024	41.0	19.1	21.9	"	.000722	.009848	.006182	.004924	
13	.0026	40.8	14.9	25.9	"	.000854	.008776	.004924	.004388	
14									.004706	
15										
16										
17										
18										
19										
20										
21										

RESULTS  
Maximum Deflection = .011070  
Elastic Deflection = .008511  
Permanent Deflection = .002559

At .5" allowable total deflection - will take 16.3 max. blasts

DOOR 60-12-07 - T2

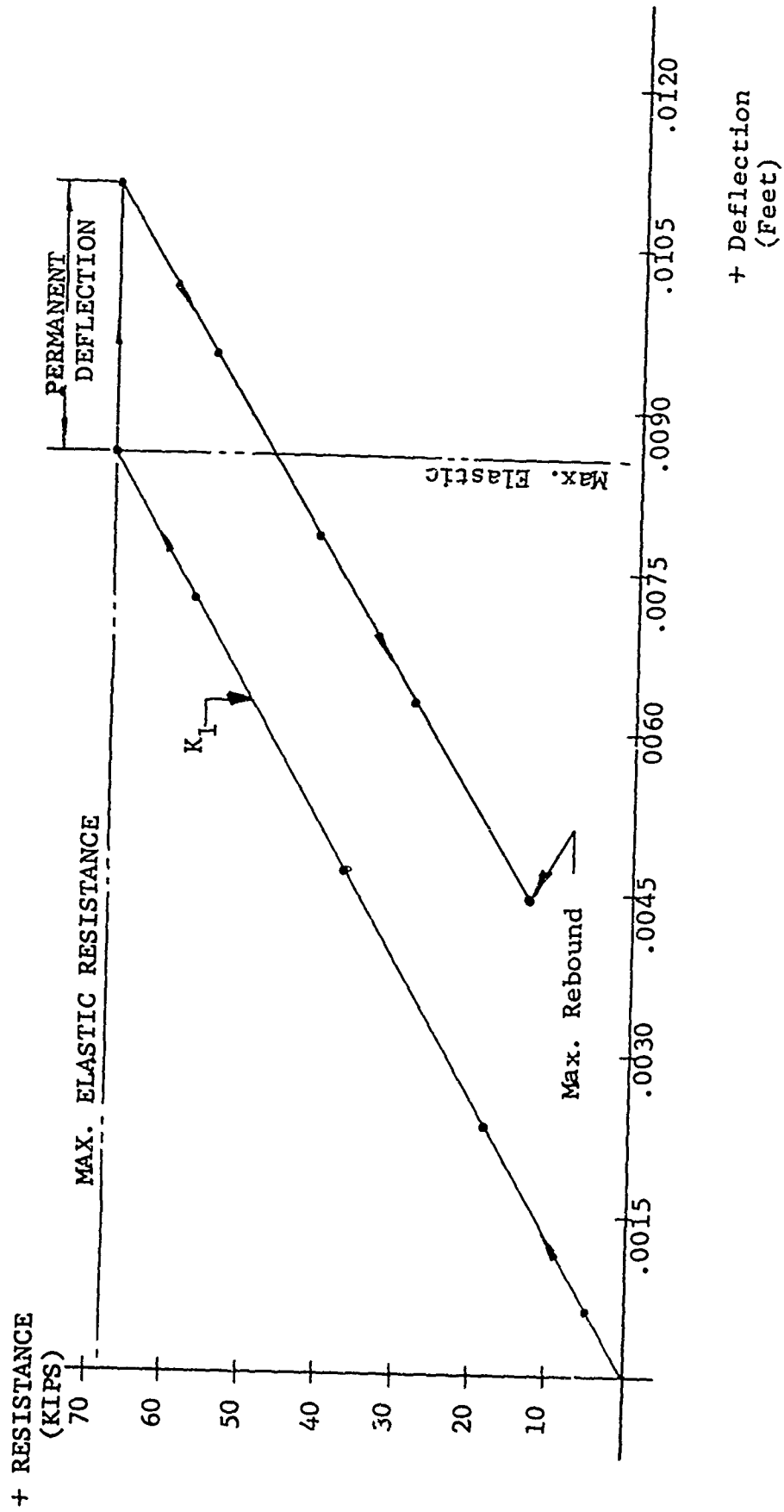
T = .05

R<sub>x</sub> TABLE

Maximum R<sub>x</sub> to Minus R<sub>el</sub>

R <sub>Max.</sub>	$\left[ \left( \frac{x_{Max.}}{x_x} \right) - \frac{K_1}{K_1} \right] = R_x$					
68	.011070	.010694	.000426	7,949	3.4	64.6
"	"	.009466	.001604	"	12.8	55.2
"	"	.007839	.003231	"	25.7	42.3
"	"	.006182	.004888	"	38.9	29.1
"	"	.004924	.006146	"	48.9	19.1
"	"	.004388	.006682	"	53.1	14.9





26 e

Scale:	Approved by:
DOOR NO. 60-12-07 - T2	
1-WAY SPAN, BUILT-UP	
LOAD DURATION - .050 Sec.	

DOOR 60-12-07 - T2  
Time = .009

7. CONSTANTS FOR EXTRAPOLATION TABLE

ELASTIC RANGE

$$a. \frac{T_n}{10} = \frac{.00266}{10} = .000266$$

$$b. \triangle t = .0002$$

$$c. (\triangle t)^2 = 4 \times 10^{-8}$$

$$d. P_o = \frac{P_r \times A}{1,000} = \frac{197 \times 220.5}{1,000} \text{ KIP } 43.4$$

$$e. P_1 = P_o \left(1 - \frac{t}{.009}\right) = 43.4 \left(1 - \frac{.0002}{.009}\right) = 42.4$$

$$f. P_o - P_1 = 43.4 - 42.4 = 1$$

$$g. a_o = \frac{1}{M_e} \left( \frac{P_o}{2} + \frac{P_1 - P_o}{6} \right) = \frac{1}{.001420} \left( \frac{43.4}{2} - \frac{1}{6} \right) = 15,162$$

$$h. X_1 = a_o \times (\triangle t)^2 = 15,162 \times (4 \times 10^{-8}) = .000606$$

$$i. \frac{(\triangle t)^2}{M_e} = \frac{4 \times 10^{-8}}{.001420} = 2,817 \times 10^{-8}$$

PLASTIC RANGE

$$a. \triangle t = .0002$$

$$b. (\triangle t)^2 = 4 \times 10^{-8}$$

$$c. \frac{(\triangle t)^2}{M_p} = \frac{4 \times 10^{-8}}{.001213} = 3,298 \times 10^{-8}$$

# ACCELERATION IMPULSE EXTRAPOLATION TABLE

$X_{el} = .008511$

$K_1 = 7949$

N	t (Sec.)	$P_n$ (Kips)	$R_n$ (Kips)	$P_n - R_n$ (Kips)	$\frac{(\Delta t)^2}{M}$	$A_n (\Delta t)^2$ (Feet)	$2 X_n$ (Feet)	$X_n - 1$ (Feet)	$X_n + 1$ (Feet)	Remarks
0	0	43.4	--	--	$10^{-8} \times 2817$	.000606	0	0	0	
1	.0002	42.4	4.8	37.6	"	.001059	.001212	0	.000606	
2	.0004	41.4	18.1	23.3	"	.000656	.004542	.000606	.002271	
3	.0006	40.4	36.5	3.9	"	.000106	.009184	.002271	.004592	
4	.0008	39.4	55.8	-16.4	"	-.000462	.014038	.004592	.007019	
5	.0010	38.4	68.0	-29.6	$10^{-8} \times 3298$	-.000976	.017968	.007019	.008984	
6	.0012	37.4	68.0	-30.6	"	-.001009	.019946	.008984	.009973	MAX.
7	.0014	36.4	67.8	-31.4	"	-.001036	.019906	.009973	.009953	
8	.0016	35.4	59.4	-24.0	"	-.000792	.017794	.009953	.008897	
9	.0018	34.4	44.8	-10.4	"	-.000343	.014098	.008897	.007049	
10	.0020	33.4	27.3	6.1	"	.000201	.009716	.007049	.004858	
11	.0022	32.4	11.5	20.9	"	.000689	.005736	.004858	.002868	
12	.0024	31.4	1.2	30.2	"	.000996	.003134	.002868	.001567	
13	.0026	30.4	- 1.2	31.6	"	.001042	.002524	.001567	.001262	
14	.0028							.001262	.001999	
15										
16										
17										
18										
19										
20										
21										

$$\text{Ratio} = \frac{1.2}{68} =$$

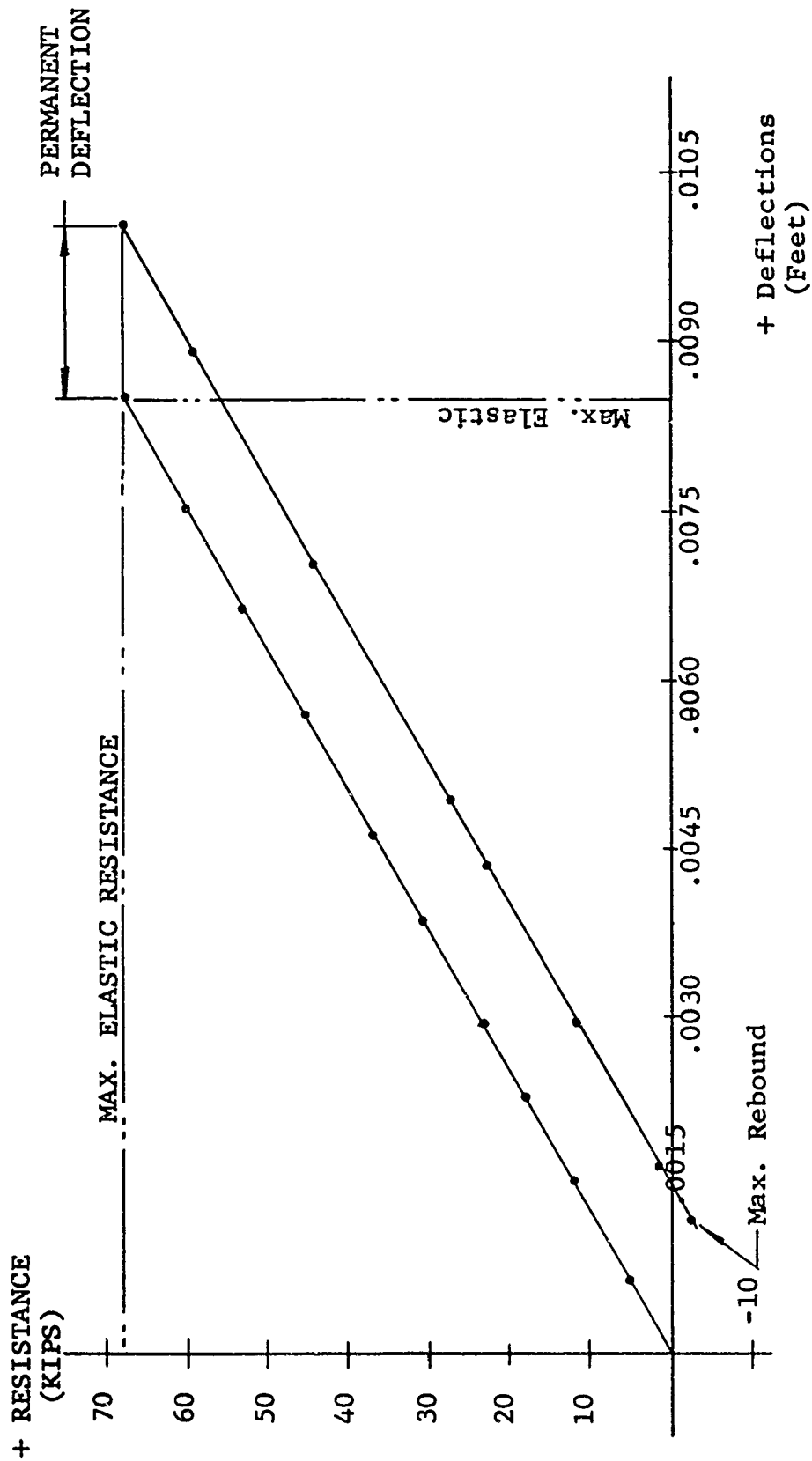
$$\text{Max. Rebound} =$$

DOOR 60-12-07 - T2  
T - .009

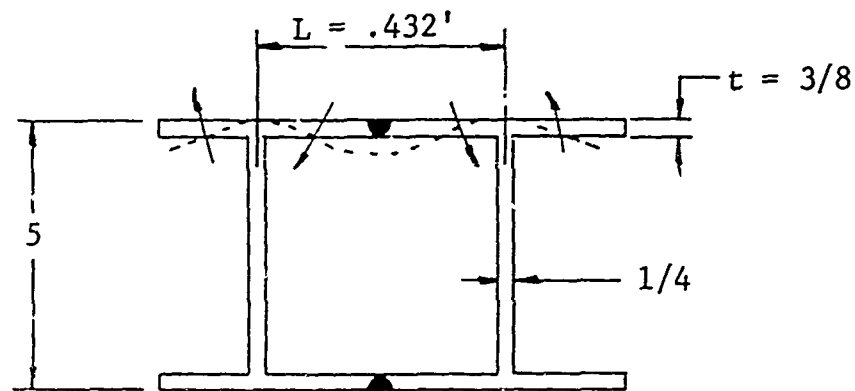
R<sub>x</sub> TABLE

Maximum R<sub>x</sub> to Minus R<sub>el</sub>

R <sub>Max.</sub>	$\left[ \left( X_{Max.} - X_x \right) = \right]$	$\times K_1 =$	$= R_x$
68	.009973	.009953 .000020 7,949 0.2	67.8
"	"	.008897 .001076 " 8.6	59.4
"	"	.007049 .002924 " 23.2	44.8
"	"	.004858 .005115 " 40.7	27.3
"	"	.002868 .007105 " 56.5	11.5
"	"	.001567 .008406 " 66.8	1.2
"	"	.001262 .008711 " 69.2	- 1.2



Scale:	Approved by:
DOOR NO. 60-12-07 - T2	
1-WAY SPAN, BUILT-UP	
LOAD DURATION - .009 Sec.	

CALCULATION FOR LOCAL CONDITION

$$1. \quad M_{\text{L}} = M_{\text{S}} = 1/4 \times 41.6 \times t^2 = 1/4 \times 41.6 \times .141 \\ = 1.4 \text{ K in/in}$$

$$2. \quad \sum M = \frac{2 M}{12} = \frac{1}{6} \times \frac{1.4}{6} = .233 \text{ K-ft/in}$$

$$3. \quad R = \frac{8M}{L} = \frac{8 \times .233}{.432} = 4.3 \text{ K/in}$$

$$4. \quad F = \frac{12 P_{\text{r}} \times L \times 1 \text{ (per inch)}}{1,000} = \frac{(12)(197)(432)}{1,000} = 1 \text{ K/in}$$

$$5. \quad \text{D.L.F.} = \frac{R}{F} = \frac{4.3}{1} = 4.3 > 2 \quad (\text{Member remains elastic})$$

CHECK FOR LOCAL BUCKLING OF ONE-WAY BEAMS

Beam = 5 x 5 WF @ 16#

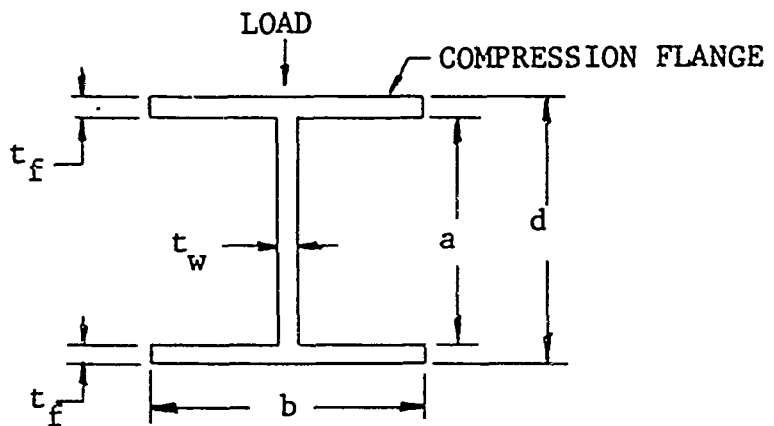
$$a = 4-1/4$$

$$b = 5-3/16$$

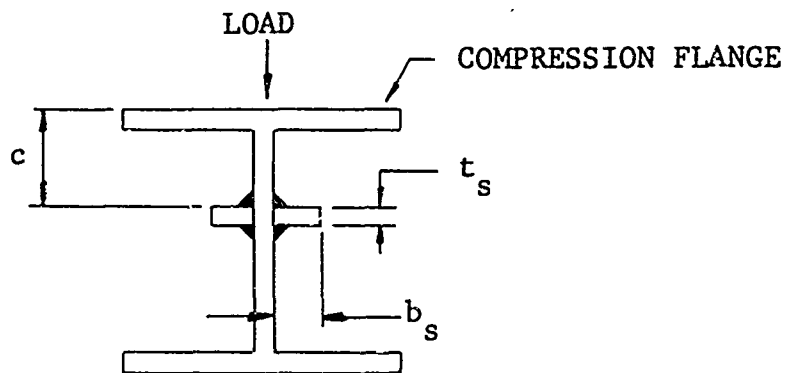
$$d = 5$$

$$t_f = 3/8$$

$$t_w = 1/4$$



$$\text{Web Ratio} = \frac{a}{t_w} = \frac{4.25}{.25} = 17$$

WEB REINFORCEMENT (WHEN REQUIRED)

Length of Stiffeners

Locate symmetrical with mid-point of door

CHECK FOR LATERAL-TORSIONAL BUCKLING

GIVEN:

$$K^1 = 0.51$$

$$L = \text{Span} = 42$$

$$d = \text{Depth of Beam} = 5.000$$

$$b = \text{Width of Flange} = 5.184$$

$$T_f = \text{Thickness of Flange} = .360$$

$$\begin{aligned} 1. \quad \frac{K^1 L d}{b T_f} &= \frac{.51 \times 42 \times 5.000}{5.184 \times .360} \\ &= \frac{107.100}{1.866} \\ &= 57.4 < 100 \quad \text{O.K.} \end{aligned}$$



BEARING AREA STRESS

$R_m$  = Maximum Resistance of Door

$$= R_{el} \times \frac{\text{Area of Leaf}}{\text{Area of Beam}} = R_{el} \times \frac{L_2 \times h}{L_2 \times W_b} = R_{el} \times \frac{h}{W_b}$$

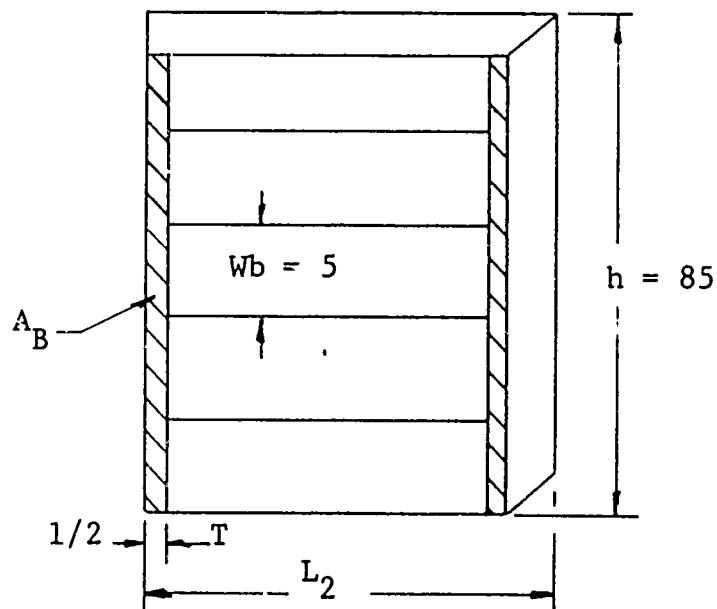
$$R_{el} = 68,000\#$$

$$R_m = 68,000 \times \frac{85}{5.000} = 1,156,000$$

$$S_b = \text{Bearing Stress} = \frac{R_m}{A_B} = \frac{R_m}{2T \times h}$$

$$A_B = 2 \times 1/2 \times 85 = 85 \text{ in}^2$$

$$S_b = \frac{1,156,000}{85} = 13,600 < 30,000 \text{ PSI} \quad \text{OK}$$



STRIKER THICKNESS CALCULATIONS

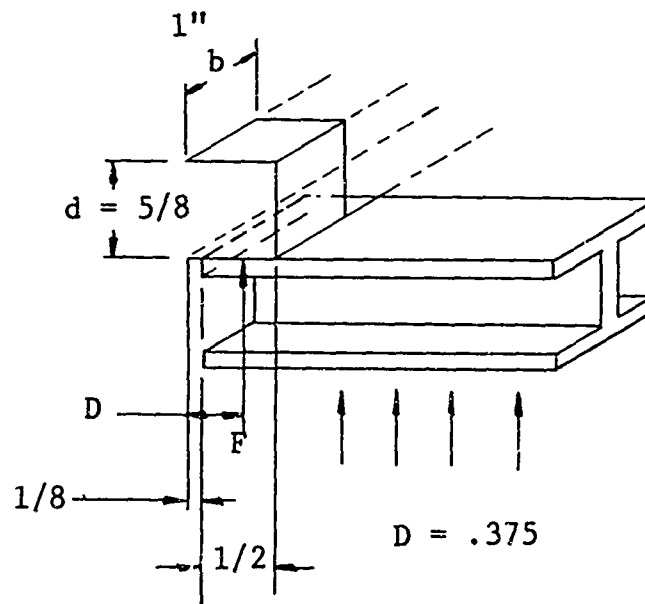
Take a 1" wide typical strip.

$$\text{Force per Lineal Inch} = F = \frac{R_m}{2 \times L_1} \quad (\text{see p. 26m})$$

$$= S_B \times T = 13,600 \times .500 = 6,800$$

$$\text{Bending Moment} = M = F \times D = 6,800 \times .372 = 2,550$$

$$\text{Thickness} = d = \sqrt{\frac{6M}{S_B}} = \sqrt{.367788} = .60696 \quad \underline{\text{USE 1"}}$$



\* $S_B$  = Allowable Bending Stress #A-7 Steel = 41,600

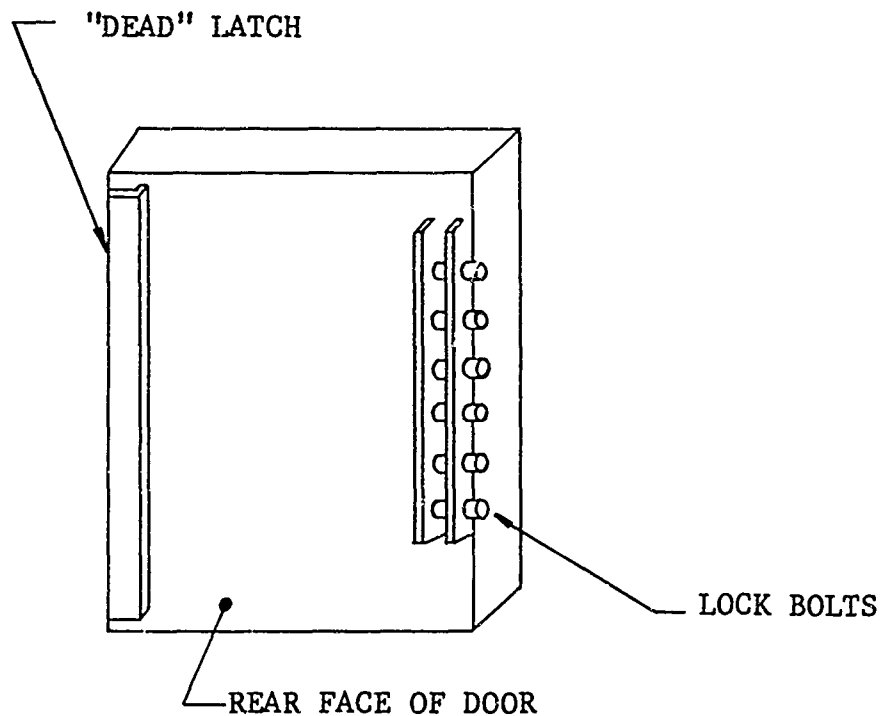
REBOUND LOAD CALCULATION FOR LOCK BOLTS

Consider rebound resisted equally by "dead latch" and lock bolts.

Then:

$$\begin{aligned}\text{Rebound force per bolt} = P &= \frac{.25 P_m}{2 \times \text{no. of lock bolts}} \\ &= \frac{289,000}{12} = 24,083\end{aligned}$$

Maximum total rebound force is obtained from rebound calculations.



LOCK BOLT CALCULATIONS - REBOUND - BLAST DOOR

MAX. L = .909

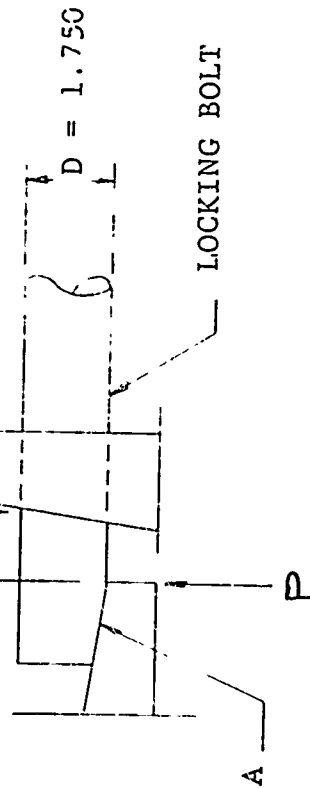
L P = 24,083

P = Equiv. Static Force per Bolt  
in Pounds

L = Length in inches

D = Diameter in inches

A = Bearing area in sq. in.



MIN. A = .803

1. Vertical Shear =  $\frac{4 P}{\pi \times D^2} = \frac{4 \times 24,083}{3.1416 \times 3.0625} = \frac{96,332}{9.62} = 10,014$
2. Horiz. Shear =  $\frac{16 P}{3\pi \times D^2} = \frac{16 \times 24,083}{3 \times 3.1416 \times 3.0625} = \frac{385,328}{28.86} = 13,352$
3. Bending Stress =  $\frac{32 \times P \times L}{\pi \times D^3} = \frac{32 \times 24,083 \times .875}{3.1416 \times 5.359} = \frac{674,324}{16.84} = 40,043$
4. Bearing Stress =  $\frac{P}{A} = \frac{24,083}{1.898} = 12,689$

Allowable Stresses - #A-7 Steel:

1. 21,000 PSI
2. 21,000 PSI
3. 41,600 PSI
4. 30,000 PSI

CALCULATIONS FOR RADIAL-THRUST BEARINGSIN LOWER HINGE\*

$$\text{RPM} \leq 50 \quad F_a/F_r = .65$$

Rotating Inner Ring

$$\text{Thrust Load} = F_a = 2,076$$

$$\text{Radial Load} = F_r = 746$$

$$\text{Rotation Factor} = V = 1$$

$$\text{Thrust Factor} = Y = 1.45$$

$$\text{Radial Factor} = X = .67$$

P = Equivalent Load

$$\begin{aligned} P &= XV F_r + Y F_a \\ &= .67 F_r + 1.45 F_a \\ &= (.67 \times 746) + (1.45 \times 2,076) \\ &= 500 + 3,010 \\ &= 3,510 \end{aligned}$$

$$\frac{C}{P} \geq 1.0$$

∴ Minimum bearing is SKF #5303 or equivalent.

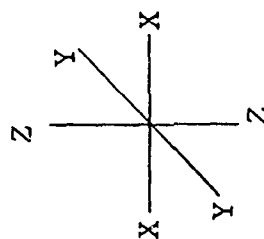
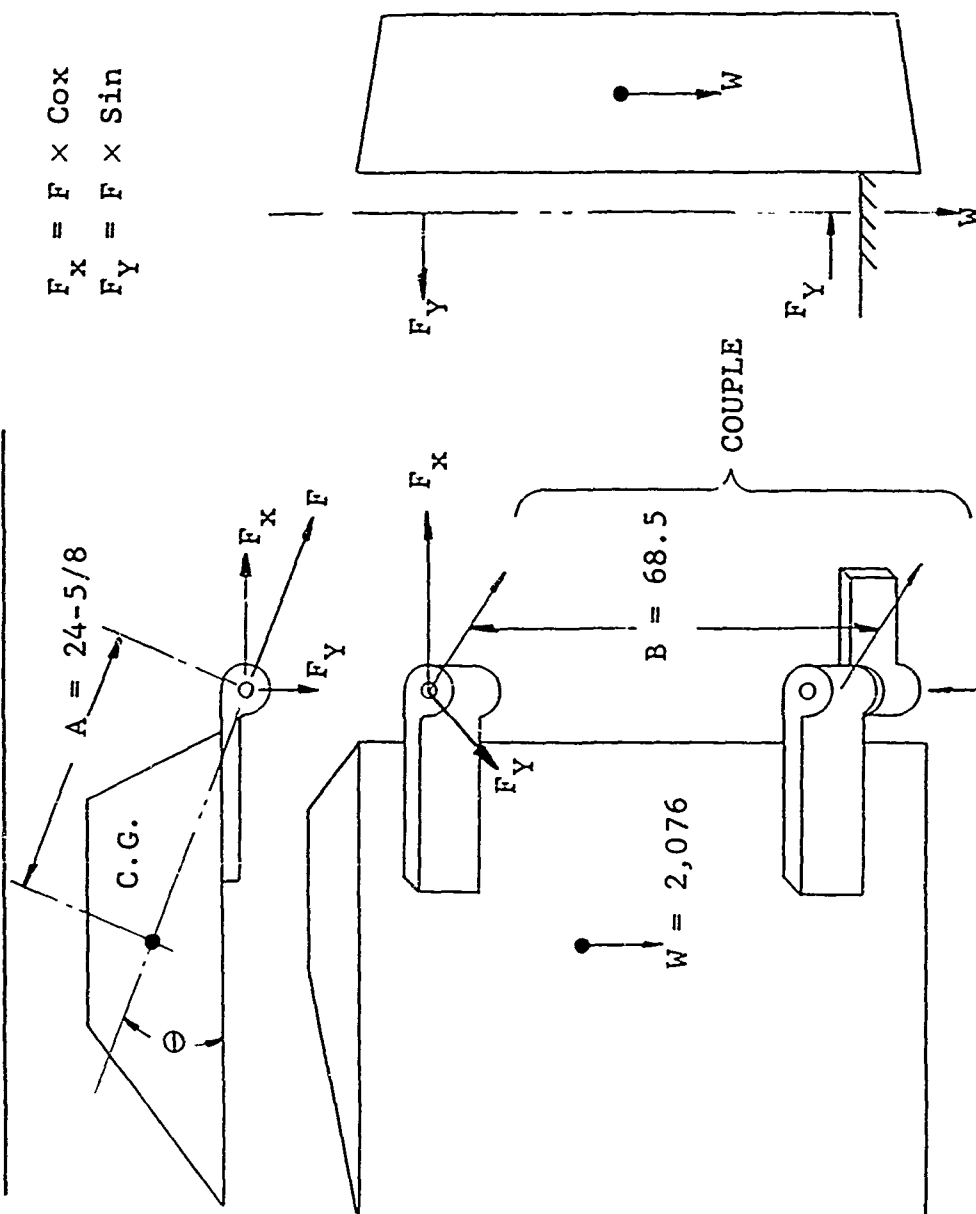
Use SKF bearing #5304 or equivalent.

\* Formula shown is for Series 5200 and 5300 double row, deep groove SKF bearings. Series #5300 preferred. For other design bearings, check formula.

STRESS ANALYSIS DIAGRAM - HINGE BEARINGS

$$F_x = F \times \cos \theta$$

$$F_y = F \times \sin \theta$$



$$W \times A = F \times B$$

$$F = \frac{W \times A}{B} = \frac{2,076 \times 24.625}{68.5} = \frac{51,121.5}{68.5} = 746$$

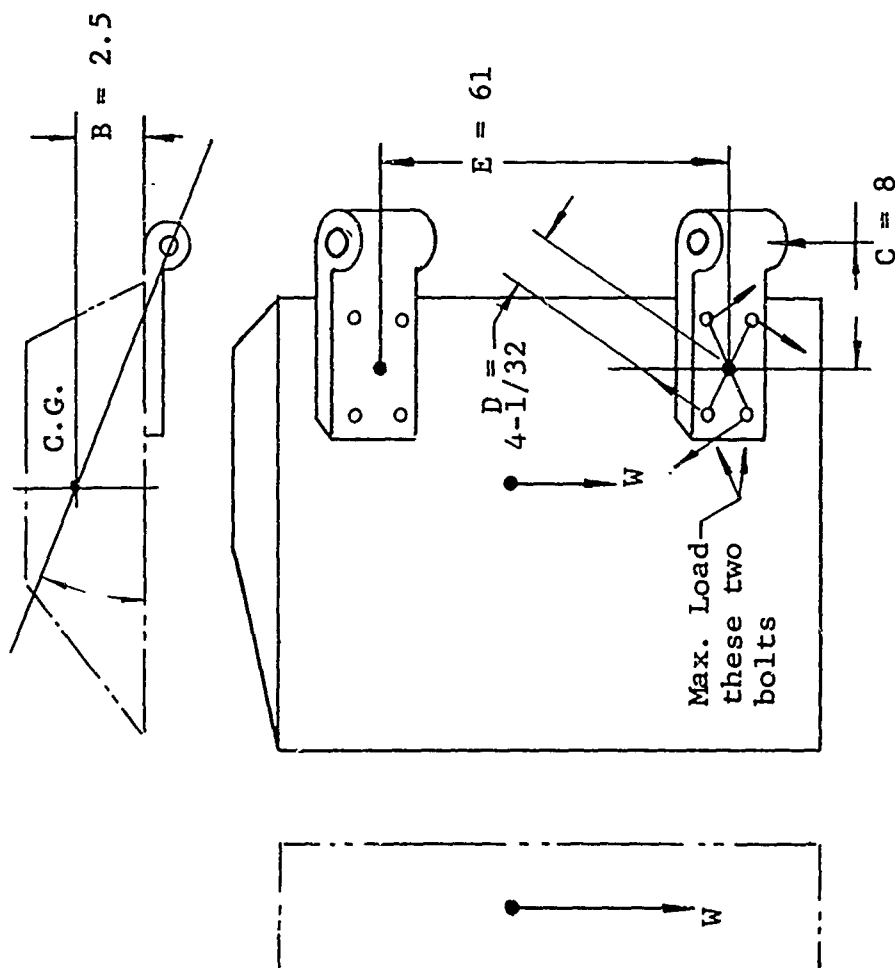
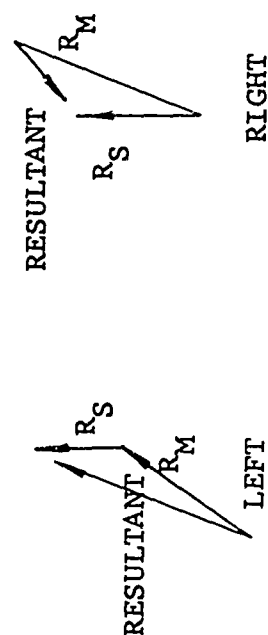
STRESS ANALYSIS DIAGRAM - HINGE BOLTS (NO SAFETY FACTOR)

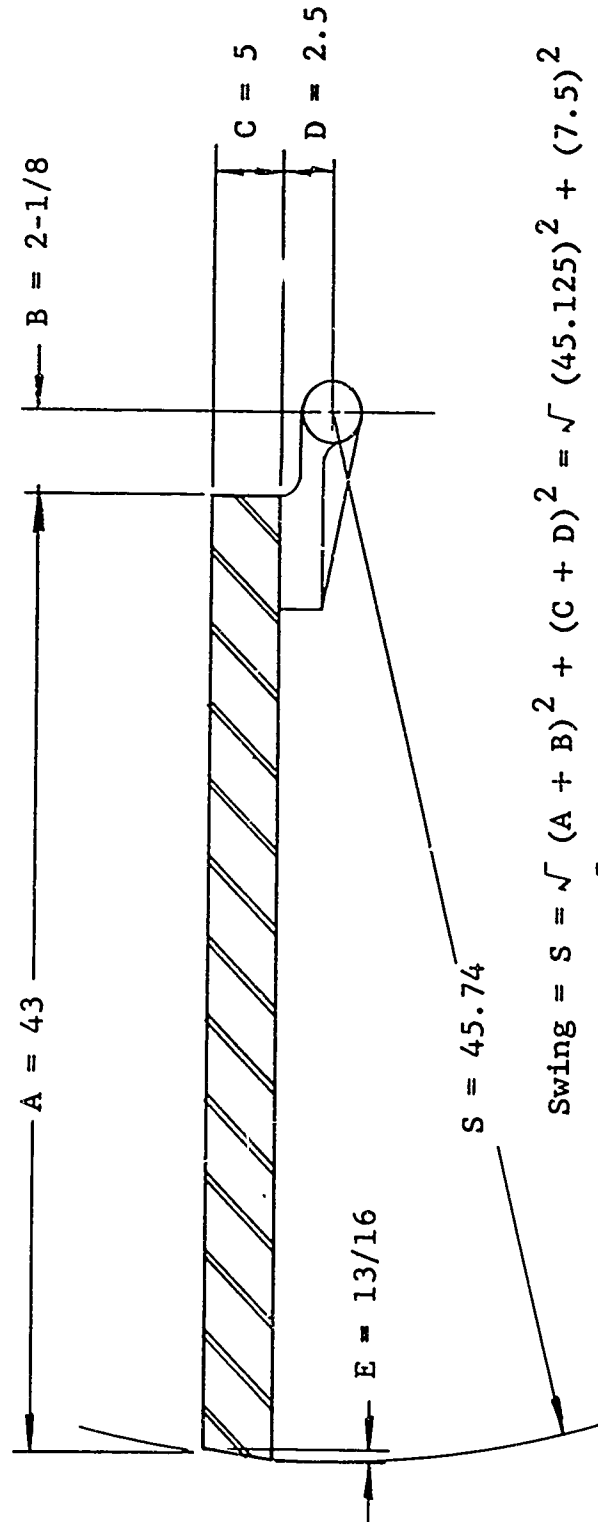
$W = \text{Weight} = 2,076$   
 (Lower 4 bolts)  
 Min. Resistance to Twisting Moment  
 per Bolt:  

$$R_M = \frac{W \times C}{4 \times D} = \frac{2,076 \times 8}{4 \times 4.033} = \frac{16,608}{16.132} = 1,029$$
  
 (Upper 4 Bolts only)  
 Min. Resistance to Tension per Bolt:  

$$R_T = \frac{W \times B}{4 \times E} = \frac{2,076 \times 2.5}{4 \times 61} = \frac{5190}{244} = 21.27$$
  
 (Lower 4 Bolts only)  
 Min. Resistance to Shear per Bolt:  

$$R_S = \frac{W}{4} = \frac{2,076}{4} = 519$$

VECTOR ADDITION FORCES ON LOWER BOLTS

CALCULATIONS - DOOR SWING AND DOOR TAPER

$$\begin{aligned} \text{Swing} = S &= \sqrt{(A + B)^2 + (C + D)^2} = \sqrt{(45.125)^2 + (7.5)^2} \\ &= \sqrt{2036.27 + 56.25} = \sqrt{2092.52} = 45.74 \end{aligned}$$

$$\text{Taper} = E = \frac{C^2 + (C \times D)}{(A + B)} = \frac{24 + 12.5}{45.125} = \frac{27.500}{45.125} = .831 \quad \text{Use } 13/16$$



### CALCULATIONS

1-WAY SPAN DOOR  
BUILT-UP DESIGN  
SIMPLY SUPPORTED 2 SIDES  
PARTIALLY LOADED OVER FULL SPAN  
14'-0" x 18'-0", 50 PSI

TRIAL NO. 2

ELASTO-PLASTIC  
DOOR NO. 60-12-19  
CALCULATIONS BY T.A.  
CHECKED BY H.S.

### GIVEN:

Assumed Beam	=	24 WF @ 145
T = Load Duration	=	.050 Sec.
$p_r$ = Peak Reflected Pressure	=	197 PSI
W = Total Weight of Beam	=	2465 Lbs.
A = Area of Beam (Width x Span)	=	2268 Sq. In.
$L_2$ = Span Length of Beam	=	17 Feet
S = Section Modulus of Beam	=	3725 Inch <sup>3</sup>
I = Moment of Inertia of Beam	=	4561 Inch <sup>4</sup>
$K_{LM_e}$ = Elastic Mass Constant	=	.67
$K_{LM_p}$ = Plastic Mass Constant	=	.57
$L_1$ = Loaded Portion of Beam	=	14 Feet

Figure IV-3

### FIND:

#### 1. MAXIMUM ELASTIC DEFLECTION (FEET)

$$x_{el} = .000346666 \times \frac{S}{I} \left( \frac{8 L_2^3 - 4 L_1^2 L_2 + L_1^3}{2 L_2 - L_1} \right) =$$
$$(.000346666)(.081671) \left( \frac{39304 - 13328 + 2744}{20} \right) =$$
$$.000346666 \times 94.869034 = \underline{.032888}$$

#### 2. NATURAL PERIOD (SECONDS)

$$T_n = 6.2832 \times \sqrt{\frac{M_e}{K_1}}$$
$$= 6.2832 \times \sqrt{\frac{.051290}{15706}}$$
$$= 6.2832 \times \sqrt{.000003265631}$$
$$= 6.2832 \times .001807 = \underline{.011354}$$

3. EQUIVALENT MASS (ELASTIC) (KIP-SEC<sup>2</sup>/FT.)

$$M_e = \frac{W \times K_{LM_e}}{32,200} = \frac{2465 \times .67}{32,200} = \underline{.051290}$$

4. EQUIVALENT MASS (PLASTIC) (KIP-SEC<sup>2</sup>/FT.)

$$M_p = W \times 20.704 \times 10^{-6} = 2465 \times 20.704 \times 10^{-6} = \underline{.051035}$$

5. STIFFNESS FACTOR (KIP/FOOT)

$$\begin{aligned} K_1 &= 80,000 \times \frac{I}{8 L_2^3 - 4 L_1^2 L_2 + L_1^3} \\ &= 80,000 \times \frac{4561}{39304 - 13328 + 2744} \\ &= 80,000 \times \frac{4561}{23,232} = \underline{15,706} \end{aligned}$$

6. MAX. ELASTIC RESISTANCE (KIP LB)

$$R_{el} = \frac{27.7333 \times S}{2 L_2 - L_1} = \underline{517}$$

7. CONSTANTS FOR EXTRAPOLATION TABLEELASTIC RANGE

$$a. \frac{T_n}{10} = \frac{.01}{10} = \underline{.001}$$

$$b. \Delta t = \underline{.001}$$

$$c. (\Delta t)^2 = \underline{1 \times 10^{-6}}$$

$$d. P_o = \frac{P_r \times A}{1000} = \underline{447 \text{ KIP}}$$

$$e. P_1 = P_o \left(1 - \frac{t}{.05}\right) = 447 \left(1 - \frac{.001}{.05}\right) = \underline{438}$$

$$f. P_o - P_1 = 447 - 438 = \underline{9}$$

$$g. a_o = \frac{1}{M_e} \left( \frac{P_o}{2} + \frac{P_1 - P_o}{6} \right) = \underline{4,328}$$

$$h. X_1 = a_o \times (\Delta t)^2 = 4328 \times 10^{-6} \times 1 = \underline{.004328}$$

$$i. \frac{(\Delta t)^2}{M_e} = \frac{1 \times 10^{-6}}{.051290} = \underline{19.496 \times 10^{-6}}$$

PLASTIC RANGE

$$a. \Delta t = .001$$

$$b. (\Delta t)^2 = 1 \times 10^{-6}$$

$$c. \frac{(\Delta t)^2}{M_p} = \frac{10^{-6}}{.051035} = \underline{19.594 \times 10^{-6}}$$

# ACCELERATION IMPULSE EXTRAPOLATION TABLE

$X_{el} = .032888$   $R_{el} = 517$   $K_1 = 15,706$

N	t (Sec.)	P <sub>n</sub> (Kips)	R <sub>n</sub> (Kips)	P <sub>n</sub> - R <sub>n</sub> (Kips)	$\frac{(\Delta t)^2}{m}$	A <sub>n</sub> (Δt) <sup>2</sup> Feet	2 X <sub>n</sub> (Feet)	X <sub>n</sub> - 1 (Feet)	X <sub>n</sub> + 1 (Feet)	Remarks
0	.000	447	0	447	19496 × 10 <sup>-6</sup>	.004328	0	0	0	
1	.001	438	68	370	"	.007214	.008656	0	.004328	
2	.002	429	249	180	"	.003509	.031740	.004328	.015870	
3	.003	420	486	- 66	"	-.001287	.061842	.015870	.030921	
4	.004	411	517	-106	19594 × 10 <sup>-6</sup>	-.002077	.089370	.030921	.044685	
5	.005	402	517	-115	"	-.002253	.112744	.044685	.056372	
6	.006	393	517	-124	"	-.002430	.131612	.056372	.065806	
7	.007	384	517	-133	"	-.002606	.145620	.065806	.072810	
8	.008	375	517	-142	"	-.002782	.154416	.072810	.077208	
9	.009	366	517	-151	"	-.002959	.157648	.077208	.078824	
10	.010	357	496	-139	19496 × 10 <sup>-6</sup>	-.002710	.154962	.078824	.077481	
11	.011	348	432	- 84	"	-.001638	.146856	.077481	.073428	
12	.012	339	343	- 4	"	-.000078	.135474	.073428	.067737	
13	.013	330	252	78	"	.001520	.123936	.067737	.061968	
14	.014	321	186	135	"	.002632	.115438	.061968	.057719	
15	.015	312	160	152	"	.002962	.112204	.057719	.056102	
16	.016	303						.056102	.057448	
17										
18										
19										
20										
21										

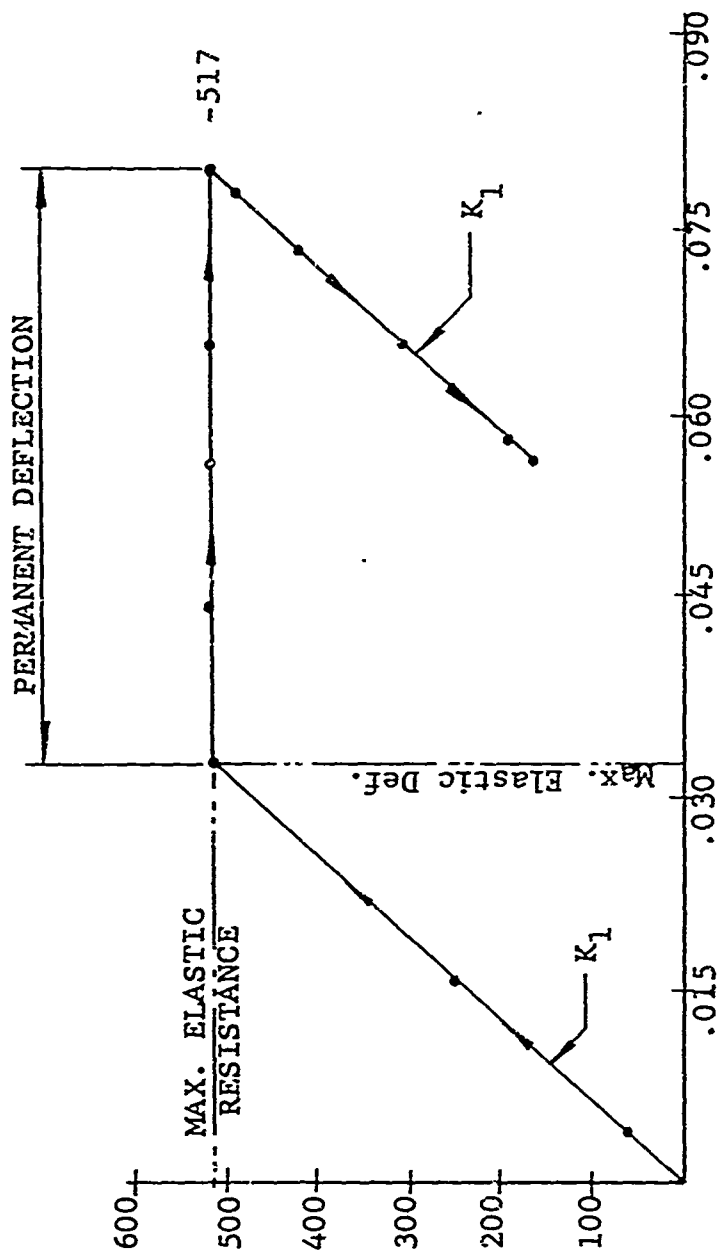
**RESULTS**  
 Maximum Deflection = .078824  
 Elastic Deflection = .032888  
 Permanent Deflection = .045936  
 Ratio =  $\frac{517}{447} = 1.16$   
 Max. Rebound =

At 3" allowable total deflection - will take 5.4 max. blasts

R<sub>x</sub> TABLE

Maximum R<sub>x</sub> to Minus R<sub>el</sub>

R <sub>Max.</sub>	$\left[ \left( x_{\text{Max.}} - x_x \right) \right]$	$\times K_1$	$= R_x$
517	.073824	.077481	.001343
"	"	.073423	.005396
"	"	.067737	.011087
"	"	.061968	.016856
"	"	.057719	.021105
"	"	.056102	.022722



$X_N$  Def. Ft.

Scale:	Approved by:	
DOOR NO. 60-12-19 - T1		
24-1/2" thick - 50 PSI Incident Pressure		
LOAD DURATION - .05 Sec.		

## 7. CONSTANTS FOR EXTRAPOLATION TABLE

### ELASTIC RANGE

$$a. \frac{T_n}{10} = .001$$

$$b. \Delta t = .001$$

$$c. (\Delta t)^2 = 1 \times 10^{-6}$$

$$d. P_o = \frac{P_r \times A}{1,000} = 447 \text{ KIP}$$

$$e. P_1 = P_o \left(1 - \frac{\Delta t}{.024}\right) = 428 \text{ KIP}$$

$$f. P_o - P_1 = 447 - 428 = 19 \text{ KIP}$$

$$g. a_o = \frac{1}{M_e} \left( \frac{P_o}{2} + \frac{P_1 - P_o}{6} \right) = 4296$$

$$h. x_1 = a_o \times (\Delta t)^2 = 4296 \times 1 \times 10^{-6} = .004296$$

$$i. \frac{(\Delta t)^2}{M_e} = \frac{1 \times 10^{-6}}{.051290} = 19.496 \times 10^{-6}$$

### PLASTIC RANGE

$$a. \Delta t = .001$$

$$b. (\Delta t)^2 = 1 \times 10^{-6}$$

$$c. \frac{(\Delta t)^2}{M_p} = 19.594 \times 10^{-6}$$

# ACCELERATION IMPULSE EXTRAPOLATION TABLE

$X_{el} = .032888$

$R_{el} = 517$

$K_1 = 15,706$

N	t (Sec.)	P <sub>n</sub> (Kips)	R <sub>n</sub> (Kips)	P <sub>n</sub> - R <sub>n</sub> (Kips)	$\frac{(\Delta t)^2}{m}$	A <sub>n</sub> (Δt) <sup>2</sup> (Feet)	2 X <sub>n</sub> (Feet)	X <sub>n</sub> - 1 (Feet)	X <sub>n</sub> + 1 (Feet)	Remarks
0	0	447	0	447	$19426 \times 10^{-6}$	.004296	0	0	0	
1	.001	428	67	361	"	.007038	.008592	0	.004296	
2	.002	409	245	164	"	.003197	.031260	.004296	.015630	
3	.003	390	474	- 84	"	-.001638	.060322	.015630	.030161	
4	.004	371	517	-146	$19594 \times 10^{-6}$	-.002861	.086108	.030161	.043054	
5	.005	352	517	-165	"	-.003233	.106172	.043054	.053086	
6	.006	333	517	-184	"	-.003605	.119770	.053086	.059885	
7	.007	314	517	-203	"	-.003978	.126158	.059885	.063079	
8	.008	295	505	-210	$19496 \times 10^{-6}$	-.004094	.124590	.063079	.062295	
9	.009	276	428	-152	"	-.002963	.114834	.062295	.057417	
10	.010	257	305	- 48	"	-.000936	.099152	.057417	.049576	
11	.011	238	167	71	"	.001384	.081598	.049576	.040799	
12	.012	219	51	168	"	.003275	.066812	.040799	.033406	
13	.013	200	- 14	214	"	.004172	.058576	.033406	.029288	
14	.014	181						.029288	.029342	
15										
16										
17										
18										
19										
20										
21										

## RESULTS

Maximum Deflection = .063079  
 Elastic Deflection = .032888  
 Permanent Deflection = .030191

Ratio =  $\frac{517}{447} = 1.16$   
 Max. Rebound = -14 Kips

At 3" allowable total deflection - will take \_\_\_ max. blasts

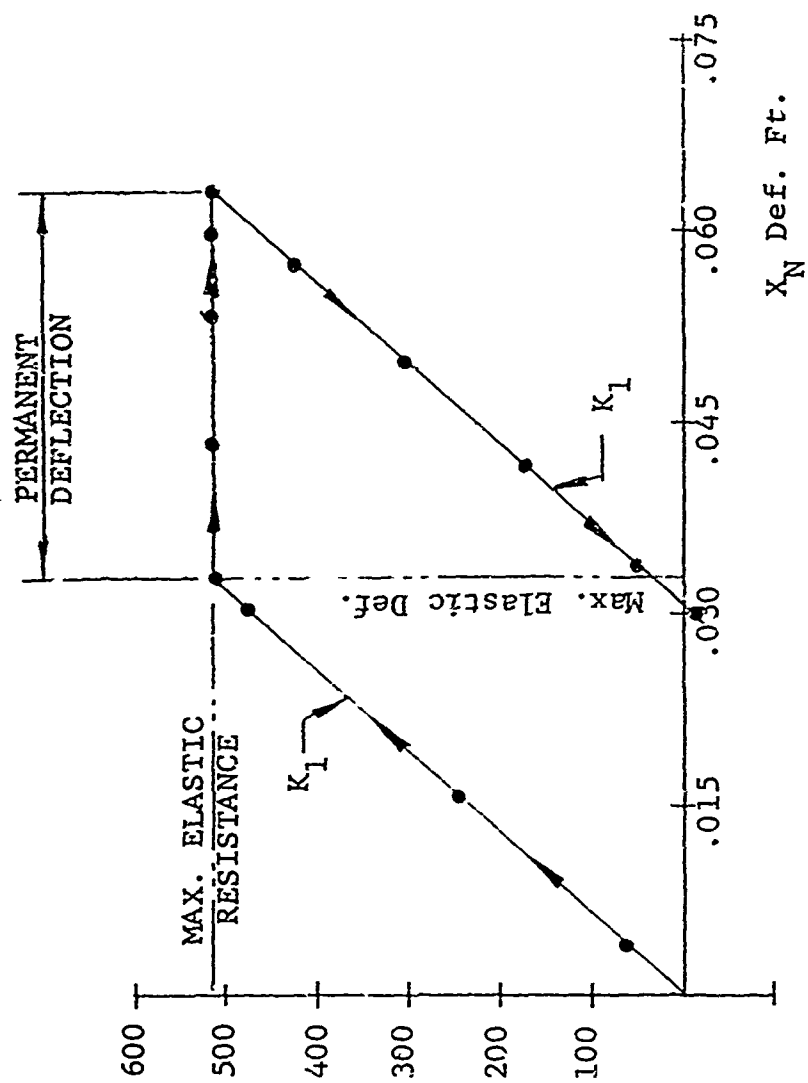


R<sub>x</sub> TABLE

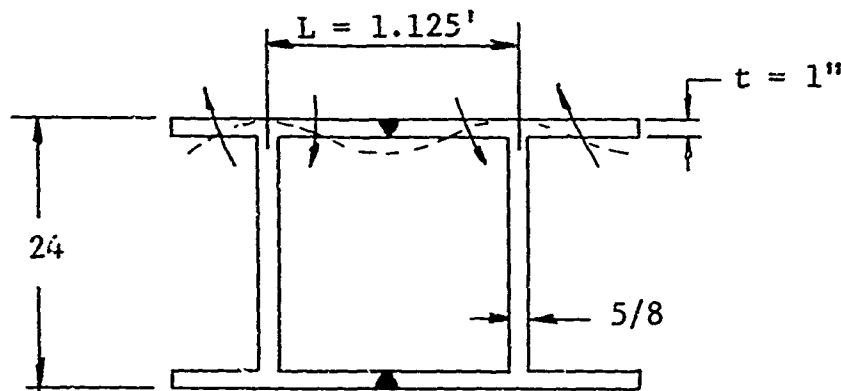
Maximum R<sub>x</sub> to Minus R<sub>el</sub>

$$R_{Max.} - \left[ \left( X_{Max.} - X_x \right) \times K_1 \right] = R_x$$

517	.063079	.062295	.000784	15,706	12	505
"	"	.057417	.005662	"	89	428
"	"	.049576	.013503	"	212	305
"	"	.040799	.022280	"	350	167
"	"	.033406	.029673	"	466	51
"	"	.029288	.033791	"	531	- 14



Scale:	Approved by:
DOOR NO. 60-12-19 - T1	
24-1/2" thick - 50 PSI Incident Pressure	
LOAD DURATION - .024 Sec.	

CALCULATION FOR LOCAL CONDITION

$$1. \quad M_L = M_s = \frac{1}{4} \times 41.6 \times t^2 = \frac{1}{4} \times 41.6 \times 1$$

$$= 10.4 \text{ K in/in}$$

$$2. \quad \sum M = \frac{2 M}{12} = \frac{1}{6} \times 10.4 = 1.73 \text{ K-ft/in}$$

$$3. \quad R = \frac{8 M}{L} = \frac{1.73 \times 8}{1.125} = 12.3 \text{ K/in}$$

$$4. \quad F = \frac{12 P_r \times L \times 1 \text{ (per inch)}}{1,000} = \frac{12 \times 197 \times 1.125}{1,000} = 2.66 \text{ K/in}$$

$$5. \quad \text{D.L.F.} = \frac{R}{F} = \frac{12.3}{2.66} = 4.6 > 2 \quad (\text{Member remains elastic})$$

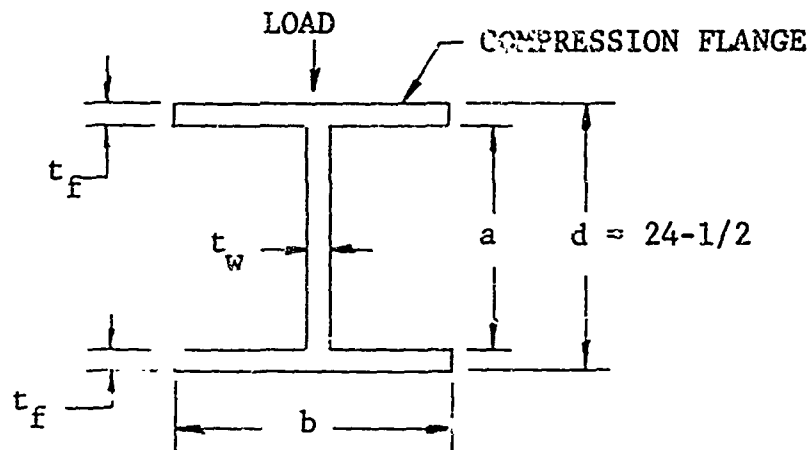
CHECK FOR LOCAL BUCKLING OF ONE-WAY BEAMS

Beam = 24 WF @ 145

a = 22-1/2

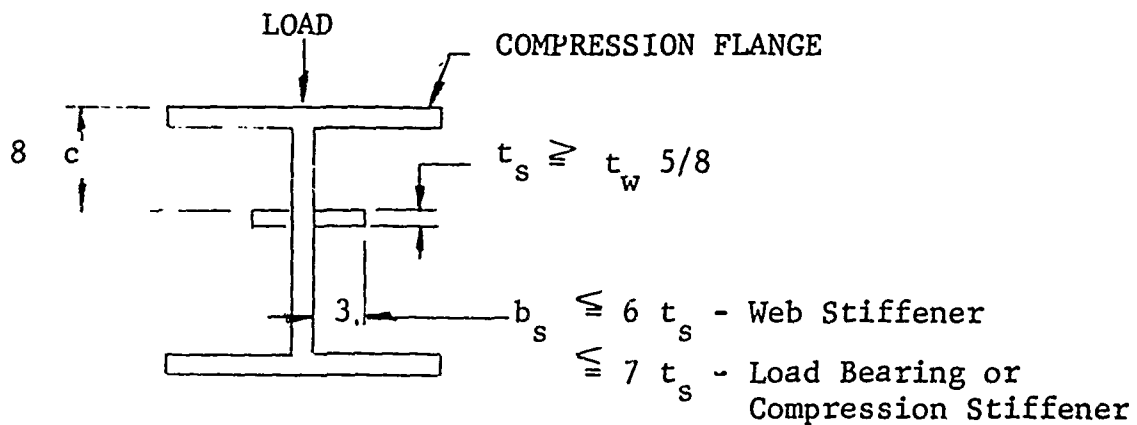
b = 13-1/2

d = 24-1/2

 $t_f = 1$  $t_w = .625$ 

1. Compression Flange Ratio =  $\frac{b}{t_f} = 13.5$

2. Web Ratio =  $\frac{a}{t_w} = \frac{22.5}{.625} = 36$

WEB REINFORCEMENT (When required)

Length of Stiffeners

Locate symmetrical with mid-point of door

CHECK FOR LATERAL-TORSIONAL BUCKLING

GIVEN:

$$K^1 = .51$$

$$L = \text{Span} = 204$$

$$d = \text{Depth of Beam} = 24-1/2$$

$$b = \text{Width of Flange} = 13-1/2$$

$$T_f = \text{Thickness of Flange} = 1$$

$$1. \frac{K^1 L d}{b T_f} = \frac{.51 \times 204 \times 24-1/2}{13.5 \times 1} = 188.8$$

# BLAST COLUMN DESIGN

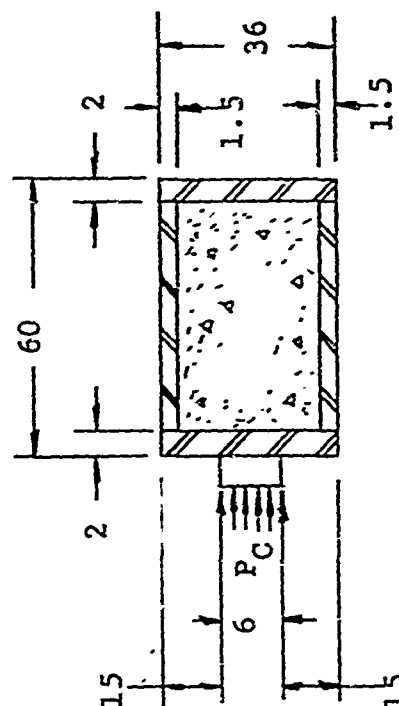
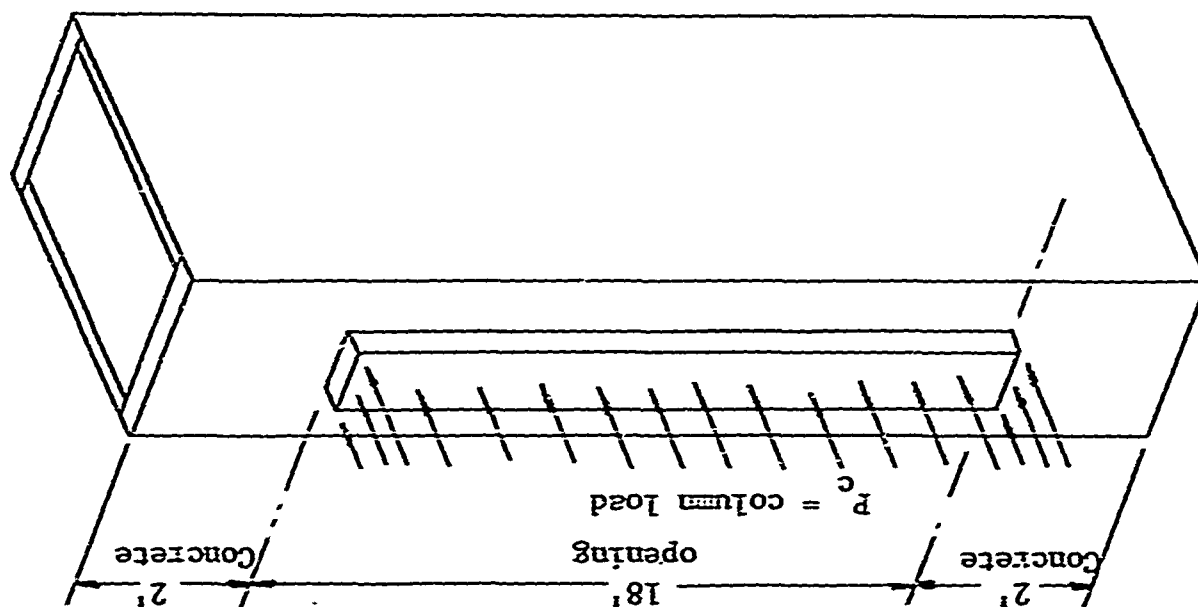
PLAN SECTION OF COLUMN

$$P_T = \text{Total Blast Load}$$
$$P_c = \text{Column Load} = \frac{P_T}{2}$$

$$P_T = H \times W \times P_R \times \frac{Z R_{EL}}{P_{Max.}} \times 144 = 18 \times 14 \times 197 \times 1.2 \times 144$$

**= 8,578 KIIPS**

$$P_C = \frac{P_T}{2} = \frac{3,578}{2} = 4,289 \text{ KIIPS}$$



BLAST COLUMN DESIGNA. COLUMN LOADING - NO ALLOWANCE FOR CONCRETE

$$S = \frac{M}{Z} \quad \begin{array}{l} M = \text{Maximum Bending Moment} \\ Z = \text{Section Modulus} \end{array}$$

$$M = \frac{wL^2}{8} = \frac{WL}{8}, \text{ since } W = wL$$

$$M = \frac{4,289 \times 216}{8} = 115,803 \text{ in. Kips}$$

$$S = \frac{M}{Z} = \frac{115,803,000 \text{ in}\cdot\text{#}}{5,503 \text{ in}^3} = 21,044 \text{ #/in}^2 < 41,600 \text{ #/in}^2$$

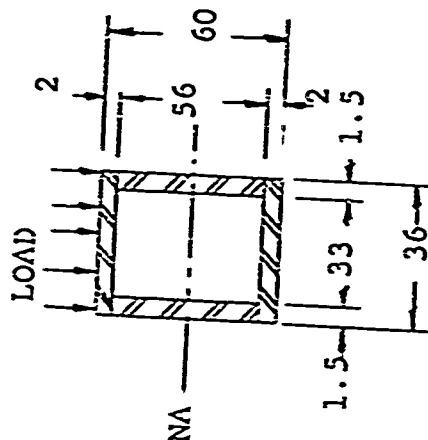
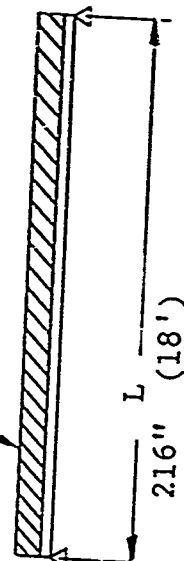
∴ Column section is satisfactory for bending stresses. Concrete filling of column will prevent buckling or twisting of column.

$$I_{na} = \frac{36 \times 60^3}{12} - \frac{30 \times 56^3}{12} = (3 \times 60^3) - (2.75 \times 56^3) = 165,078 \text{ in}^4$$

$$Z - \text{Section Modulus} = \frac{I_{na}}{c} = \frac{165,078 \text{ in}^4}{30 \text{ in.}} = 5,503 \text{ in}^3$$

$$W = P_c = 4289 \text{ KIPS}$$

$$w = \frac{W}{L} = 43.6 \text{ KIPS/IN}$$



BLAST COLUMN DESIGNB. COLUMN FRONT PLATE LOADING

Assume 1" wide strip and 45° stress distribution to concrete.

$$1. \quad W = \text{Column load per inch} = \frac{4,289 \text{ KIPS}}{216 \text{ in}} = 19,856 \#$$

$$2. \quad R_C = \text{Resistance of concrete} = S_C \times A$$

$$S_C = 3,900 \text{ PSI}$$

$$R_C = 3,900 \times 1 \times 9 = 42,900 \#$$

3. Thus steel must resist a load of  $(W - R_C)$  and  $(\text{in} - R_C)$  can be used as the applied load.

$$W - R_C = 19,856 - 35,100$$

$W_A$  = Since concrete resistance is enough, any steel plate is O.K.

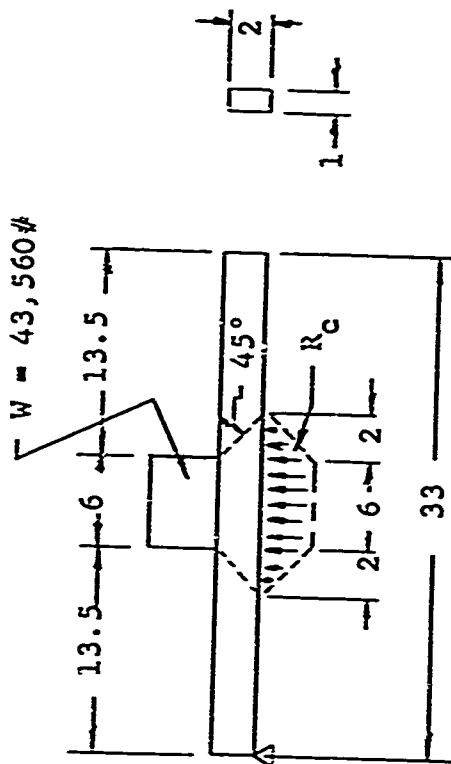
$$4. \quad S_g = \frac{M}{Z} \quad Z = \frac{bh^2}{6} = \frac{1 \times 3^2}{6} = 1.5$$

$$M_{\text{max}} = \left[ \left( 18 \frac{W_a}{2} \right) \right] + \frac{4 W_a}{2 \times 2}$$

$$M = 9 W_a + W_a = 10 W_a = 10 \times 660 = 6,600 \text{ in}\#$$

$$S_g = \frac{6600 \text{ in}\#}{1.5 \text{ in}^3} = 4,400 \#/\text{in}^2 < 41,600 \#/\text{in}^2$$

∴ 2" plate is O.K.





BLAST COLUMN DESIGNC. CONCRETE BEARING STRESS

Assume column set 24" in concrete

$$S_c = \frac{P}{A} \quad P = \text{Bearing Load} = \frac{P_c}{2}$$

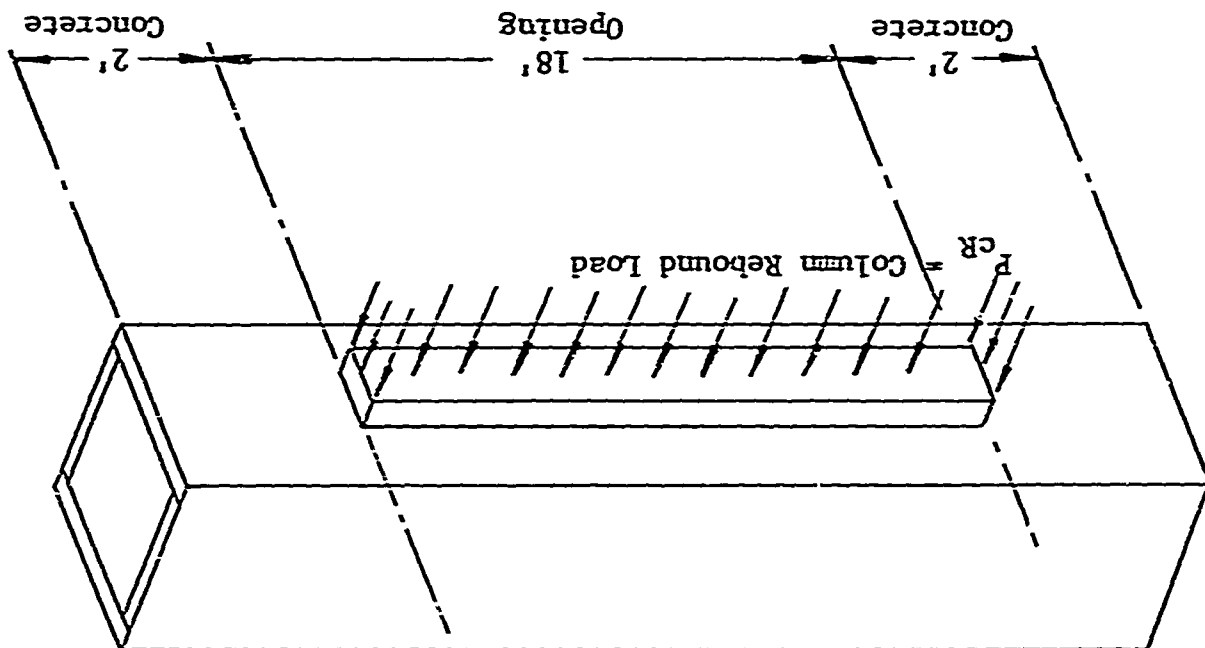
A = Bearing Area = W x h where W = column width

h = depth of column in concrete

$$S_c = \frac{P_c}{2A} = \frac{4.289 \text{ KIPS}}{2 \times 36 \times 24} = 2,482 \text{ KIPS/in}^2 < 3,900 \text{ \#/in}^2$$

∴ Column set 24" in concrete in O.K.

DOOR 60-12-19



REBOUND COLUMN DESIGN

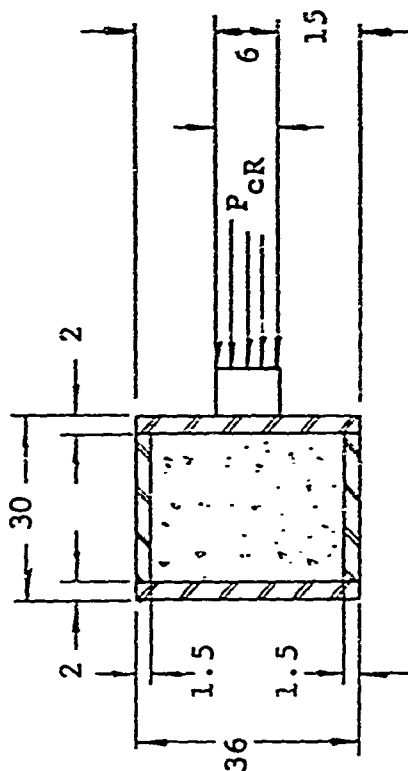
PLAN SECTION OF COLUMN

$P_c$  = Column Load (applied blast)

$P_{c_r}$  = Column Rebound Load

Assume 25% rebound

$$\text{Then } P_{c_r} = \frac{P_c}{4} = \frac{4,289}{4} \text{ KIPS} = 1,072 \text{ KIPS}$$



REBOUND COLUMN DESIGN

A. COLUMN LOADING - NO ALLOWANCE FOR CONCRETE

$$S = \frac{M}{Z} \quad \begin{matrix} M = \text{Maximum Bending Moment} \\ Z = \text{Section Modulus} \end{matrix}$$

$$M = \frac{wL^2}{8} = \frac{WL}{8}, \text{ since } W = wL$$

$$M = \frac{1,072 \times 216}{8} = 28,944 \text{ in. Kips}$$

$$S = \frac{M}{Z} = \frac{28,944,000 \text{ in}\#}{2,178} = 13,289\#/\text{in}^2 < 41,600\#/\text{in}^2$$

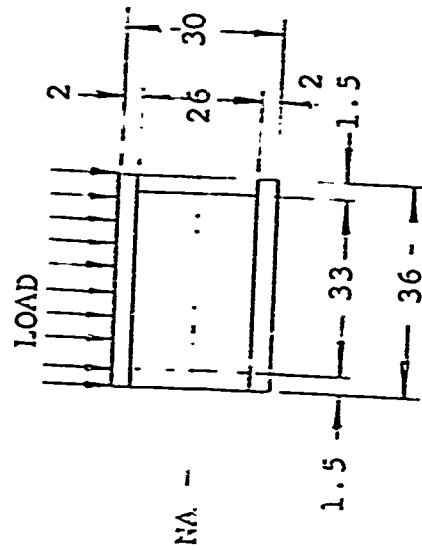
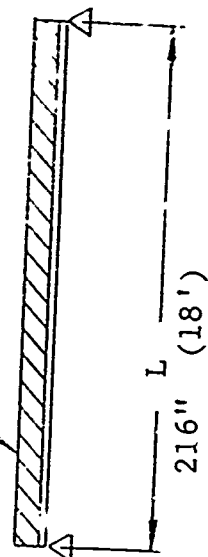
∴ Column section is satisfactory for bending stresses.  
Concrete filling will prevent buckling or twisting of column.

$$I_{na} = \frac{36 \times 30^3}{12} - \frac{33 \times 26^3}{12} = (3 \times 30^3) - (2.75 \times 26^3) = 32,660 \text{ in}^4$$

$$Z = \text{Section Modulus} = \frac{I_{na}}{c} = \frac{32,660 \text{ in}^4}{15 \text{ in}} = 2,178 \text{ in}^3$$

$$W = P_{CR} = 1072 \text{ KIPS}$$

$$w = 4962\#/\text{IN}$$



REBOUND COLUMN DESIGN

B. CHECK REBOUND COLUMN LOADED BY DIRECT BLAST ON COLUMN FACE -  
NO ALLOWANCE FOR CONCRETE

1.  $W_L = h \times W \times 144 \times 2P_r = 18 \times 3 \times 144 \times 394 = 3,064 \text{ KIPS}$

2.  $M = \frac{W_L L}{8} = \frac{3,064 \times 216}{8} = 82,128 \text{ in-Kips}$

3.  $S = \frac{M}{Z} \quad Z = 2,178 \text{ in}^3$

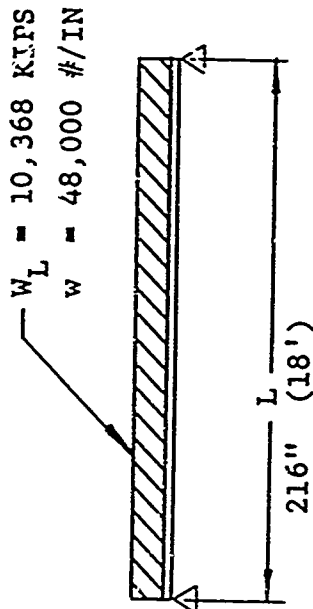
$S = \frac{82,728,000 \text{ in}^{\#}}{2,178 \text{ in}^3} = 37,983\#/\text{in}^2 \quad 41,600\#/\text{in}^2$

Since no allowance was made for concrete, the concrete fill will make this column strong enough to withstand a direct blast.

4. Concrete Bearing Stress  
Column set 36" into concrete

$S_c = \frac{P}{A} = \frac{P \times \frac{W_L}{2}}{A \times (48)(36)}$   
 $S_c = \frac{3064}{(2)(36)(15)} = 3 \text{ KIPS}/\text{IN}^2$   
 $S_c = 2837 \#/\text{IN}^2 \quad 3900 \#/\text{IN}^2$

∴ Column set 24" in concrete is O.K.



CALCULATIONS

2-WAY SPAN DOOR  
SOLID DESIGN  
SIMPLY SUPPORTED 4 SIDES  
2'-6" x 4'-0", 100 PSI

TRIAL NO. 1

ELASTO-PLASTIC  
DOOR NO. 60-12-26  
CALCULATIONS BY T.A.  
CHECKED BY H.S.

GIVEN:

t	= Assumed Thickness	=	2.50 Inches
T	= Load Duration	=	.050 Sec.
P <sub>r</sub>	= Peak Reflected Pressure	=	500 PSI
W	= Total Weight of Door	=	1021 Lbs.
a	= Short Span of Door	=	30 Inches
b	= Long Span of Door	=	48 Inches
β	= Timoshenko Moment Constant	=	.0862
α	= Timoshenko Deflection Constant	=	.0906
K <sub>LM</sub>	= Mass-Load Constant	=	$\frac{.74}{\text{ELASTIC}}$ $\frac{.58}{\text{PLASTIC}}$

Figure IV-4

FIND:

1. ELASTIC RESISTANCE (KIP)

$$R_{el} = \frac{6.933 \times t^2 \times b}{\beta \times a} = \frac{6.933 \times 2.50^2 \times 48}{.0862 \times 30}$$
$$= \frac{2079.90}{2.586} = 804$$

2. ELASTIC DEFLECTION (FEET)

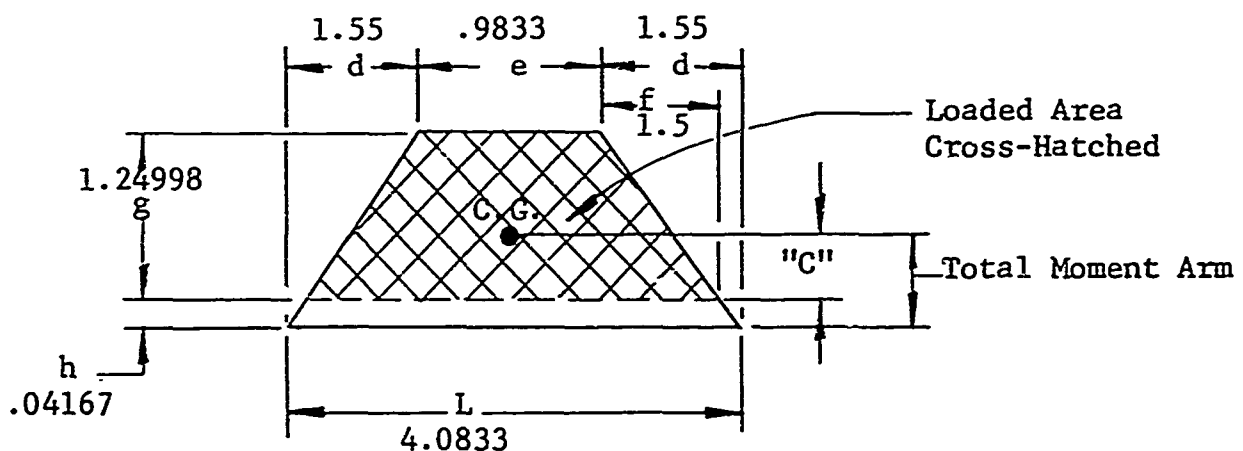
$$X_{el} = \frac{6.933 \times \alpha \times a^2}{360 \times 10^3 \times t \times \beta} = \frac{.0906 \times 30^2 \times 6.933}{360 \times 10^3 \times 2.5 \times .0862}$$
$$= \frac{565.31682}{77,580} = .007287$$

3. PLASTIC MOMENT (KIP-Inch/Inch)

$$M_p = 10.4 \times t^2 = 10.4 \times 2.5^2 = 65$$

4. ASSUMED TRAPEZOID FOR CRACK-LINE SECTION

(All dimensions in feet)

5. AREA OF TRAPEZOID LOADED (SQUARE FEET)

$$A = (f + e) \times g = (1.5 + .9833) \times 1.24998 = 3.10408$$

6. MOMENT ARM "c" (FEET)

$$\begin{aligned} "c" &= \frac{\frac{f \times g^2}{3} + \frac{e \times g^2}{2}}{A} \\ &= \frac{\frac{1.5 \times 1.24998^2}{3} + \frac{.9833 \times 1.24998^2}{2}}{3.10408} \\ &= .49915 \end{aligned}$$

7. TOTAL MOMENT ARM (FEET)

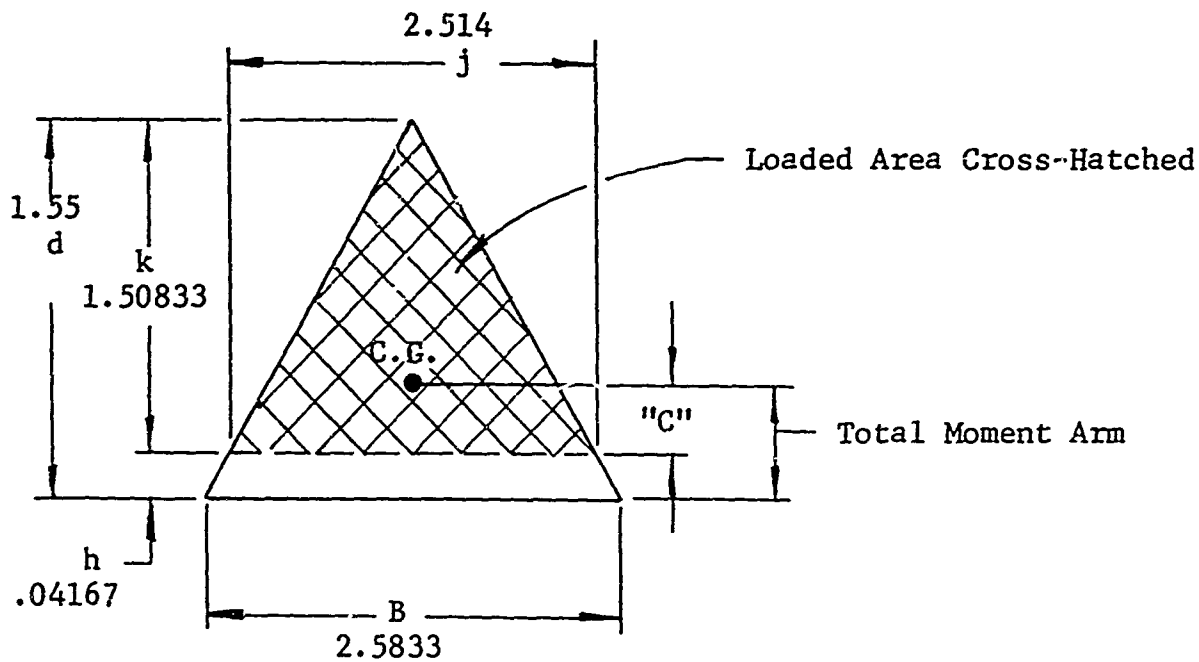
$$TMA = "c" + h = .4991511 + .04167 = .54082$$

8. UNIT RESISTANCE (Kip/Foot<sup>2</sup>)

$$R_{unit} = \frac{M_p \times L}{TMA \times A} = \frac{65 \times 4.0833}{.54082 \times 3.10408} = 158$$

9. ASSUMED TRIANGLE FOR CRACK-LINE SECTION

(All dimensions in feet)



10. AREA OF TRIANGLE LOADED (SQUARE FEET)

$$A = 1/2 \times k \times j = 1/2 \times 1.50833 \times 2.514 = 1.8960$$

11. MOMENT ARM "c" (FEET)

$$"c" = \frac{k}{3} = \frac{1.50833}{3} = .50278$$

12. TOTAL MOMENT ARM (FEET)

$$TMA = "c" + h = .50278 + .04167 = .54445$$

13. UNIT RESISTANCE (Kip/Foot<sup>2</sup>)

$$\begin{aligned} R_{\text{unit}} &= \frac{M_p \times E}{TMA \times A} = \frac{65 \times 2.5833}{.54445 \times 1.8960} \\ &= \frac{167.9145}{1.032277} = 163 \end{aligned}$$

14. TOTAL EFFECTIVE RESISTANCE (KIP)

$$\begin{aligned} R_1 &= 2 \times (R_{\text{unit}} \times A + R_{\text{unit}} \times A) \times .80 \\ &= 2 \times (158 \times 3.10408) + (163 \times 1.8960) \times .80 \\ &= 1.60 \times 799.49 = 1279 \end{aligned}$$

15. PEAK LOAD (KIP)

$$P_o = \frac{P_r \times a \times b}{1,000} = \frac{500 \times 30 \times 48}{1,000} = 720$$

16. ELASTIC SPRING CONSTANT (Kip/Foot)

$$K_1 = \frac{R_{el}}{X_{el}} = \frac{804}{.007287} = .110333 \times 10^6$$



17. PLASTIC SPRING CONSTANT (Kip/Foot)

$$\text{(Assume } X_1 = 3 X_{e1}\text{)}$$

$$K_2 = \frac{R_1 - R_{e1}}{X_1 - X_{e1}} = \frac{1272 - 804}{.005757} = \frac{475}{.005757}$$

$$= .082508 \times 10^6$$

18. EFFECTIVE MASS (Kip - Sec<sup>2</sup>/Foot)

$$M_e = \frac{W \times K_{LM}}{32,200} = \frac{1021 \times .74}{32,200} = .023464$$

$$M_p = \frac{W \times K_{LM}}{32,200} = \frac{1021 \times .58}{32,200} = .018391$$

19. NATURAL PERIOD (SECONDS)

$$T_n = 2\pi \times \sqrt{\frac{M_e}{K_1}}$$

$$= 6.2832 \times \sqrt{\frac{.023464}{.110333 \times 10^6}}$$

$$= 6.2832 \times \sqrt{.000000212665295}$$

$$= 6.2832 \times .0004612 = .002898$$

20. CONSTANTS FOR EXTRAPOLATION TABLEELASTIC

$$a. \frac{T_n}{10} = \frac{.0029}{10} = .00029 \text{ Sec.}$$

$$b. \triangle t = .0002 \text{ Sec.}$$

$$c. (\triangle t)^2 = 4 \times 10^{-8} \text{ Sec.}^2$$

$$d. P_o = 720 \text{ Kip}$$

$$e. P_1 = P_o \left( 1 - \frac{\triangle t}{.050} \right) = 720 \left( 1 - \frac{.0002}{.050} \right) \\ = 717 \text{ KIP}$$

$$f. P_o - P_1 = 720 - 717 = 3 \text{ Kip}$$

$$g. a_o = \frac{1}{m_e} \times \left( \frac{P_o}{2} + \frac{P_1 - P_o}{6} \right) \\ = \frac{1}{.023464} \left( \frac{720}{2} - \frac{3}{6} \right) = 15,321$$

$$h. x_1 = a_o \times (\triangle t)^2 = 15,321 \times 4 \times 10^{-8} \\ = .000613 \text{ ft.}$$

$$i. \frac{(\triangle t)^2}{m_e} = \frac{4 \times 10^{-8}}{.023464} = 170 \times 10^{-8}$$

DOOR 60-12-26 - T1

ELASTO-PLASTIC

$$M_e \hat{=} M_{ep}$$

\* PLASTIC (For  $X_1$   $3X_{el}$  only)

$$a. \frac{(\triangle t)^2}{m_p} =$$

$$b. \bar{K}_2 =$$

$$c. R_{el} =$$

$$d. R_x = R_{el} + K_2 (X_x - X_{el})$$

\* Not used this calculation

ACCELERATION IMPULSE EXTRAPOLATION TABLE

$X_{e1} = .007287$        $R_{e1} = 804$        $K_1 = 110,333$        $K_2 = 82,508$

N	t (Sec.)	$P_n$ (Kips)	$R_n$ (Kips)	$P_n - R_n$ (Kips)	$\frac{(\Delta t)^2}{m}$	$A_n (\Delta t)^2$ (Feet)	$2 X_n$ (Feet)	$X_n - 1$ (Feet)	$X_n + 1$ (Feet)	Remarks
0	0	720	0	720	$170 \times 10^{-8}$	.000613	0	0	0	
1	.0002	717	68	649	"	.001103	.001226	0	.000613	
2	.0004	714	257	457	"	.000777	.004568	.000613	.002329	
3	.0006	711	532	179	"	.000304	.009644	.002329	.004822	ELASTIC
4	.0008	708	831	-123	"	-.000209	.015238	.004822	.007619	
5	.0010	705	1045	-340	"	-.000578	.020414	.007619	.010207	
6	.0012	702	1210	-508	"	-.000864	.024434	.010207	.012217	
7	.0014	699	1305	-606	"	-.001030	.026726	.012217	.013363	
8	.0016	696	1315	-619	"	-.001052	.026958	.013363	.013479	MAX.
9	.0018	693	1212	-519	"	-.000882	.025086	.013479	.012543	
10	.0020	690	1011	-321	"	-.000546	.021450	.012543	.010725	
11	.0022	687	750	-63	"	-.000107	.016722	.010725	.008361	
12	.0024	684	478	206	"	.000350	.011780	.008361	.005890	
13	.0026	681	244	437	"	.000743	.007538	.005890	.003769	
14	.0028	678	92	586	"	.000996	.004782	.003769	.002391	
15	.0030	675	49	626	"	.001064	.004018	.002391	.002009	MIN.
16								.002009	.002691	
17										
18										
19										
20										
21										

RESULTS

Maximum Deflection = .013479  
 Elastic Deflection = .007287  
 Permanent Deflection = .006192

Ratio =  $\frac{1315}{720} = 1.83$

Max. Rebound =

At .5" allowable total deflection - will take 6.7 max. blasts

R<sub>x</sub> TABLE (T = .05)

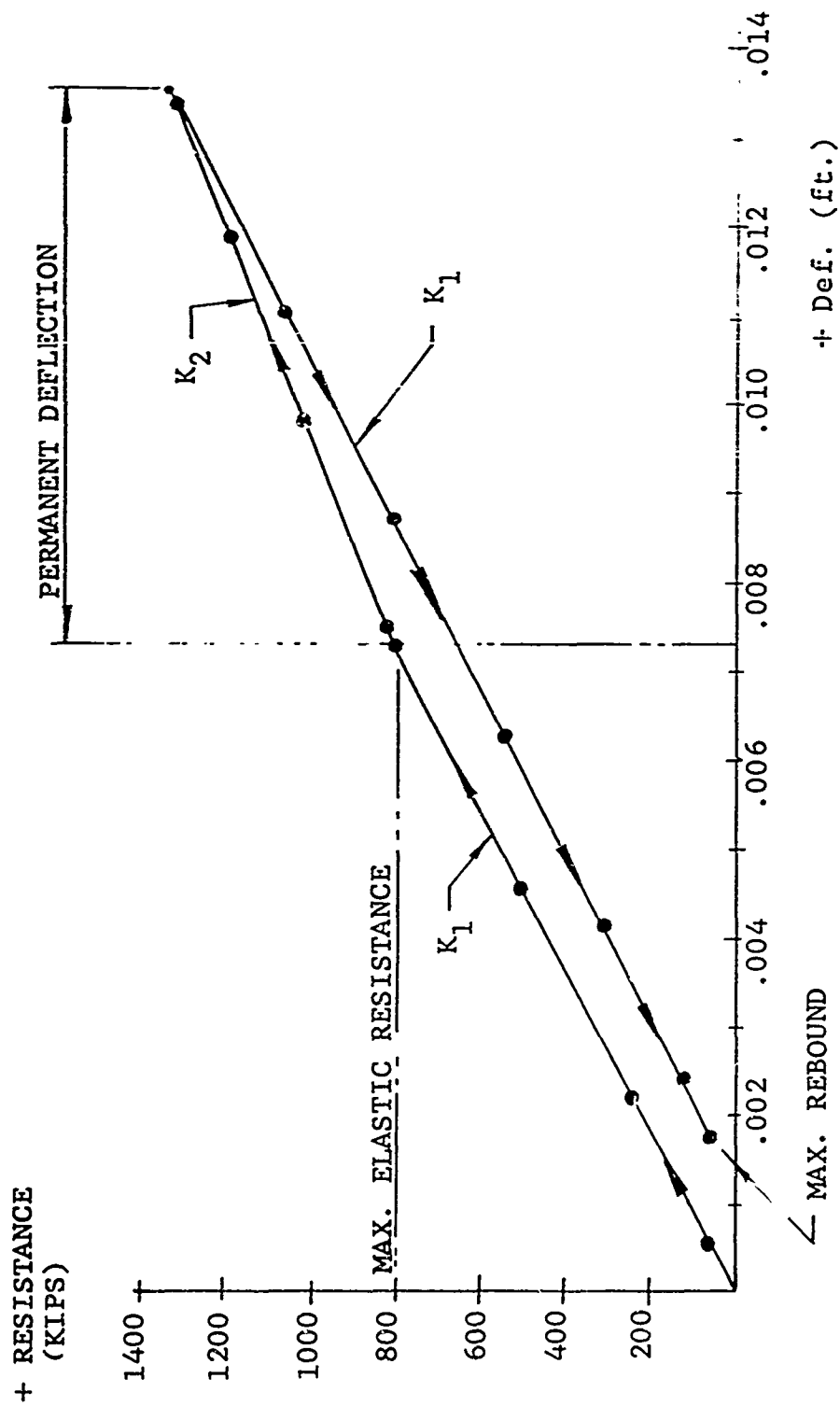
Plastic Range to Maximum R<sub>x</sub>

X <sub>x</sub>	X <sub>el</sub>		K <sub>2</sub>		R <sub>el</sub>	R <sub>x</sub>
.007619	.007287	.000332	82,508	27	804	831
.010207	"	.002920	"	241	"	1045
.012217	"	.004930	"	406	"	1210
.013363	"	.006076	"	501	"	1305
.013479	"	.006192	"	511	"	1315

# R<sub>x</sub> TABLE

Maximum R<sub>x</sub> to Minus R<sub>el</sub>

$\bar{R}_{Max.} -$	$\left[ \left( \bar{X}_{Max.} - \bar{X}_x \right) \right] =$	$\times \bar{K}_1 =$	$= \bar{R}_x$			
1315	.013479	.012543	.000936	110,333	103	1212
"	"	.010725	.002754	"	304	1011
"	"	.008361	.005118	"	565	750
"	"	.005890	.007589	"	837	478
"	"	.003769	.009710	"	1071	244
"	"	.002391	.011088	"	1223	92
"	"	.002009	.011470	"	1266	49



Scale:	Approved by:	
DOOR NO. 60-12-26 - T1		
2-1/2" THICK SOLID STEEL - 100 PSI INCIDENT		
LOAD DURATION - .050 Sec.		

20. CONSTANTS FOR EXTRAPOLATION TABLE (T = .0041)ELASTIC

$$a. \frac{T_n}{10} = \frac{.0029}{10} = .00029$$

$$b. \Delta t = .0002$$

$$c. (\Delta t)^2 = 4 \times 10^{-8}$$

$$d. P_o = \frac{P_r \times A}{1,000} = 720 \text{ KIP}$$

$$e. P_1 = P_o \left( 1 - \frac{\Delta t}{.0041} \right) = 720 \left( 1 - \frac{.0002}{.0041} \right) = 685 \text{ KIP}$$

$$f. P_o - P_1 = 720 - 685 = 35 \text{ KIP}$$

$$g. a_o = \frac{1}{m_e} \times \left( \frac{P_o}{2} + \frac{P_1 - P_o}{6} \right)$$

$$= \frac{1}{.023464} \left( \frac{720}{2} - \frac{35}{6} \right) = 15,094$$

$$h. X_1 = a_o \times (\Delta t)^2 = 15,094 \times 4 \times 10^{-8} = .000604$$

$$i. \frac{(\Delta t)^2}{m_e} = \frac{4 \times 10^{-8}}{.023464} = 170 \times 10^{-8}$$

ELASTO-PLASTIC

$$M_e \approx M_{ep}$$

\* PLASTIC

\* Not used this calculation



ACCELERATION IMPULSE EXTRAPOLATION TABLE

$X_{e1} = .007287$        $R_{e1} = 804$        $K_1 = 110,333$        $K_2 = 82,508$

N	t (Sec.)	P <sub>n</sub> (Kips)	R <sub>n</sub> (Kips)	P <sub>n</sub> - R <sub>n</sub> (Kips)	$\frac{(\Delta t)^2}{m}$	A <sub>n</sub> (Δt) <sup>2</sup> (Feet)	2 X <sub>n</sub> (Feet)	X <sub>n</sub> - .1 (Feet)	X <sub>n</sub> + .1 (Feet)	Remarks
0	0	720	0	720	$170 \times 10^{-6}$	.000604	0	0	0	
1	.0002	685	67	618	"	.001051	.001208	0	.000604	
2	.0004	650	249	401	"	.000682	.004518	.000604	.002259	
3	.0006	615	507	108	"	.000182	.009192	.002259	.004596	
4	.0008	580	785	-205	"	-.000349	.014230	.004596	.007115	
5	.0010	545	971	-426	"	-.000724	.018570	.007115	.009285	
6	.0012	510	1088	-578	"	-.000983	.021462	.009285	.010731	
7	.0014	475	1126	-651	"	-.001107	.022388	.010731	.011194	MAX.
8	.0016	440	1055	-615	"	-.001046	.021100	.011194	.010550	
9	.0018	405	868	-463	"	-.000787	.017720	.010550	.008860	
10	.0020	370	595	-225	"	-.000383	.012766	.008860	.006383	
11	.0022	335	280	55	"	.000094	.007046	.006383	.003523	
12	.0024	300	-24	324	"	.000551	.001550	.003523	.000775	
13	.0026	265	-266	531	"	.000903	-.002844	.000775	-.001422	
14	.0028	230	-409	639	"	.001086	-.005432	-.001422	-.002716	
15	.0030	195	-432	627	"	.001066	-.005848	-.002716	-.002924	REVERSE
16								-.002924	-.002066	
17										
18										
19										
20										
21										

Ratio =  $\frac{432}{1315} = 32.9\%$

Max. Rebound = 432 Kips

DOOR 60-12-26 - T1

R<sub>x</sub> TABLE (T = .0041)

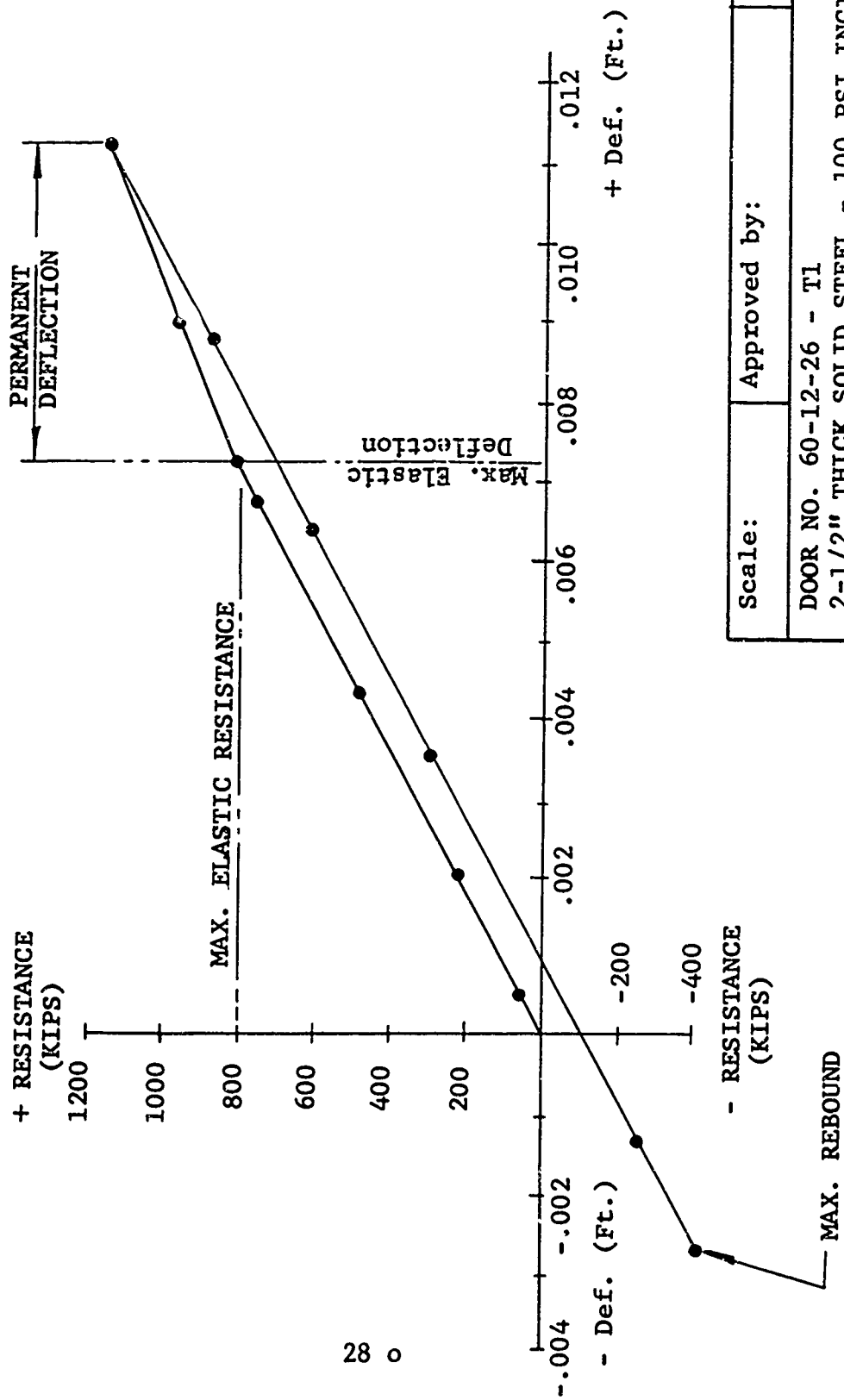
Plastic Range to Maximum R<sub>x</sub>

X <sub>x</sub>	X <sub>el</sub>	X <sub>2</sub>	R <sub>el</sub>	R <sub>x</sub>		
.009285	.007287	.001998	82,508	167	804	971
.010731	"	.003444	"	284	"	1088
.011194	"	.003907	"	322	"	1126

R<sub>x</sub> TABLE

Maximum R<sub>x</sub> to Minus R<sub>el</sub>

R <sub>Max.</sub>	[ ( X <sub>Max.</sub> - X <sub>x</sub> ) =	X	K <sub>1</sub>	= ]	= R <sub>x</sub>
1126	.011194	.010550	.000644	110,333	71 1055
"	"	.008860	.002334	"	258 868
"	"	.006383	.004811	"	531 595
"	"	.003523	.007671	"	846 280
"	"	.000775	.010419	"	1150 - 24
"	"	-.001422	.012616	"	1392 -266
"	"	-.002716	.013910	"	1535 -409
"	"	-.002924	.014118	"	1558 -432



28 o

Scale:	Approved by:
DOOR NO. 60-12-26 - T1	
2-1/2" THICK SOLID STEEL - 100 PSI INCIDENT	
LOAD DURATION - .0041 Sec.	

DOOR 60'-12-26

BEARING STRESS

A =  
B = 32  
C = 50  
D = 48  
E = 18  
F = 1.6  
T = 1

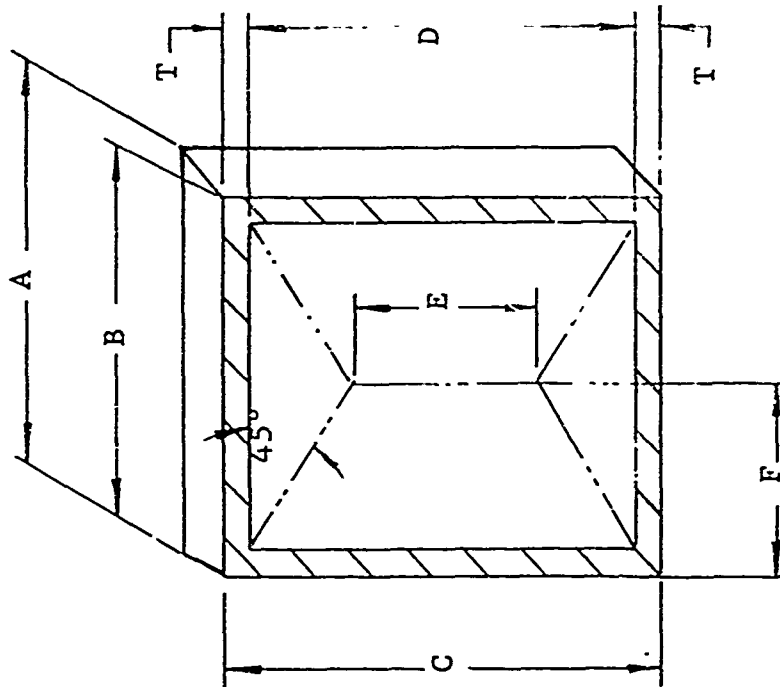
$R_M$  = Maximum Door Resistance = 1,315,000

Bearing Stress (along long edge is a maximum) =

$$\frac{R_M \times \frac{(C + E)}{2} \times F}{B \times C \times D \times T} = \frac{1,315,000 \times 34 \times 16}{32 \times 50 \times 48 \times 1} = \frac{44,710,000}{4,800}$$

$S_B = 9,315$  for  $T = 1"$

Use  $T = 1/2"$  ( $S_B = 18,730\#/D"$ )



VERTICAL STRIKER THICKNESS CALCULATION

Take a typical 1" long vertical strip.

$$\text{Average Force per Lineal Inch} = F = S_B \times T = 9,315$$

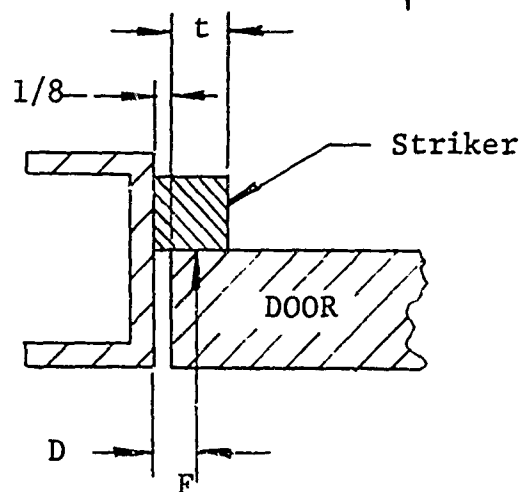
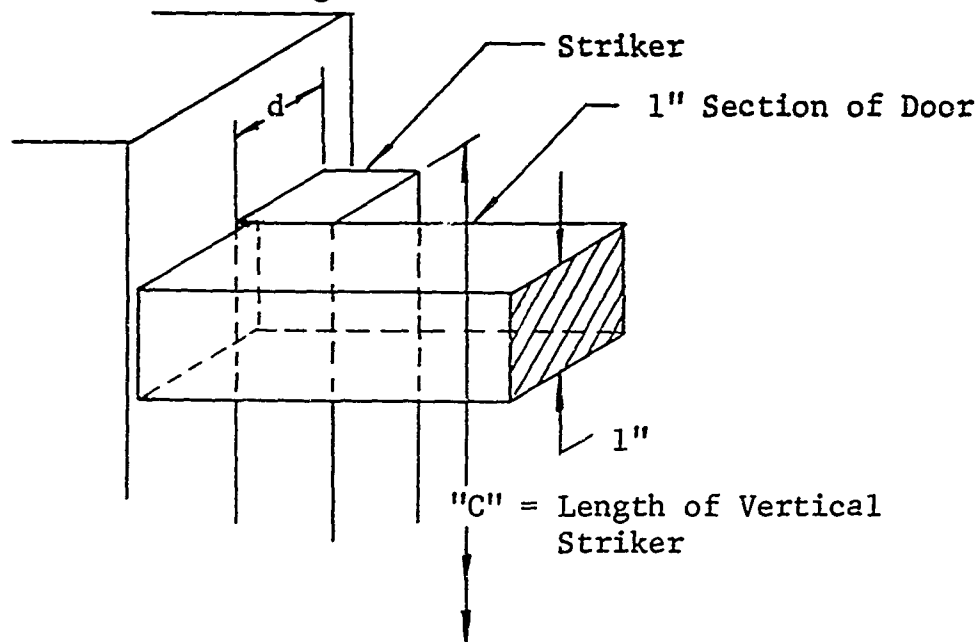
$$\text{Bending Moment} = M_b = F \times D = 9,315 \times .625 = 5,822$$

$$\begin{aligned} \text{Minimum Required Thickness} = d &= \sqrt{\frac{6 M_b}{41,600}} = \sqrt{\frac{34,932}{41,600}} \\ &= \sqrt{.839712} = .916 \quad (\text{for } T = 1") \end{aligned}$$

Use  $d = 3/4"$  (.7117 Min.) (for  $T = 1/2"$ )

$F_c$  = Total force on vertical striker

41,600 = allowable bending stress



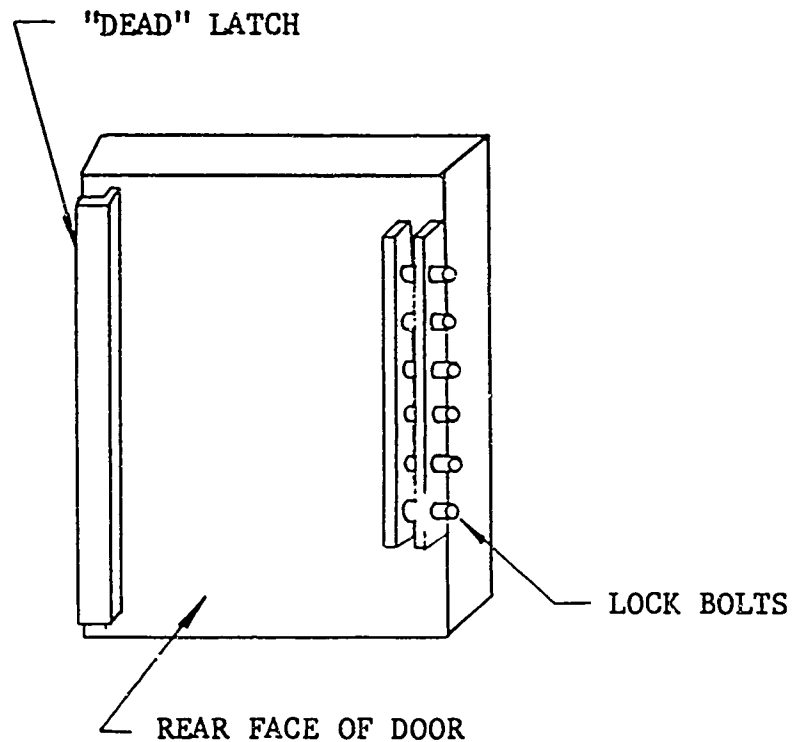
REBOUND LOAD CALCULATION FOR LOCK BOLTS

Consider rebound resisted equally by "dead latch" and lock bolts.

Then:

$$\begin{aligned}\text{Rebound force per bolt} = P &= \frac{\text{Max. Rebound Force}}{2 \times \text{no. of lock bolts}} \\ &= \frac{432,000}{8} = 54,000\end{aligned}$$

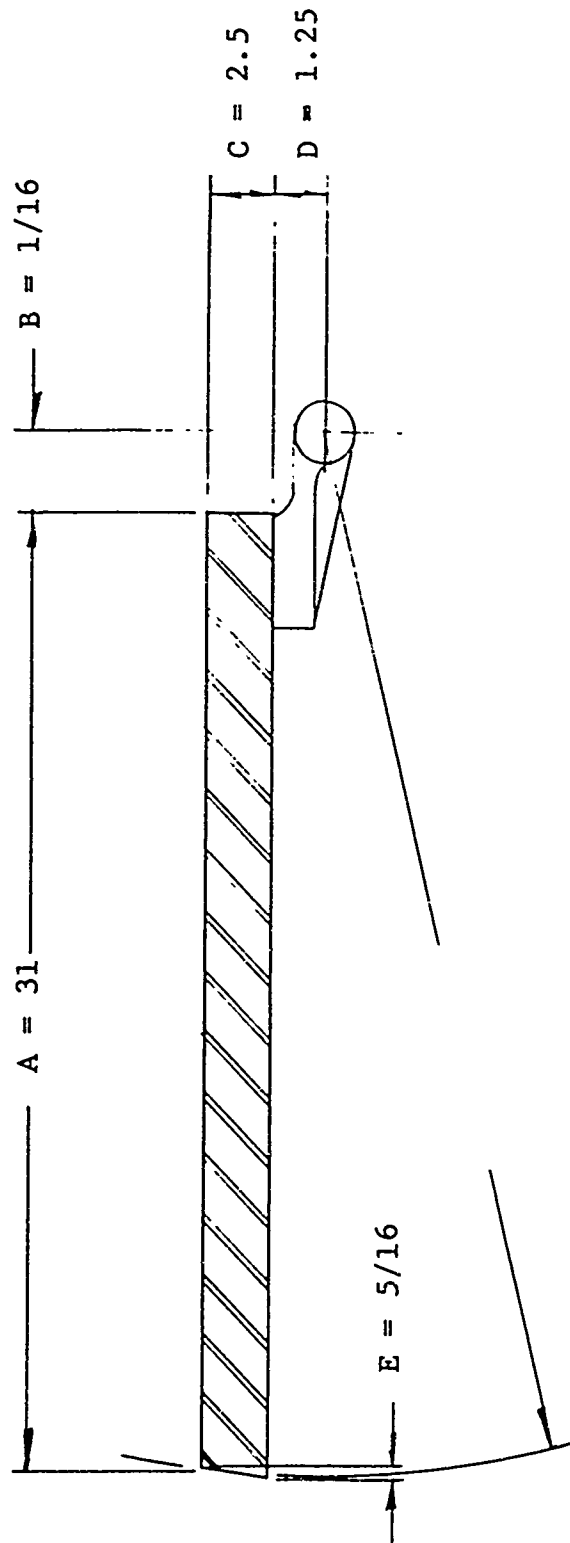
Maximum total rebound force is obtained from rebound calculations.







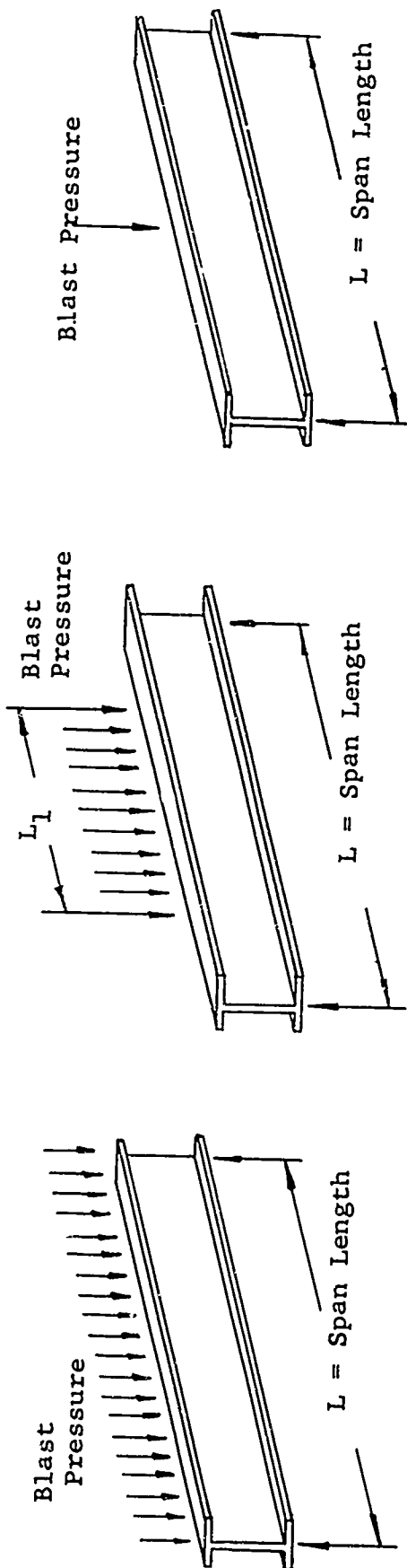
CALCULATIONS - DOOR SWING AND DOOR TAPER



$$\text{Swing} = S = \sqrt{(A + B)^2 + (C + D)^2} = \sqrt{(31.0625)^2 + (3.75)^2} = \sqrt{978.94140625} = 31.2880$$

$$\text{Taper} = E = \frac{C^2 + CD}{(A + B)} = \frac{6.25 + 3.125}{31.0625} = \frac{9.375}{31.0625} = .30181 \quad \text{Use } 5/16''$$

# $K_{LM}$ FACTOR FOR VARIOUS BEAM BLAST LOADING CONDITIONS



UNIFORM BLAST LOADING OVER ENTIRE SPAN

Strain Range	Load-Mass Factor $K_{LM}$
Elastic	.78
Plastic	.66

SYMMETRICAL UNIFORM BLAST LOADING OVER PART OF SPAN

Strain Range	Load-Mass Factor $K_{LM}^*$
Elastic	$384 \times L^3 / \pi^4 (8L^3 + L_1^3 - 4LL_1^2)$
Plastic	$2L / (3(2L - L_1))$
Elasto-Plastic	$.5(K_{LM_e} + K_{LM_p})$

\* Expressed in terms of L and  $L_1$

CONCENTRATED BLAST LOAD AT MID-POINT

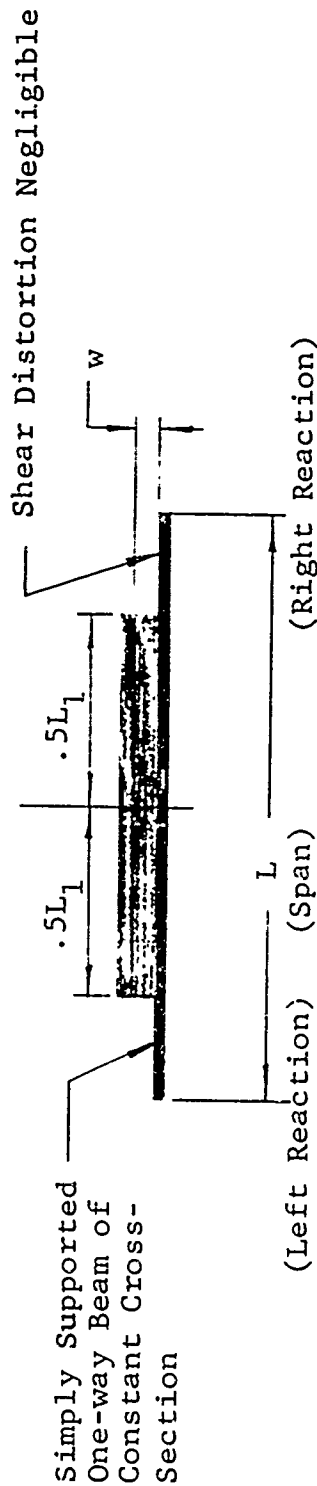
Strain Range	Load-Mass Factor $K_{LM}$	
	A	B
Elastic	1.0	.49
Plastic	1.0	.33

A = Concentrated Mass  
B = Uniform Mass

Figure IV-5

# DERIVATION OF $K_{LM}$ FOR BEAM

## PARTIALLY LOADED SPAN



GIVEN:

Simply supported one-way beam of constant cross-section

FIND:

$K_{LM}$  - Elastic and Plastic

$$\text{Total Load} = w \times L_1 = W$$

$$\text{Spring Constant} = k = \frac{384 \times E \times I}{(8L^3 + L_1^3 - 4LL_1^2)}$$

## ELASTIC

$$2\pi \times \sqrt{\frac{m_e}{k}} = \frac{2}{\pi \times n^2} \times \sqrt{\frac{m \times L^3}{E \times I}}$$

$$\frac{\pi^2 \times m_e}{k} = \frac{m \times L^3}{2 \times \pi \times E \times I}$$

(Consider fundamental mode only  
 $n = 1$ )

$$K_{LM_e} = \frac{m_e}{m} = \frac{k \times L^3}{\pi^4 \times E \times I} = \frac{384 \times E \times I \times L^3}{\pi^4 \times E \times I \times (8L^3 + L_1^3 - 4LL_1^2)}$$

$$= \frac{384 L^3}{\pi^4 (8L^3 + L_1^3 - 4LL_1^2)}$$

### PLASTIC

$$\frac{W}{2} \times L_o - M_E = \frac{I_{AB} \times \dot{X}_G}{\frac{L}{2}} \quad \left( \text{Where } L_o = \frac{L}{2} - \frac{L_1}{4} \right)$$

$$W - 2 M_D = \frac{4 I_{AB} \times \dot{X}_{CL}}{L \times L_o} = m_e \times \dot{X}_{CL}$$

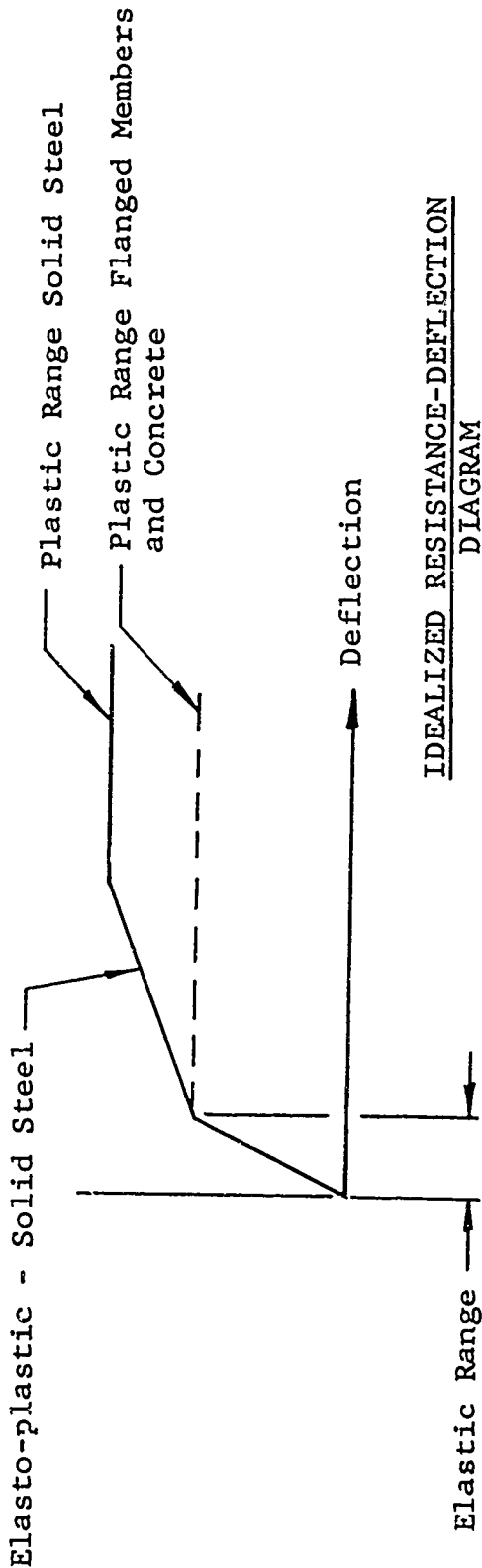
$$m_e = \frac{4 I_{AB}}{L \times L_o} = \frac{4}{L \times L_o} \times \frac{m L^2}{24_6}$$

$$K_{LM_p} = \frac{m_e}{m} = \frac{m \times L}{m \times 6 \times L_o} = \frac{L}{6L_o} = \frac{4 \times L}{6(2L - L_1)} = \frac{2 \times L}{3(2L - L_1)}$$

### ELASTO-PLASTIC

$$K_{LM_{ep}} \approx .05 (K_{LM_e} + K_{LM_p})$$

# DERIVATION OF $K_{LM}$ FOR BEAM - PARTLY LOADED SPAN



IDEALIZED RESISTANCE-DEFLECTION  
DIAGRAM

## MAXIMUM POSSIBLE ERRORS USING FIRST MODE ONLY - ELASTIC RANGE

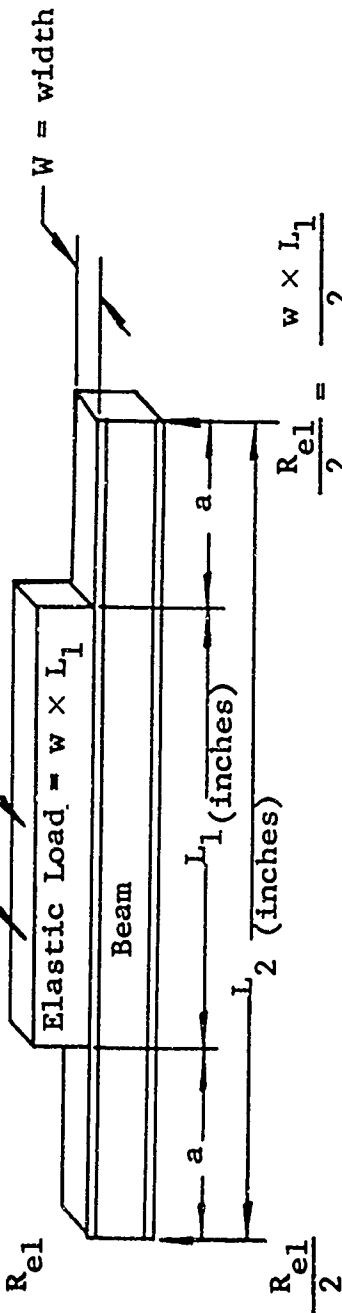
UNIFORM LOAD ( $\frac{T}{T_n} > 2$ )		CONCENTRATED LOAD ( $\frac{T}{T_n} > 2$ )	
Absolute*	Average**	Absolute*	Average**
< 14%	< 2%	< 70%	
< 5%		~ 0	< -10%
< 1%		~ 0	

\* Assuming Maximums of all Modes Occur Simultaneously and Neglecting Damping

\*\* Using Average of all Modes and Neglecting Damping

# DERIVATION OF $R_{el}$ , $X_{el}$ , and $K_1$ FOR PARTIALLY LOADED SPAN

GIVEN:  $a = \frac{L_2 - L_1}{2}$   
 FIND:  $R_{el}$   
 $P_e = \text{Elastic Pressure (Unit) = PSI}$   
 $w = \text{Pressure per Unit of Length} = W \times P_e \text{ \# / inch}$   
 $W = \text{width}$



$$R_{el} = w \times L_1 = \frac{w \times 8M}{w (2L_2 - L_1)} = \frac{8M}{(2L_2 - L_1)} = \frac{332.8 S}{(2L_2 - L_1)} \text{ K-}\#$$

or, if  $L_1$  and  $L_2$  are in feet:

$$R_{el} = \frac{332.8 S}{12(2L_2 - L_1)} = \frac{27.73333 S}{(2L_2 - L_1)} \text{ K-}\#$$

$$M_{elastic} = M_{max. @ center} = \left[ \frac{w \times L_1}{2} \times \frac{L_2}{2} - \frac{w \times L_1 \times L_2}{4} \right] = \frac{w \times L_1^2}{8}$$

$$= \frac{w \times w \times L_1 \times L_2}{8} = \frac{wL_1^2}{8} (2L_2 - L_1) \text{ or } L_1 = \frac{8M}{w(2L_2 - L_1)}$$

Figure IV-6

GIVEN:  $w$  = Elastic load per lineal inch

FIND:  $X_{el}$  @  $x = \frac{L_2}{2}$

$$\begin{aligned}
 X_{el} &= 2 \int_a^{\frac{L_2}{2}} \frac{wxdx}{48 EI} (3L_2^2 - 4x^2) \\
 &= \frac{2w}{48 EI} \left[ 3L_2^2 \int_a^{\frac{L_2}{2}} xdx - 4 \int_a^{\frac{L_2}{2}} x^3 dx \right] = \frac{2w}{48 EI} \left\{ 3L_2^2 \left[ \frac{x^2}{2} \right]_a^{\frac{L_2}{2}} - 4 \left[ \frac{x^4}{4} \right]_a^{\frac{L_2}{2}} \right\} \\
 &= \frac{2w}{48 EI} \left\{ 3L_2^2 \left( \frac{L_2^2}{8} - \frac{a^2}{2} \right) - 4 \left( \frac{L_2^4}{64} - \frac{a^4}{4} \right) \right\} \\
 &= \frac{w}{24 EI} \left( \frac{3 L_2^4}{8} - \frac{3 a^2 L_2^2}{2} - \frac{4 L_2^4}{64} + \frac{4 a^4}{4} \right) \\
 &= \frac{w}{24 EI} \left( \frac{5}{16} L_2^4 - \frac{3 a^2 L_2^2}{2} + a^4 \right)
 \end{aligned}$$

But:  $a = \frac{L_2 - L_1}{2}$

$$\therefore X_{el} = \frac{w}{24 EI} \left[ \frac{5}{16} L_2^4 - \frac{3}{2} L_2^2 \left( \frac{L_2 - L_1}{2} \right)^2 + \left( \frac{L_2 - L_1}{2} \right)^4 \right]$$

[Timoshenko "Strength of Materials"  
2nd Edition, Part 1, Page 158]

$$\begin{aligned}
X_{e1} &= \frac{w}{24EI} \left[ \frac{5}{16} L_2^4 - \frac{3}{2} L_2^2 \left( \frac{L_2^2 - 2L_1L_2 + L_1^2}{4} \right) + \frac{L_2^2 - 4L_1L_2^3 + 6L_1^2L_2^2 - 4L_1^3L_2 + L_1^4}{16} \right] \\
&= \frac{w}{24EI} \left[ \frac{5}{16} L_2^4 - \frac{3}{8} (L_2^4 - 2L_1L_2^3 + L_1^2L_2^2) + \frac{L_2^2}{16} - \frac{1}{4} L_1L_2^3 + \frac{3}{8} L_1^2L_2^2 - \frac{1}{4} L_1^3L_2 + \frac{L_1^4}{16} \right] \\
&= \frac{w}{24EI} \left( \frac{5}{16} L_2^4 - \frac{3}{8} L_2^4 + \frac{3}{4} L_1L_2^3 - \frac{3}{8} L_1^2L_2^2 + \frac{L_2^2}{16} - \frac{1}{4} L_1L_2^3 + \frac{3}{8} L_1^2L_2^2 - \frac{1}{4} L_1^3L_2 + \frac{L_1^4}{16} \right) \\
&= \frac{w}{24EI} \left( \frac{1}{2} L_1L_2^3 - \frac{1}{4} L_1^3L_2 + \frac{L_1^4}{16} \right)
\end{aligned}$$

But:  $w = \frac{332.8 \times S}{L_1(2L_2 - L_1)} - K \text{ \#/Lineal Inch (per page 30 c)}$

$$\begin{aligned}
\therefore X_{e1} &= \frac{332.8 \times S}{L_1(2L_2 - L_1)} \times \frac{L_1}{24EI} \left( \frac{L_2^3}{2} - \frac{L_1^2L_2}{4} + \frac{L_1^3}{16} \right) \text{ Kip Inches} \\
&= \frac{.46222 \times 10^{-6}}{(2L_2 - L_1)} \times \frac{S}{I} \left( \frac{8L_2^3 - 4L_1^2L_2 + L_1^3}{16} \right) \quad " \quad " \\
&= 28.8888 \times 10^{-6} \times \frac{S}{I} \left( \frac{8L_2^3 - 4L_1^2L_2 + L_1^3}{2L_2 - L_1} \right) = .00002888 \times \frac{S}{I} \left( \frac{8L_2^3 - 4L_1^2L_2 + L_1^3}{2L_2 - L_1} \right)
\end{aligned}$$

or, if  $L_1$  and  $L_2$  are in feet:

$$X_{e1} = .000346666 \times \frac{S}{I} \left( \frac{8L_2^3 - 4L_1^2L_2 + L_1^3}{2L_2 - L_1} \right)$$

Check this formula for case where  $L_2 = L_1 = L$  :  $X_{e1} = \frac{w}{24EI} \left( \frac{L^4}{2} - \frac{L^4}{4} + \frac{L^4}{16} \right)$

$$= \frac{w}{24EI} \left( \frac{5}{16} L^4 \right) = \frac{5 w L^4}{384 EI} \quad - \text{ Formula checks}$$



$$\text{Elastic Moment} = 41,600 \times S \text{ " \#} = M_{el} \quad (1)$$

$$\text{Also, Elastic Moment} = \frac{w L_1}{8} (2L_2 - L_1) = M_{el} \quad (2)$$

$$\text{or } w = W \times P_e = \frac{8 M_{el}}{L_1 (2L_2 - L_1)} \quad (2a)$$

$$= \frac{8 \times 41,600 \times S}{L_1 (2L_2 - L_1)} \quad \text{\# / lineal inch} \quad (2b)$$

$$= \frac{332.8 \times S}{L_1 (2L_2 - L_1)} \quad K \text{ \# / lineal inch} \quad (3)$$

Figure IV-7

FIND:  $K_1$

$$\begin{aligned}
 K_1 &= \frac{R_{e1}}{X_{e1}} = \frac{27.33333 \times S}{(2L_2 - L_1)} \times \frac{I (2L_1 - L_1)}{.000346666 \times S \times (8L_2^3 - 4L_1^2L_2 + L_1^3)} \\
 &= \frac{27.33333 \times I}{.000346666 \times (8L_2^3 - 4L_1^2L_2 + L_1^3)} \\
 &= 80,000 \times \frac{I}{8L_2^3 - 4L_1^2L_2 + L_1^3}
 \end{aligned}$$

Check this formula for case where  $L_2 = L_1 = L$  (in feet)

$$\begin{aligned}
 K_1 &= 80,000 \times \frac{I}{8L^3 - 4L^3 + L^3} \\
 &= 80,000 \times \frac{I}{5L^3} = 16,000 \times \frac{I}{L^3}
 \end{aligned}$$

Formula checks.

# DERIVATION OF CONSTANTS $X_{el}$ , $R_{el}$ , and $K_1$

$w$  = Pressure  
Stress =  $\frac{M}{S}$

$b$  is in inches  
 $L$  is in feet  
 $b = 12 L$

or Moment = Stress  $\times$  Section Modulus = 41,600 S Inch-lbs.

$$\text{Also, Moment} = \frac{w \times b^2}{.8} = \frac{R \times b}{8} \quad (R - w \times b = \text{Resistance})$$

$$\text{or } R = w \times b = \frac{8 \times M}{b} = \frac{8 \times 41,600 \times S}{b}$$

$$\therefore X_{el} = \frac{5 \times w \times b^4}{384 EI} = \frac{(w b) (5 b^3)}{384 EI} = \frac{w b}{\frac{384 EI}{5 L^3}} = \frac{R \text{ (lbs.)}}{K_1 \text{ (lbs/in)}}$$

(Inches)

$$= \frac{8 \times 41,600 \times S \times 5 \times b^3}{b \times 384 \times E \times I} = \frac{8 \times 41,600 \times 5 \times b^2 \times S}{384 \times 30 \times 10^6 \times I}$$

$$= \frac{1,664,000 \times b^2 \times S}{11,520,000 I} = \frac{b^2 \times S}{.0001444 I} \quad \text{Inches}$$

$$\text{Or } X_{el} = \frac{.0001444 (12L)^2 \times S}{12 \times I} = .0001444 \times 12 \times \frac{L^2 \times S}{I}$$

(Feet)

$$= .0017333 \times \frac{L^2 \times S}{I} \quad \text{Feet}$$

$$t_y = \text{Stress}_{el} = \frac{M}{S} \quad R_{el} = w_{el} \times L \quad w_{el} L^2 = R_{el} \times L \quad (L \text{ is in feet})$$

$$M = f_{dy} \times S = 41.6 \times S \quad K\text{-Ft.}$$

$$wb^2 = 8M$$

$$R_{el} = \frac{8 \times M}{L} = \frac{8 \times 41.6 \times S}{L \times 12} = \frac{8 \times 41.6}{12} \left( \frac{S}{L} \right) = 27.7333 \frac{1}{3} \left( \frac{S}{L} \right) \quad K - \#$$

$$K_1 = \frac{384 \times E \times I}{5 \times L^3} = \frac{384 \times 30 \times 10^6 \times I}{5 \times (12 L)^3}$$

$$= \frac{384 \times 30 \times 10^6 \times I}{5 \times 12^3 \times L^3} = 1,333,333 \frac{1}{3} \left( \frac{I}{L^3} \right) \quad \#/\text{In.}$$

$$= 1,333 \frac{1}{3} \times \left( \frac{I}{L^3} \right) \quad K/\text{In.} \quad (\text{Divided by 1,000})$$

$$= 16,000 \left( \frac{I}{L^3} \right) \quad K/\text{Ft.} \quad (\text{Divided by 12})$$

$$\text{Also, } K_1 = \frac{R_{el}}{x_{el}} = \frac{27.7333 \times S}{L} \times \frac{I}{.0017333 \times L^2 \times S}$$

$$= \frac{27.7333}{.001733} \times \frac{I}{L^3} = 16,000 \left( \frac{I}{L^3} \right) \quad (\text{Checks with above derivation})$$

# SOLID STEEL PLATE DOOR

## DERIVATION OF CONSTANTS $R_{el}$ and $X_{el}$

Bending Moment = Section Modulus  $\times$  Unit Stress

$f_{dy}$  = Dynamic Yield Stress - 41.6 K for A-7 Steel

$a$  = Short span in inches       $b$  = long span in inches

$q$  = Elastic unit pressure

$\beta$  = Timoshenko constant

$$1. \text{ Elastic Moment (for 1" width)} = M_{el} = \frac{1 \times t^2}{6} \times f_{dy} = \frac{41.6}{6} t^2 = 6.933 t^2 - K \text{ in/lb.}$$

$$\text{Also, } M_{el} = \beta \times a^2 * \quad \text{or} \quad = \frac{M_{el}}{\beta \times a^2} = \frac{6.933 \times t^2}{\beta \times a^2} - K \text{ Lb./sq. in.}$$

$$\begin{aligned} \therefore \text{ Total Elastic Resistance} = R_{el} &= q \times \text{Area} \\ &= \frac{6.933 \times t^2 \times b \times a}{\beta \times a^2} = \frac{6.933 \times t^2 \times b}{\beta \times a} - Kip \end{aligned}$$

\* Timoshenko "Plates & Shells" p. 133

2. Elastic Deflection =  $X_{el} = \frac{\alpha \times a^4 \times q}{E \times t^3}$  \*

$q = \frac{6.933 \times t^2}{\beta \times a} - \text{Kip Lb/sq. in.}$

$\alpha$  = Timoshenko Constant

$\beta$  = Timoshenko Constant

$t$  = thickness in inches

$a$  = Short span of door in inches

$b$  = Long span of door in inches

$$\begin{aligned}
 X_{el} &= \frac{\alpha \times a^4 \times 6.933 \times t^2}{30 \times 10^6 \times t^3 \times \beta \times a^2} = \frac{\alpha \times a^2 \times 6.933}{30 \times 10^6 \times t \times \beta} \text{ Kip-Inches} \\
 &= \frac{6.933 \times \alpha \times a^2 \times 10^3}{30 \times 10^6 \times t \times \beta \times 12} \text{ Feet} \\
 &= \frac{6.933 \times \alpha \times a^2}{360 \times 10^3 \times t \times \beta} \text{ Feet}
 \end{aligned}$$

\* Timoshenko "Plates and Shells" p. 133

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